Multi-Objective Optimization of a Solar-Powered Triple-Effect Absorption Chiller for Air-Conditioning Applications

Ali Shirazi, Robert A. Taylor, Stephen D. White, Graham L. Morrison

Abstract—In this paper, a detailed simulation model of a solar-powered triple-effect LiBr–H₂O absorption chiller is developed to supply both cooling and heating demand of a large-scale building, aiming to reduce the fossil fuel consumption and greenhouse gas emissions in building sector. TRNSYS 17 is used to simulate the performance of the system over a typical year. A combined energetic-economic-environmental analysis is conducted to determine the system annual primary energy consumption and the total cost, which are considered as two conflicting objectives. A multi-objective optimization of the system is performed using a genetic algorithm to minimize these objectives simultaneously. The optimization results show that the final optimal design of the proposed plant has a solar fraction of 72% and leads to an annual primary energy saving of 0.69 GWh and annual CO₂ emissions reduction of ~166 tonnes, as compared to a conventional HVAC system. The economics of this design, however, is not appealing without public funding, which is often the case for many renewable energy systems. The results show that a good funding policy is required in order for these technologies to achieve satisfactory payback periods within the lifetime of the plant.

Keywords—Economic, environmental, multi-objective optimization, solar air-conditioning, triple-effect absorption chiller.

I. INTRODUCTION

THE primary energy use in buildings has been dominated by conventional air-conditioning systems which contribute to about 40% of the greenhouse gas emissions in building sector [1], [2]. With the rising demand for indoor comfort, rising concerns about climate change and depletion of fossil fuel resources, finding an environmentally friendly and energy-efficient alternative to conventional air-conditioning systems is necessary [3]. Solar heating and cooling (SHC) absorption chillers are considered as one promising alternative to conventional air-conditioning systems since much of the technology has already been proven at commercial scales. Absorption chillers are mainly categorized by the number of effects which refer to the number of times the high temperature heat source is used by the chiller to produce cooling. Moving toward a higher effect cycle leads to higher chiller COPs, but in turn requires higher driving temperature. Single-effect chillers operate in the temperature range of 80 °C to 100 °C, achieving thermal COPs of up to 0.7-0.8 [4]. Double-effect chillers can achieve higher COPs up to 1.4, but require significantly higher driving temperatures of around 180 °C [5]. Having three cascading generators, triple-effect absorption chillers can produce cooling at even higher COPs of around 1.8, but require a very high-temperature heat source of 210-240 °C [6]. Such temperatures can be supplied by using high temperature concentrating collectors such as parabolic troughs.

Most of solar absorption chillers installed around the world are based on single-effect chillers and non-concentrating flat plate or evacuated tube collectors [7]–[10]. The major disadvantage to single-effect chillers is its low COP, which leads to a large collector area to supply the thermal heat demand of the chiller. Combining high-temperature solar thermal collectors and multi-effect absorption chillers can be more energy-efficient due to the higher COP of these chillers, resulting in less solar thermal energy and potentially less collector area to supply a given amount of cooling [11], [12]. Cabrera et al. [13] carried out a comprehensive literature review on the use of parabolic trough collectors (PTCs) in solar air-conditioning applications and summarized the existing experiences and realizations for the potential application of these collectors to drive double-effect absorption chillers. They found that the yearly installation rate of this type of systems is still low, but according to the market potential, this rate is expected to increase in the near future.

The potential of triple-effect absorption systems coupled with high-temperature solar thermal collectors have been studied by a few researchers [14], [15]. Although triple-effect absorption chillers have been around for a while, there has been no system-level modeling and optimization of these chillers coupled with high-temperature concentrating solar thermal collectors for air-conditioning applications. Motivated by this gap, this paper presents a detailed multi-objective optimization of a SHC triple-effect LiBr–H₂O absorption chiller, aiming to determine the optimal performance of the system from energetic, economic, and environmental perspective simultaneously. A complete dynamic simulation model of this system was developed in TRNSYS 17 [16], where its energy performance was evaluated. A detailed economic analysis was conducted to calculate the total levelized cost of the plant, including the capital cost, operating and maintenance cost, the fuel cost, and a penalty cost for CO₂ emissions. A multi-objective optimization approach using a genetic algorithm was
employed through coupling TRNSYS and MATLAB to determine the optimal design of the system. The optimization objectives were the primary energy consumption and the total levelized cost of the system, which were both minimized. Finally, a LINMAP decision-making method was used to determine the final optimal design of the system, which was compared to that of a reference conventional system.

II. SYSTEM DESCRIPTION

In this paper, PTCs were coupled with a triple-effect LiBr–H₂O absorption chiller in order to supply both cooling and heating demand of a large reference building. This improves the economics of the plant compared to those producing either chilled or hot water alone. It should be noted that PTCs are the only solar thermal collectors available on the market, which are capable of delivering temperatures greater than 210 °C with an acceptable thermal efficiency. As illustrated in Fig. 1, a gas burner is employed as the backup system, delivering heat to the chiller when solar-driven energy is not sufficient. The rate cooling capacity of the absorption chiller is selected in order to satisfy the maximum cooling load of the building.

The incident solar radiation absorbed by the collector arrays increases the temperature of the stratified hot water storage tank. A feedback controller is used to adjust the pump flow rate to achieve a fixed set-point temperature at the collector outlet. A pressure relief valve is used to limit the fluid outlet temperature to the maximum allowable value specified by the user as an input to the model. During cooling periods when the temperature at the top 75% of the storage tank is above the chiller’s required hot water temperature, only the solar heat source is used to drive the absorption chiller to produce chilled water for space cooling. Once the temperature at the top of the tank drops below the required value at the chiller’s generator, the gas burner is switched on to supply the entire cooling demand of the building. The chilled water produced by the chiller is delivered to the cooling fan coil using a fixed flow pump to satisfy the required building cooling load. The chiller is also connected to a cooling tower loop to remove heat from its absorber and condenser into the ambient. During heating periods, the hot water stored in the tank is directly delivered to the heating fan coil unit to cover the building heating load. Similarly, if the temperature of the storage tank drops below the required temperature for the distribution system, the gas burner is turned on to satisfy the entire heating load.

A conventional air-conditioning system, consisting of a vapor compression mechanical chiller and a gas-fired heater, is considered here as a reference system to compare the performance of the proposed solar triple-effect absorption chiller from energetic, economic, and environmental viewpoints.

III. SYSTEM SIMULATION

The proposed SHC absorption chiller system was modeled in TRNSYS 17 [16], which is commonly used for simulation of transient thermal systems. The following details the mathematical model of the key system components.

A. Parabolic Trough Solar Collector

The useful heat collected from a PTC module \( Q_{u,SC} \) can be calculated as [17]:

\[
Q_{u,SC} = \dot{m}_u c_p u (T_{SC,\text{out}} - T_{SC,\text{in}})
\]

\[
F'U_L = c_1 + c_2 (T_{avg} - T_a)
\]

where \( F'(\tau_0) \) is the collector zero loss efficiency at normal incidence, \( K_{0h} (0) \) and \( G_b \) denote the collector efficiency factor and overall heat loss coefficient, and \( A_s \) and \( CR_{SC} \) are the collector aperture area and concentration ratio. The terms \( c_1 \) and \( c_2 \) are the first and second order heat loss coefficients, and \( T_{avg} \) and \( T_a \) are the average temperature of the collector working fluid and ambient temperature, respectively. A new type (labelled ‘Type 237’) was developed to simulate the performance of the PTC module in TRNSYS environment. The design parameters used for this type are representative of NEP Polytrough 1800 [18], which are summarized in Table I.

B. Hot Water Storage Tank

A TRNSYS ‘Type534’ TESS model [19] was used to simulate the performance of the stratified storage tank in this study. The tank was assumed to have 10 thermal stratification nodes, an aspect ratio of 3.5 [20], and a heat loss coefficient of 0.833W/m²K. More details about the mathematical model of the tank can be found in TRNSYS TESS Library documentation [19].

C. Solar-Gas Heat Source Controller

Combining the mathematical equations of ‘Type 6’ (an auxiliary gas-fired heater) and ‘Type 11 (a tee-piece) from the TRNSYS standard library with some control-logic necessary to switch between solar and gas modes, a new TRNSYS type (labelled ‘Type 223’) was developed to model the solar-gas heat source component. The outlet temperature of the heater...
can be determined by [21]:

\[ T_{\text{AH,out}} = T_{\text{AH,in}} + \frac{\dot{Q}_{\text{AH}} - \dot{Q}_{\text{loss,AH}}}{m_w \cdot c_{p,w}} \]  

(3)

where \( \dot{Q}_{\text{AH}} \) and \( \dot{Q}_{\text{loss,AH}} \) are the burner heating rate and heat losses through the burner, respectively.

### TABLE I
**Performance Parameters of the PTC Used in This Study** [18]

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aperture area</td>
<td>m²</td>
<td>18.45</td>
</tr>
<tr>
<td>Max operating pressure</td>
<td>bar</td>
<td>40</td>
</tr>
<tr>
<td>Test flow rate</td>
<td>L/h m²</td>
<td>75.9</td>
</tr>
<tr>
<td>Collector azimuth</td>
<td>°</td>
<td>0</td>
</tr>
<tr>
<td>Concentration ratio</td>
<td></td>
<td>54</td>
</tr>
<tr>
<td>( F'_{\text{cin}} )</td>
<td></td>
<td>0.689</td>
</tr>
<tr>
<td>( c_1 )</td>
<td>W/m² K</td>
<td>0.36</td>
</tr>
<tr>
<td>( c_2 )</td>
<td>W/m² K²</td>
<td>0.0011</td>
</tr>
</tbody>
</table>

#### D. Absorption Chiller

The triple-effect absorption chiller was modeled using the adapted characteristic equation method capable of predicting the chiller’s performance by using two algebraic equations to calculate the chiller cooling capacity and the driving heat input as functions of a term called \( \Delta \Delta T' \) [22]. \( \Delta \Delta T' \) can be expressed as:

\[ \Delta \Delta T' = T_G + a \times T_{\text{AC}} + e \times T_E \]  

(4)

where \( T_G, T_{\text{AC}}, \) and \( T_E \) are the average temperature of the external heat carrier fluids at the generator, absorber-condenser, and evaporator. The characteristic equations for the cooling capacity and driving heat of the chiller are defined as:

\[ \dot{Q}_{\text{E}} = s_e \Delta \Delta T' + r_e \]  

(5)

\[ \dot{Q}_{\text{G}} = s_G \Delta \Delta T' + r_G \]  

(6)

The characteristic coefficients (i.e., \( a, e, s_e, r_e, s_G, \) and \( r_G \)) are determined using multiple linear regression algorithms applied to a set of performance data points given by the chiller manufacturer. The heat removal rate from the absorber and condenser and the chiller COP can be determined by:

\[ \dot{Q}_{\text{AC}} = \dot{Q}_E + \dot{Q}_G + \dot{Q}_{\text{aux}} \]  

(7)

\[ \text{COP} = \frac{\dot{Q}_E}{\dot{Q}_G + \dot{Q}_{\text{aux}}} \]  

(8)

where \( \dot{Q}_{\text{aux}} \) is the energy consumption of the absorption chiller pump. Based on this method, a TRNSYS type (labelled ‘Type 220’) was developed to simulate the performance of the absorption chiller. The triple-effect chiller was selected from Thermax Ltd [23], and its technical specifications at rated conditions are summarized in Table II.

#### Table II
**Technical Specifications of the Triple-Effect Absorption Chiller Used in This Study**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>CHW temperature (inlet/outlet)</td>
<td>°C</td>
<td>12/7</td>
</tr>
<tr>
<td>CW temperature (inlet/outlet)</td>
<td>°C</td>
<td>30/37</td>
</tr>
<tr>
<td>HW temperature (inlet/outlet)</td>
<td>°C</td>
<td>210/195</td>
</tr>
<tr>
<td>CHW flow rate</td>
<td>m³/hr kWₑ</td>
<td>0.172</td>
</tr>
<tr>
<td>CW flow rate</td>
<td>m³/hr kWₑ</td>
<td>0.191</td>
</tr>
<tr>
<td>HW flow rate</td>
<td>m³/hr kWₑ</td>
<td>0.032</td>
</tr>
<tr>
<td>COP</td>
<td></td>
<td>1.81</td>
</tr>
</tbody>
</table>

#### E. Vapor Compression Chiller

A water-cooled vapor compression chiller was employed in the reference conventional system to provide the building cooling load. TRNSYS ‘Type 666’ was used to model the performance of the chiller. The detailed mathematical model of this type can be found in TRNSYS documentation [24].

#### F. Cooling Tower

An open circuit cooling tower was used to reject heat from the chiller to the ambient. TRNSYS ‘Type51b’ was used to simulate the performance of the cooling tower. More details about the mathematical model of this type can be found in TRNSYS documentation [21].

#### G. Building Load

The building considered in this paper represents a large hotel consisting of 6 floors and a basement with total floor area of 11,346 m². The building has an average window-to-wall ratio of 30.2% in total. The building walls and fabric were designed to meet minimum requirements provided by the Building Code of Australia [25]. The thermal behavior of the building was simulated using multi-zone building model ‘Type 56’ and the weather data module ‘Type 15-2’ in TRNSYS.

### IV. ENERGETIC ANALYSIS

The energy performance of the proposed SHC triple-effect chiller is analyzed by the primary energy consumption of the plant (PECₜₚₜₜ):

\[ \text{PEC}_{\text{SHC}} = \text{PEC}_{\text{SHC,E}} + \text{PEC}_{\text{SHC,NG}} \]  

(9)

\[ \text{PEC}_{\text{SHC,E}} = \text{PEF}_E \times E_E \]  

(10)

\[ \text{PEC}_{\text{SHC,NG}} = \text{PEF}_{\text{NG}} \times E_{\text{NG}} \]  

(11)

\( E_E \) and \( E_{\text{NG}} \) are the annual energy consumed by the electric equipment and the auxiliary gas burner. \( \text{PEF}_E \) and \( \text{PEF}_{\text{NG}} \), respectively, denote the primary energy conversion factors for electricity grid and natural gas, which are presented in Table III.
V. Economic Analysis

The levelized annual total cost of the plant \(C_{\text{tot,L}}\) consists of four main elements: the capital investment \(\text{CI}_L\), the operating and maintenance cost \(\text{OMC}_L\), the fuel cost \(\text{FC}_L\), and the pollution cost due to CO\(_2\) emissions \(\text{CDE}_L\): \[ C_{\text{tot,L}} = \text{CI}_L + \text{OMC}_L + \text{FC}_L + \text{CDE}_L \] (12)

The input parameters used for the economic analysis of the proposed SHC absorption system are summarized in Tables III and IV [26]–[28].

\[ \text{CDE}_{\text{SHC}} = \text{CDE}_{\text{SHC,E}} + \text{CDE}_{\text{SHC,NG}} \] (14)

\[ \text{CDE}_{\text{SHC,E}} = E_E \times \text{EF}_{\text{CO}_2,E} \] (15)

\[ \text{CDE}_{\text{SHC,NG}} = E_{\text{NG}} \times \text{EF}_{\text{CO}_2,\text{NG}} \] (16)

where \(\text{EF}_{\text{CO}_2,E}\) and \(\text{EF}_{\text{CO}_2,\text{NG}}\) are the CO\(_2\) emission factors for grid electricity and natural gas, which are listed in Table III.

VII. System Optimization

Multi-objective optimization is a realistic approach to handle real-world engineering problems dealing with conflicting objectives which must be addressed simultaneously. In a multi-objective optimization problem, a set of non-dominated solutions, known as Pareto optimal solutions, is obtained, which represents a hierarchy of best possible trade-offs between the considered objective functions [30]. Genetic algorithms have been proven to provide a robust and efficient approach to achieve a set of reliable global optimal solutions to a multi-objective optimization problem [31]. As such, TRNSYS was coupled with MATLAB in the present study, using its genetic algorithm optimization toolbox to perform the multi-objective optimization of the system. The primary energy consumption and the total annual cost of the SHC plant were selected as two conflicting objective functions to be minimized simultaneously. Five design parameters were selected for the system optimization, which are presented in Table V. It should be noted that the lower and upper bounds of the collector specific area \((A_{\text{SC,\text{min}}} \text{ and } A_{\text{SC,\text{max}}})\) were selected in a way to limit the total solar fraction of the plant between \(-25\% \text{ and } -90\%\).

VIII. Results and Discussion

To demonstrate the modeling and optimization methodology described above, a case study was developed for the proposed SHC plant integrated into the modeled reference hotel building in Sydney, Australia, a location with relative...
sunny climate with annual global horizontal and beam irradiance of about 1608.5 kWh/m² and 853.9 kWh/m², respectively [32]. The annual cooling and heating load profile of the building under Sydney’s climate is shown in Fig. 2.

TABLE V
DESIGN PARAMETERS CONSIDERED FOR SYSTEM OPTIMIZATION

<table>
<thead>
<tr>
<th>Design parameter</th>
<th>Unit</th>
<th>Range of variation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Solar collector specific area (ASC)</td>
<td>m²/kWc</td>
<td>ASC,min &lt; ASC &lt; ASC,max</td>
</tr>
<tr>
<td>Storage tank specific volume (VST)</td>
<td>L/m²</td>
<td>10 &lt; VST &lt; 100</td>
</tr>
<tr>
<td>Solar pump nominal flow rate (m₁,nominal)</td>
<td>L/hr m²</td>
<td>49 &lt; m₁,nominal &lt; 195</td>
</tr>
<tr>
<td>Collector set-point temperature in summer (TSP,s)</td>
<td>°C</td>
<td>190 &lt; TSP,s &lt; 220</td>
</tr>
<tr>
<td>Collector set-point temperature in winter (TSP,w)</td>
<td>°C</td>
<td>70 &lt; TSP,w &lt; 100</td>
</tr>
</tbody>
</table>

The maximum cooling and heating demands of the building are 965 kW and 520 kW, respectively. Accordingly, a triple-effect absorption chiller with a nominal cooling capacity of 1163 kW was selected from Thermax Ltd. The characteristic coefficients obtained for this chiller are:

\[ a = -2.14, \quad e = 3.29, \quad s_E = 14.6, \quad t_E = -1171.7, \quad s_G = 7.05, \quad \text{and} \quad r_G = -504.2 \]

Fig. 2 Monthly load demand of the reference hotel building modeled in this study under Sydney’s climate

The Pareto front of optimal solutions obtained from multi-objective optimization of the system is shown in Fig. 3. As mentioned earlier, the conflicting relation between the two objective functions is evident in this figure. The lowest primary energy consumption (and thus the minimum environmental impact) is achieved at design point A, while the total levelized cost has its highest value at this point. The highest primary energy consumption occurs at design point B, where the system total cost stands at its minimum. If the primary energy consumption was considered as the sole objective function, point A then would represent the optimal design point of the system. In other words, point A shows an extreme design where the solar energy source is most weighted to contribute to meeting the load requirements of the buildings. Were the plant levelized cost to be the sole objective in the optimization process, then point B would be preferred as the optimum design. Fig. 3 also shows the levelized cost and the primary energy consumption corresponding to the reference conventional system operating under the same conditions. As can be seen in this figure, all optimal solutions corresponding to SHC plant outperform the conventional system, proving the acceptable energy efficiency of a gas-fired backup when used with a high-COP triple-effect chiller-based design.

To comprehensively analyze the energetic/environmental and economic performance of the proposed SHC plant, a final optimal solution should be selected from the Pareto front presented in Fig. 3. Since the dimension of the objective functions considered in this study is not the same (i.e. PEC in GWh/year and Ctot,L in MS/year), all objectives must be non-dimensionalized first. The Euclidian technique was therefore used to non-dimensionalize the vectors of objectives in the present work. More details about this method can be found in [33].

Assuming equal weights assigned to both objective functions, a LINMAP decision-making method was employed to determine the final optimal design point of the SHC plants. In this method, an ideal point is defined at which both objectives are at their optimal values independent of the one another [34]. The solution with a minimum spatial distance from the ideal point is selected as the desired optimal solution, which is marked in Fig. 3. It should be noted that in general no decision-making method has superiority over the other; thus, selection of the final optimal design point merely depends on the importance of each objective function to the designer under certain circumstances. The optimal values of design parameters corresponding to the final optimal point as well as points A and B are presented in Table VI. As shown in this table, the final optimal point selected by LINMAP decision-maker has reached an equal trade-off between the energetic, economic and environmental performance of the system.

The capital cost breakdown of the SHC plant at the final optimal design point is shown in Fig. 4. According to this figure, the solar collector array has the highest share of the capital cost, accounting for about 43% of the total capital cost of the plant. The absorption chiller is the second most expensive component in each configuration, comprising 25% of the total capital cost of the plant. The next highest capital costs can be attributed to the storage tank, cooling coils, cooling tower, and heating coils.
The results presented in Table VII show that the proposed SHC plant at its final optimal design point has a solar fraction of 72%, achieving an annual primary energy saving of 0.69 GWh and saving ~166 tonnes of CO2 emission as compared to the reference conventional system. Nevertheless, based on today’s market the economic performance of the proposed SHC plant does not seem satisfactory without government subsidies, which is often the case for many renewable energy systems. The low competitive economics of the proposed SHC system relative to conventional HVAC systems is mainly due to the high capital costs of concentrating high-temperature solar collectors. In addition, the lower solar gain of concentrating PTCs due to capturing only beam radiation leads the plant to have larger collector areas to compensate for the loss of diffuse component, thereby increasing the capital cost of the solar field.

If 50% of the capital cost of the plant was financed by subsidies, the payback period of the SHC plant at the final optimal design presented in Table VI would drop just above the lifetime of the plant (~21 year), which is still unacceptable from an economic perspective. Increasing the financial incentive up to 75%, the proposed SHC plant can achieve a satisfactory payback time of about 6 years. Since such high rates of financial incentives may not always be available from public funding, another approach to improve the economics of the proposed SHC system with less reliance on public subsidies is to size the solar field to achieve lower solar fractions. In other words, the solar collector field can be (under) sized for high base load utilization, while the backup heating and cooling energy source covers the remaining more variable part of the overall building thermal load. As a case in point, for an optimal design point which has a solar fraction of about 40%, only 32% subsidies on the capital costs (of the innovative components) is required in order for the additional capital costs (compared to the reference conventional system) to be recovered in ~9 years. Thus, based on the current market the economically viable design of the proposed SHC plant is better understood as a gas-driven system with solar enhancement rather than a solar-powered system with gas cooling and heating back-up. Overall, with increasing maturity, the SHC absorption technology will likely become more competitive with conventional systems for air-conditioning applications.

IX. CONCLUSIONS

A comprehensive energetic, economic, and environmental analyses and multi-objective optimization of a novel solar-powered triple-effect LiBr–H2O absorption chiller was carried out to evaluate the techno-economic potential of such systems for air-conditioning applications. PTCs were employed to drive the triple-effect chillers, while a gas burner was used as backup when solar heat was not sufficient. A complete dynamic simulation model of the proposed SHC plant was developed in TRNSYS program, which was coupled with MATLAB to perform the multi-objective optimization of the system, where the primary energy consumption and levelized annual total cost of the plant were minimized simultaneously. Overall, the multi-objective approach of this study satisfied both primary energy and economic and performance objectives better than single-objective optimizations alone. The optimization results indicated that the final optimum design of the proposed SHC system results in a solar fraction of 72%, achieving an annual primary energy saving of 0.69 GWh and saving ~166 tonnes of CO2 emission as compared to
a reference conventional system. The economic performance of the system, however, was not appealing, mainly due to the high capital cost of concentrating PTCs required to drive the triple-effect chiller. It was found that ~75% public funding was required in order for the proposed SHC system to achieve a satisfactory payback period of ~6 years. Finally, our results showed that if some small amount of government subsidies is available, the solar field can be sized to achieve lower solar fractions to improve the economic feasibility of such systems. This means that the most economically viable design (today) is one in which the SHC absorption chillers are used as an enhancement to the conventional system, rather than attempting to rely mostly on solar-derived heat. Overall, the challenge for the solar industry is to lower the cost of high temperature collectors, thereby paving the way for implementation of highly-efficient triple-effect chiller systems integrated with solar thermal energy.

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