## Pairwise Relative Primality of Integers and Independent Sets of Graphs


#### Abstract

Authors: Jerry Hu Abstract : Let $\mathrm{G}=(\mathrm{V}, \mathrm{E})$ with $\mathrm{V}=\{1,2, \ldots, \mathrm{k}\}$ be a graph, the k positive integers $\mathrm{a}_{1}, \mathrm{a}_{2}, \ldots$, ak are G -wise relatively prime if ( $\mathrm{a}_{\mathrm{i}}$, $\left.a_{j}\right)=1$ for $\{i, j\} \in E$. We use an inductive approach to give an asymptotic formula for the number of k-tuples of integers that are G-wise relatively prime. An exact formula is obtained for the probability that $k$ positive integers are $G$-wise relatively prime. As a corollary, we also provide an exact formula for the probability that $k$ positive integers have exactly $r$ relatively prime pairs.


Keywords : graph, independent set, G-wise relatively prime, probability
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