Active Power Filtering Implementation Using Photovoltaic System with Reduced Energy Storage Capacitor

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Abstract—A novel three-phase active power filter (APF) circuit with photovoltaic (PV) system to improve the quality of service and to reduce the capacity of energy storage capacitor is presented. The energy balance concept and sampling technique were used to simplify the calculation algorithm for the required utility source current and to control the voltage of the energy storage capacitor. The feasibility was verified by using the Pspice simulations and experiments. When the APF mode was used during non-operational period, not only the utilization rate, power factor and power quality could be improved, but also the capacity of energy storage capacitor could spare. As the results, the advantages of the APF circuit are simplicity of control circuits, low cost, and good transient response.

Keywords—active power filter, sampling, energy-storage capacitor, harmonic current, energy balance.

I. INTRODUCTION

POWER electronics circuits are widely used in many different types of industrial equipment, such as frequency changers, motor drive systems, etc. This equipment presents nonlinear impedance to the utility, generating large harmonic currents with well known negative effects, such as a low power factor, low efficiency and destruction of other currents with known negative effects, such as a low nonlinear impedance to the utility, generating large harmonic currents. Capacitors were used to suppress the harmonics. Capacitors were used to compensate the lag power factor. However, they have many disadvantages, such as large size, resonance, and fixed compensation characteristics [1, 2]. Therefore, conventional passive power filter can not provide a complete solution.

Many specialists approach the solution from the viewpoint of preventing the generation of harmonics, such as high power factor switching power supply, frequency changer and uninterruptible power supply (UPS) etc. [3-7] However, the present harmonic pollution sources, still need to be improved. Some APF methods have been proposed to compensate for the present harmonic loads. They are in the type of parallel with the non-linear load to provide the reactive power and to compensate for the harmonic current, in order to achieve the goal of high quality of service of utility sources [8-14].

Due to the limitations of sunshine, the average operating time of a PV system is only 6–8 hours. Hence, the equipment of a PV system operates at a low utilization rate. If the system is transferred to the APF operation mode during non-operational moments, so that the utilization rate, power factor and power quality can be improved [15].

This paper proposes a new three-phase active power filter (APF) technique, based on the concept of energy balance. At the end of each period, we use a sampling technique to detect the energy deviation of the energy-storage capacitor and to calculate the peak value of utility command current at the end of each period. By employing a set of a three-phase sinusoidal reference voltage in phase with the utility source to multiply with this peak value, we can obtain the required utility source current. The difference between the instantaneous load current and this current is the command current for the APF. This command current includes reactive fundamental power and harmonics. The current is provided by a bilateral converter using a hysteresis current control technique [16-20].

Because the instantaneous fundamental reactive power of a balanced three-phase system is zero, the instantaneous fundamental reactive power transfers only among phases. In theory, the required capacity of the energy-storage capacitor is zero. But, harmonics power transfers between the load and the energy-storage capacitor (charging and discharging), hence we still need to use a small capacitance for the energy-storage, and the average capacitor voltage can be maintained at a constant value. However, due to the losses in the converter such as switching loss, capacitor leakage current etc., the utility must provide not only the real power needed by the load but also these overhead required by converter to maintain the capacitor voltage at a prescribed value.

In this paper, a new DC bus voltage controller, using the energy balance concept, is proposed. As there is no delay element (such as LPF or PI control) used in this control circuit, and the transient response is fast and good.
II. PRINCIPLES OF OPERATION

A. System description

The basic circuit configuration of a utility interactive PV system is shown in Fig. 1. The battery bank of a DC bus is replaced by a capacity due to less power storage in the DC bus. The system configuration is the same as APF except for the DC converter stage. DC converter stage will be disabled and the system will be transferred to APF mode during non-operation duration. The Fig. 1(a) shows the utility interaction PV system operates on generation mode, and the Fig. 1(b) shows the system operates on APF mode.

\[ v_{L,k}(t) = V_{sm} \Re e^{j(\omega t - \frac{k\pi}{2})}, \quad k = -1, 0, \text{ and } 1 \]  

If a nonlinear load is applied, then the load current will consist of the fundamental component and all the higher order harmonics. It can be represented as

\[ i_{L,k}(t) = \sum_{n=1}^{\infty} I_{n,k} \Re e^{j(n(\omega t - \frac{k\pi}{2}) + \phi_k)}, \quad k = -1, 0, \text{ and } 1 \]

Therefore, the three-load power can be expresses as

\[ p_{\text{load}}(t) = \frac{1}{3} V_{sm} i_{L,k}(t) \times i_{L,k}(t) \]

\[ = \frac{3}{2} V_{sm} I_{L,1} \cos \theta_1 + \frac{1}{2} \sum_{k=-1}^{0} \sum_{n=2}^{\infty} I_{n,k} \Re e^{j(n(\omega t - \frac{k\pi}{2}) + \phi_k)} + V_{sm} I_{L,2} \Re e^{j(2\omega t - \frac{2\pi}{3})} \]

\[ + V_{sm} I_{L,3} \Re e^{j(2\omega t - \frac{2\pi}{3})}, \]

where \( k = -1, 0, \text{ and } 1 \)

In eq.(3), the first term is the real power supplied by the utility source, the second term is the reactive power, and the third term is the harmonic power. The last two terms are supplied by the APF. For a balanced three phase system, the second item is zero, i.e.

\[ p_{\text{load}}(t) = P_s + P_{\text{total,c}}(t) \]

\[ P_s = \frac{3}{2} V_{sm} I_{L,1} \cos \theta_1 = \frac{3V_{sm}I_m}{2} \]

\[ P_{\text{total,c}}(t) = V_{sm} \sum_{k=-1}^{0} \sum_{n=2}^{\infty} I_{n,k} \Re e^{j(n(\omega t - \frac{k\pi}{2}) + \phi_k)} \]

As the APF provides the harmonic power \( P_{\text{total,c}} \), the current supplied by the utility will be

\[ i_{L,k}(t) = I_m \Re e^{j(\omega t - \frac{k\pi}{2})} \]

where

\[ I_m = \frac{2P_s}{3V_{sm}} = I_{L,1} \cos \theta_1 \]

The current \( i_{L,k}(t) \) is in phase with the utility voltage and is pure sinusoidal. Therefore, The APF must provide the compensation current.

\[ i_{c,k}(t) = i_{L,k}(t) - i_{n,k}(t) \]
Hence, the APF needs to calculate the current \( i_{s,k}(t) \) accurately and instantaneously as described in the following.

### B. Calculation of fundamental component \( i_{s,k}(t) \)

For a three-phase APF in a steady state, the energy transformations are shown in Fig. 3.

![Fig. 3 The energy transfers in APF](image)

The power consumption of the load is

\[
P_L = \frac{V_{DC}^2}{R_L}
\]

(10)

This power will be provided by the utility source. Because the reactive power and harmonic power are supplied by APF, the utility only needs to supply the pure sinusoidal current and in phase with the utility voltage (i.e. \( pF=1.0 \)). The power supplied by the utility is

\[
P_L = \frac{3V_{sm}I_m}{2}
\]

(11)

where

\[
I_m = \frac{V_{DC}^2}{R_L} \cdot \frac{2}{3V_{sm}}
\]

(12)

In theory, the energy-storage capacitor does not need to provide real power to the load. Therefore, at the end of one complete utility cycle, the terminal voltage of storage energy converter will keep no change. However, owing to the switching loss and conductive loss of the power converter, the utility must provide not only the real power needed by the load (i.e. the in phase pure sinusoidal current \( i_{s,k}(t) \)), but also the additional power required by the converter to maintain the capacitor voltage at the presribed value.

The change of energy-storage capacitor in one period will be

\[
\Delta E_c = \frac{1}{2} C_c (V_{ref}^2 - V_c^2)
\]

(13)

where

\( V_{ref} \) the reference voltage of the energy-storage capacitor in steady state

\( V_c \) the voltage of the energy-storage capacitor at the end of each utility period.

If the energy loss of the capacitor can be compensated to the set value desired at the end of the next utility cycle by the extra utility current \( \Delta I_m \sin \omega t \), then in this cycle the energy compensated by the utility will be

\[
\Delta E_c = \frac{3}{T} \int_0^T (V_{sm} \sin \omega t \times \Delta I_m \sin \omega t) dt = \frac{3V_{sm} \Delta I_m}{2} \times T
\]

(14)

Based on the concept of energy balance, the compensation energy from the utility must equal to the energy loss of the energy-storage capacitor, i.e. \( \Delta E_c = \Delta E_c \). Therefore, in the next period the variation of the utility current is

\[
\Delta I_m = \frac{C_c (V_{ref}^2 - V_c^2)}{3V_{sm} T} = K(V_{ref}^2 - V_c^2)
\]

(15)

where \( K = \frac{C_c}{3V_{sm} T} \)

Keep in mind, this energy-loss is caused by the increment of load. If the utility makes only this variation of current, \( \Delta I_m \) it will just keep the capacitor voltage from not dropping again, and be unable to pull the capacitor voltage back to the reference level. For the capacitor voltage to return to its reference value \( V_{ref} \) at the end of the next cycle, the utility must provide \( 2\Delta I_m \) current variation in the next cycle (one \( \Delta I_m \) is for the load increment and other \( \Delta I_m \) is for the compensation of energy loss in the previous cycle).

Figure 4 shows the control block diagram of energy-storage capacitor voltage. The input is the terminal voltage of the capacitor. It follows an attenuation circuit \( (K_1) \) to adjust this voltage to an appropriate level \( (V_c/K_1) \). Then, it is connected to an isolation amplifier to isolate the main power circuit from the control circuit. The value of \( V_c^2 \) is calculated by a square circuit. The other input is the reference voltage \( (V_{ref}/K_1) \), it also follows a square circuit to calculate \( V_{ref}^2 \). The difference between \( (V_c/K_1)^2 \) and the set value \( (V_{ref}/K_1)^2 \) is multiplied by \( K_2 \) \( (K_2 = K_1^2 \times K) \) to get \( \Delta I_m \). This current \( \Delta I_m \) adds to the previous command current \( I_{UP1} \) to obtain the steady-state utility command current of this coming period, \( I_{UP} \). At the same time, one more \( \Delta I_m \) adds to the steady-state utility command current \( I_{UP} \), to get \( I_m \) \( (I_m = I_{UP} + \Delta I_m) \), and it will include the component to compensate the energy loss of the previous period. At the end of this coming period, the terminal voltage of energy-storage capacitor will return to \( V_{ref} \).

These values are sampled at the end of each period by the sample and hold the circuit to keep the value until the end of next period. Hence, during each period, the change of energy-storage capacitor voltage does not affect the compensation characteristics of the APF. That means the capacitor can endure a much larger voltage ripple. As the results, we can reduce the capacity of this capacitor.
The control block diagram of energy-storage capacitor voltage is shown in Fig. 4.

C. The current tracking circuit

The block diagram of current tracking and control circuit are shown in Fig. 5. The voltage of phase A, \( v_A(t) \), is connected to a zero cross detecting circuit (ZCD) to get a synchronous reference square wave. It will be used as the input of the phase lock loop (PLL). Using the PLL technique, we can get 256 times of the frequency of the utility source and the most significant bit of the frequency divider (Q7) which is synchronous with the utility source. The output of frequency divider of PLL (Q0~Q7) is used as the phase inputs of the three-phase sinusoidal reference voltage generator. The value of \( I_m \) is used as the reference voltage of the multiplier type digital to analog converter (DAC) to generate the utility command current \( i^*_m \).

D. Improvement of the transient response

In a balanced three-phase system, the summation of three-phase instantaneous reactive power is zero, which means the reactive power transfers only among phases. In the steady state, the energy-storage capacitor is not the same as the single-phase APF capacitor that must be provide large reactive power (reactive power transfers between load and converter). Therefore the energy-storage capacitor of three-phase APF can take a small size capacitor to operate. However, in practical experimental circuits, we use a 22\( \mu \)F capacitor for compensating the unbalance of line voltage, the unbalance of the load impedance and also the harmonic power. The test results show that under the condition of 2A load current, it has good compensation characteristics.

But, in the transient state, due to the command current of APF is calculated according to the utility current in a previous period, the extra current in current period will be supplied from the energy-storage capacitor. Using a smaller size of energy-storage capacitor, the loss of energy will make the terminal voltage of the energy-storage capacitor discharge rapidly. The capacitor voltage may drop to below the peak valve of the rectified utility \( V_{C-limit} \), as shown in Fig. 7. For example, when the load changes at \( t_1 \) (increasing load current), the capacitor voltage will discharge down to under the value of \( V_{C-limit} \). However, because the anti-parallelled diode of the power switching device (IGBT or power MOSFET), the capacitor voltage can not drop down to under the value of \( V_{C-limit} = \sqrt{2}V_{L,L} \). The voltage will keep at
\[ \sqrt{2}V_{L-L} \] until the start of next period, Since the value of \( \Delta V_C \), that is used for calculating the command current of the next period, is not in linear region (which shall be \( \Delta V_C^* \)), the variation of the utility current \( \Delta I_m \), that is calculated with eq.(15), is not correct. Hence it can not recharge the capacitor back to \( V_{ref} \) at the end of the new period. Therefore, in the transient state, the control circuit must be modified.

If we wish to recover the capacitor voltage to \( V_{ref} \) during the remaining time in this period, the utility command current must be increased by an amount of

\[ \Delta I_m = \frac{C_v(V_{ref}^2 - V_C^2)T}{(t_2 - t_1)\Delta V_{sc}(T - t_2)} = K'(V_{ref}^2 - V_C^2) \]  (17)

where

\[ K' = \frac{K T^2}{(t_2 - t_1)(T - t_2)} \]  (18)

Since the modified value of \( K' \) changes according to \( t_1 \) and \( t_2 \), it is difficult to implement in the hardware. If \( I_m \) is updated immediately, using the \( K' \) in eq.(18), it will be often too large and will push the control system into saturation. Furthermore, the capacitor voltage cannot drop down to under the value of \( V_{C-limit} \), hence we cannot accurately calculate the utility increment current directly from the capacitor voltage.

In practice, when the capacitor voltage drops down to below \( V_{low} \), the controller sends out the sampling signal for updating the utility command current, using original \( K \) in order to increase the utility current. Although, this current is smaller than the real need for the new load current, it can decrease the drop-down speed of the capacitor voltage. If the new \( I_m \) is updated at the rate of \( \frac{1}{t} \), this is equivalent to increasing the utility command current by \( \Delta I_m \) at every update time. Therefore, after \( n \) sampling pulses, it is equivalent to increasing the utility command current by \( n \times \Delta I_m \).

Eventually, the utility command current will be able to provide the energy needed for the new loading current. The capacitor voltage will be charged up from \( V_{C-limit} \) and return to the linear region again. Then the amount \( \Delta I_m \) decays progressively and the capacitor voltage will approach to \( V_{ref} \). After the capacitor voltage rises over \( V_{low} \), the system will be stayed in the linear region and the APF can work in steady-state during the next new period.

### E. Determination of energy-storage capacitor

When the voltage or the load of a three-phase system is in an unbalanced condition, the instantaneous summation of the line frequency volt-ampere supplied from the energy-storage capacitor is not equal to zero. Assuming that under the steady state condition, the volt-ampere which needs to be compensated is equal to \( S_{UB} \), then the maximum energy supplied by the capacitor will be equal to

\[ \Delta E_{UB,max} = S_{UB} \times \frac{T}{2} \]  (19)

If this energy output make the capacitor voltage drop down to \( V_{low} \), (i.e. \( V_{C-limit} \leq 0.2(V_{ref} - V_{C-limit}) \)), then...
\[ \Delta E_{UB,\text{max}} = \frac{1}{2} C_{C,UB}(V_{\text{ref}}^2 - V_{\text{low}}^2) \]  

(20)

\[ C_{C,UB} = \frac{S_{UB} \cdot T}{(V_{\text{ref}}^2 - V_{\text{low}}^2)} \]  

(21)

For example, if \( V_{L-L} = 220\text{V} \), \( S = 10 \text{kVA} \), \( S_{UB} = 10\% \times S = 1.0 \text{kVA} \), \( V_{C-\text{limit}} = 311\text{V} \), \( V_{\text{ref}} = 1.5 \times V_{C-\text{limit}} \), and \( V_{\text{low}} = 1.1 \times V_{C-\text{limit}} \), then \( C_{C,UB} = 165\mu\text{F} \), i.e., \( 6.25\mu\text{F/amp} \).

On the other hand, the power absorbed by the nonlinear load can be represented as [17]

\[ P_L(t) = \sum_{k=1}^{\infty} v_{i,k}(t) \sum_{k=1}^{\infty} i_{d,k}(t) = P_L + \tilde{P}(t) \]  

(22)

with

\[ P_L = \frac{3V_{\text{rms}} \cdot I_{L} \cdot \cos \phi}{2} \]  

(23)

\( P_L \) is the DC component relating to the real power consumed by the load.

\[ \tilde{P}_L(t) = \sum_{n=1}^{\infty} P_{n0} \cos(3n\omega t - \varphi_{3n}) \]  

(24)

For the six-pulse rectified load, the above equation will be expressed as

\[ \tilde{P}_L(t) = \sum_{n=1}^{\infty} P_{n0} \cos(6n\omega t - \varphi_{6n}) \]  

(25)

In this equation, the six-order harmonic will be the largest, and this six-order harmonic energy supplied by the capacitor will be

\[ P_{6,L} = \frac{T}{12} C_{C,\text{IR}}(V_{\text{ref}}^2 - V_{\text{low}}^2) \]  

(26)

i.e.

\[ C_{C,\text{IR}} = \frac{T \cdot P_{6,L}}{6(V_{\text{ref}}^2 - V_{\text{low}}^2)} \]  

(27)

As in the previous case, if we assume \( P_{6,L} = \frac{P_L}{2} \), then \( C_{C,\text{IR}} = 132\mu\text{F} \) (6\mu\text{F/amp}). If we consider the both cases simultaneously, then the capacitor value is suggested as.

\[ C_C = \sqrt{C_{C,UB}^2 + C_{C,\text{IR}}^2} \]  

(28)

F. Determination of the advanced sampling time interval \( \Delta t \)

Assuming the maximum allowed transient current of this control system to be \( \Delta I_m'' \), at this time \( t_2 \), the capacitor voltage drops down to the value of \( V_{C-\text{limit}} \). Therefore the control system will modify the utility command current, using the advanced sampling technique. Since the capacitor voltage already drops down to the value of \( V_{C-\text{limit}} \), the updated amount, \( \Delta I_m' \), for each sampling is constant. In the time duration of \( T-t_2 \), the total advanced modified amount of the utility command current will be

\[ \Delta I_m' + \Delta I_m' + \ldots + \Delta I_m' = \Delta I_m'' \]  

(29)

\[ n = \frac{\Delta I_m''}{\Delta I_m'} \]  

where

\[ \Delta I_m' = K(V_{\text{ref}}^2 - V_{c,\text{limit}}^2) \]  

(30)

Hence \( \Delta t \) will be determined as

\[ \Delta t = \frac{T - t_2}{n} \]  

(31)

III. SIMULATION AND EXPERIMENTAL RESULTS

Figure 9 shows the simulation results, using Pspice simulation software, assuming \( V_{\text{DC}} = 220\text{V} \), \( L = 1 \text{mH} \), \( C_C = 22\mu\text{F} \), \( I_{L,\text{DC}} = 10\text{A} \). To verify this control algorithm, we have made a small scale three-phase APF. The three-phase voltage reduces to 55 volts, with DC load \( R_L = 40 \text{ohm} \), \( L = 1\text{mH} \), and the energy-storage capacitor \( C_C = 22\mu\text{F} \). The capacitor reference voltage is set at 120V. The steady-state test results for \( I_{DC} = 1.0 \text{p.u.} \) are shown in Fig.10. The waveform of ch1 is the energy-storage capacitor voltage, ch2 is the utility current, ch3 is the converter output compensation current, and ch4 is the load current. The test results of transient response, using the advanced sampling technique, are shown in Fig.11. The load current varies between \( I_{DC} = 0.5 \text{p.u.} \) and \( I_{DC} = 1.0 \text{p.u.} \). When the load current increases from \( I_{DC} = 0.5 \text{p.u.} \) to \( I_{DC} = 1.0 \text{p.u.} \), the capacitor voltage drops down to \( V_{\text{low}} \) and the control circuit generates the sampling clock immediately to update the utility command current.
From the test results, we can see that the transient time is only one period. At the next new period, the system is already in steady-state. On the other hand, when the load current decreases from $I_{DC}=1.0$ p.u. to $I_{DC}=0.5$ p.u., the capacitor voltage is also kept in a reasonable range. Figure 12 shows the sampling clock of the proposed advanced sampling technique. From the test results, we can see that even we use a small size capacitor (11μf/amp) which may caused a large ripple; the compensation characteristics are still good enough.

IV. CONCLUSIONS

Due to the nonlinear load characteristics of much electronic equipment, the utility power system is polluted by harmonics and the power factor is decreased. In this paper, a new APF technique is proposed, using the sampling technique to simplify the calculation of the real fundamental component of the load current. In addition, the energy-balance concept in the energy-storage capacitor is used to simplify the design of the conventional APF capacitor voltage control circuit. The merits of this APF are: (1) Simplifying the calculation of the required utility source current $i_s(t)$, (2) A large ripple voltage can be tolerated in the energy-storage capacitor. Therefore, a smaller energy-storage capacitor is needed. (3) Only a proportional control method is applied in the controller design of the capacitor voltage. Hence the transient response is fast and good. The feasibility of the above scheme is verified by Pspice simulation and experimental results. The results demonstrate that the harmonics are suppressed and nearly unity power factor is obtained.
Fig. 11  The transient response test results for load current varies between $J_{DC}=0.5$ p.u. and $J_{DC}=1.0$ p.u.. (a) R load. (b) R-C load

Fig. 12  The sampling clock of the proposed advanced sampling technique

V. REFERENCES