

## On the Girth of the Regular Digraph of Ideals of a Commutative Ring

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**Abstract :** Let  $R$  be a commutative ring. The regular digraph of ideals of  $R$ , which is denoted by  $\Gamma(R)$ , is a digraph whose vertex-set is the set of all non-trivial ideals of  $R$  and, for every two distinct vertices  $I$  and  $J$ , there is an arc from  $I$  to  $J$ , whenever  $I$  contains a non-zero-divisor on  $J$ . In this article, we show that an indecomposable Noetherian ring  $R$  is Artinian local if and only if  $Z(I)=Z(R)$  for every non-nilpotent ideal  $I$ . Then we conclude that the girth of  $\Gamma(R)$  is not equal to four.

**Keywords :** commutative ring, girth, regular digraph, zero-divisor

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