# Optimization of $CO_2$ Emissions and Cost for Composite Building Design with NSGA- $\Pi$

Ji Hyeong Park, Ji Hye Jeon, and Hyo Seon Park

**Abstract**— Environmental pollution problems have been globally main concern in all fields including economy, society and culture into the 21<sup>st</sup> century. Beginning with the Kyoto Protocol, the reduction on the emissions of greenhouse gas such as  $CO_2$  and  $SO_x$  has been a principal challenge of our day. As most buildings unlike durable goods in other industries have a characteristic and long life cycle, they consume energy in quantity and emit much  $CO_2$ . Thus, for green building construction, more research is needed to reduce the  $CO_2$ emissions at each stage in the life cycle. However, recent studies are focused on the use and maintenance phase. Also, there is a lack of research on the initial design stage, especially the structure design. Therefore, in this study, we propose an optimal design plan considering  $CO_2$  emissions and cost in composite buildings simultaneously by applying to the structural design of actual building.

*Keywords*—Multi-objective optimization, CO<sub>2</sub> emissions, structural cost, encased composite structure

## I. INTRODUCTION

WITH the progress of material civilization and rapidly industrialization, environmental pollution problems are getting very serious recently. Beginning with the Kyoto Protocol in 1997, environmental preservation has been a shared challenge all over the world, not the specific countries. In all fields of industry, various efforts have been made for reducing the environmental load.

In particular, in the construction industry, a representative environmental polluting industry, various studies for reducing  $CO_2$  emissions and energy consumption have been actively conducted since the 2000s. These studies have included the development of Life-Cycle Assessment (LCA) model [1], development of facility system and material in green building [2,3] and green building design [4]. Most studies are focused on  $CO_2$  emissions in the use and maintenance stage, because the largest amount of  $CO_2$  is generated in that stage [5]. However, most buildings unlike durable goods in other industries have a characteristic and long life cycle and the reduction of  $CO_2$ emissions is bound together in activities at each stage in the life cycle. In other words, the reduction of the environmental load

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and the effect of the environmental improvement cannot be possible by optimizing a part, not all [6]. In order to achieve environmentally friendly construction considering the LCA, the design should be derived to reduce  $CO_2$  emissions from the early building design stage and structure engineers should be able to create a design plan considering the environmental friendliness and economic feasibility [7, 8].

Preceding studies that considered CO<sub>2</sub> emissions in the structural design stage typically used optimal design methods. Moon (2008) proposed an optimal design method that minimizes the quantity of the input materials for sustainable structural designs in the steel frame structure [9]. Paya et al. (2009) proposed the optimal design technique to reduce either CO<sub>2</sub> emission levels or structural cost of reinforced concrete frame structures using a Simulated Annealing (SA) method [10]. In addition, Paya et al. (2008) suggested a multi-objective design methodology applied to the four objective functions of the structural cost, environmental impact, constructability and overall safety of RC framed structures using the SA method [11]. Although these results show that suggested optimal design methodologies can effectively reduce CO<sub>2</sub> emission levels, there are material limitations that must be overcome before they can be applied to actual buildings. In fact, the height of buildings overall is increasing, and composite members are used for high-rise buildings in place of RC members [12]. Hence, a design technique that considers environmental friendliness and economic feasibility is necessary also for composite members.

Therefore, this study describes an optimal design technique that minimizes  $CO_2$  emissions and cost generated in the material production stage simultaneously and that is applicable to actual high-rise buildings. Additionally, we applied the optimum design technique with NSGA-II proposed here to the structural design of a 35-story building to evaluate the applicability and stability of the algorithm.

## II. SCOPE AND METHOD OF THE STUDY

## A. Scope of the Study

This study was aimed at encased composite columns supporting only the gravity load in the building frame system frequently applied for high-rise buildings. In the optimization process, the load on the columns and the axial force of the members were assumed to be constant because of the relatively minor variation of the load on the columns. Moreover,  $CO_2$  emissions were limited to discharge in the material production stage.

# B. Research Methods

A large number of parameters in composite building design should be considered, including the composite cross-sectional area and the size of the steel frames, especially in high-rise building. Thus, in this study, we employed the NSGA-II, known to be appropriate for complex numerical problems [13], to optimize the two objective functions of CO<sub>2</sub> emissions and cost at once.

## III. THE OPTIMIZATION ALGORITHM

## A. Optimization Algorithm

Fig. 1 shows a process of the optimization algorithm using Pareto optimal solution applied in this study. First, the member forces are secured through a structural analysis and the parameters necessary for the genetic algorithm. Then, the early population is formed. As the procedure of NSGA-II is repeated until the terminal condition is satisfied, we obtain the non-dominant first-order optimal solution set that does not violate the constraints.



Fig. 1 Flowchart of the optimization algorithm with NSGA-II

# B. Design Variables

This study use discrete design variables to find the optimal solutions using a GA and establish databases consisting of both section properties and material properties of the SRC column. The 512 SRC section database is made up of 23 SM-490 rolled beams, 31 SM-490 built-up, 132 SM-490TMCP, 163 SM-520TMCP and 163 SM-570TMCP members per one type of strength of concrete. There are seven types of strength of concrete (21, 24, 27, 30, 35, 40 and 50*MPa*), so the member can be selected from a database that contains a total of 3854 data.

The five types of 512 SRC column database, as the design variables in this study, can be divided into rolled H beams and welded H beams depending on the processing method. When calculating the unit price ( $C_{stl}$ ) of the SM-490, SM-490TMCP, SM-520TMCP and SM-570TMCP in the form of a welded H beam, the unit price is sum of the price of the thick plate for the beams (Vton) and the fabrication cost  $\alpha$ (Vton). When calculating the unit CO<sub>2</sub> emission ( $E_{stl}$ ) of the material, the CO<sub>2</sub> emission from welding  $\beta$ (kg·CO<sub>2</sub>/kg), should be taken into consideration, not considered in this study.

# C. Objective Functions

The purpose of this study is to minimize the total  $CO_2$  emission and cost of the column line simultaneously using the unit  $CO_2$  emission and price of material depending on the strength levels of the concrete and the steel. Therefore, the objective functions were defined with respect to  $CO_2$  emission and cost of the column line of the subject building, as expressed by Eq. (1-a) and Eq. (1-b):

$$Minimize \quad f_1 = \sum_{i=1}^{M} A^i_{stl} L^i \rho_{stl} C_{stl} + A^i_{con} L^i \rho_{con} C_{con}$$
(1-a)

$$Minimize \quad f_2 = \sum_{i=1}^{M} A_{sil}^i L^i \rho_{sil} E_{sil} + A_{con}^i L^i \rho_{con} E_{con}$$
(1-b)

Eq. (1-a) is the function for the structural cost of the column line. Eq. (1-b) is the function for the CO<sub>2</sub> emission of the column line. A and L denote the member cross-sectional area and the member length, respectively.  $\rho$  denotes the density of the material. C and E denote the unit price and CO<sub>2</sub> emission in the column cross-sections depending on the design parameters, respectively. The subscripts *stl* and *con* refer to the steel material and concrete, respectively. The superscript *i* refers to the *i*th member, and M denotes the total number of members included in one column line.

# D.Constraint Conditions

The constraint functions consist of the main constraint for the resisting capacity of the cross-section and the sub-constraints for the constructability. For the main constraints, we used the P-M diagram, which was also used as the constraint in the optimal design of a RC structure using a GA by Lee and Ahn (2003) [14]. The main constraint can be expressed as Eq. (2) with  $L_m$  and  $L_u$  representing the distance between the origin and load point and the distance between the origin and cross point, respectively:

$$\frac{L_u}{L_m} \le 1 \tag{2}$$

The remaining constraints for the constructability are that the total cross-section, the inside dimension of the steel frame, the outside dimension of the steel frame, the yield strength of the steel and the concrete compressive strength of the upper members should not be greater than those of the lower members, as expressed by Eq. (3-a), (3-b), (3-c), (3-d) and (3-e). Here, i refers to the *i*th member, ranging from the first member to the (M-1)th member.

$$\frac{A_{g}^{i+1}}{A_{g}^{i}} \leq 1.0 \quad (3-a) \qquad \frac{S_{sd_{-i}}^{i+1}}{S_{sd_{-i}}^{i}} \leq 1.0 \quad (3-b) \qquad \frac{S_{sd_{-o}}^{i+1}}{S_{sd_{-o}}^{i}} \leq 1.0 \quad (3-c)$$
$$\frac{F_{ys}^{i+1}}{F_{ys}^{i}} \leq 1.0 \quad (3-d) \qquad \frac{f_{ck}^{i+1}}{f_{ck}^{i}} \leq 1.0 \quad (3-e)$$

The constraint for constructability is considered as a sub-constraint because when the constraint is violated, the software properly corrects the cross-section of the upper member by selecting the member that satisfies all of the constructability constraints.

## IV. EXAMPLE ANALYSIS

#### A. Application Example

In this section, we applied the proposed optimization algorithm to a mixed-use residential building with 29 floors above ground and 6 floors in the basement as Fig.2 and then analyzed the environmental friendliness and economic feasibility of the suggested design plan. The building consists of a total of 57 SRC column lines that are divided into 19 SRC column lines according to the location on the plane and the shared load, one of which was analyzed in this study.



Fig. 2 Framework and the typical floor plan in example building

TABLE I represents the unit price and the  $CO_2$  emission values of the concrete depending on the material strength, and TABLE II represents those of the steel types included in the SRC database. But, the unit price for the welded H beams was applied by adding the fabrication cost to the price of the thick plate.

TABLE I	
UNIT PRICE AND THE CO <sub>2</sub> EMISSION ON THE CONCRETE STRENGT	Н

$f_{ck}(MPa)$	21	24	27	30	35	40	50
Price	51,800	54,300	56,800	59,700	61,800	73,300	87,000
(Vm <sup>3</sup> )	(100%)	(104.8%)	(109.6%)	(115.3%)	(119.3%)	(141.5%)	(167.9%)
CO <sub>2</sub> emissions (kg·CO <sub>2</sub> /m <sup>3</sup> )	321.57 (100%)	325.80 (101.3%)	346.14 (107.6%)	370.51 (115.2%)	405.73 (126.2%)	391.03 (121.6%)	453.15 (140.9%)

TABLE II THE UNIT PRICE AND THE CO<sub>2</sub> EMISSION ON THE STEEL TYPE

Type of Steel	Steel plate thickness	Price of thick plate (Vton)	CO <sub>2</sub> Emission (kg-CO <sub>2</sub> /kg)
SM490	0 <t≤25< td=""><td>727,100</td><td></td></t≤25<>	727,100	
	25 <t≤38< td=""><td>735,800</td><td>0.4100</td></t≤38<>	735,800	0.4100
	38 <t≤50< td=""><td>743,700</td><td>0.4188</td></t≤50<>	743,700	0.4188
	60 <t≤100< td=""><td>753,100</td><td></td></t≤100<>	753,100	
	0 <t≤25< td=""><td>749,700</td><td></td></t≤25<>	749,700	
	25 <t≤38< td=""><td>758,400</td><td>0.4219</td></t≤38<>	758,400	0.4219
SM490 TMCP	38 <t≤50< td=""><td>766,300</td><td>0.4318</td></t≤50<>	766,300	0.4318
	50 <t≤100< td=""><td>775,700</td><td></td></t≤100<>	775,700	
	0 <t≤25< td=""><td>758,400</td><td></td></t≤25<>	758,400	
SM520 TMCD	25 <t≤38< td=""><td>767,800</td><td>0.42(9</td></t≤38<>	767,800	0.42(9
SM520 TMCP	38 <t≤50< td=""><td>775,700</td><td>0.4368</td></t≤50<>	775,700	0.4368
	50 <t≤100< td=""><td>783,600</td><td colspan="2"></td></t≤100<>	783,600	
SM570 TMCP	0 <t≤50< td=""><td>867,600</td><td>0.4007</td></t≤50<>	867,600	0.4007
	50 <t≤100< td=""><td>875,500</td><td>0.4997</td></t≤100<>	875,500	0.4997

## B. The relation of $CO_2$ emissions and cost

The SRC column sections under the same load (=1000N) were variously designed with different strength levels of the materials and the different percentage of quantities. In that case, the CO<sub>2</sub> emission and structural cost of the SRC column were analyzed.

Fig. 3(a) shows a case in which the variation of the  $CO_2$ emission of the SRC column depending on the percentage of concrete quantities was the smallest: the concrete whose compressive strength was 50MPa and the SM490 whose yield strength was 325MPa were used in the case. In contrast, Fig. 3(b) shows a case in which the variation of the CO<sub>2</sub> emission of the SRC column depending on the percentage of concrete quantities was the largest: the concrete whose compressive strength was 21MPa and the SM570TMCP whose yield strength was 440MPa were used in the case. Although the CO<sub>2</sub> emission from the designed column is different among the cases because materials of different strength levels were used, the same trend is found, in that the CO<sub>2</sub> emission from the columns increased as the percentage of the concrete quantity increases in the SRC columns. On the other hand, Fig. 4 show the cost generated in the same cases shown in Fig. 3. As shown in these figures, the cost of the SRC columns was governed by the ratio of the quantity of the steel. Consequently, Fig. 3 and Fig. 4 show that the CO<sub>2</sub> emission rates increased but the construction cost decreased as the concrete quantity ratio was increased in the SRC columns.



Fig. 3(a) (b) The smallest and the largest variation of CO<sub>2</sub> emission

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Fig. 4(a) (b) The cost variation in the same case as Fig. 3

## C. Optimization Analysis

The optimization was performed for the case in which CO<sub>2</sub> emissions for concrete strength level and that for steel strength level were constant, at 321.57(kg- CO<sub>2</sub>/m<sup>3</sup>) and 0.4188(kg- $CO_2/kg$ ), respectively. The result in Fig. 5(a) shows that the optimal design plans are located on the left bottom side of the graph, indicating that both cost and CO<sub>2</sub> emissions decrease when compared to those of the initial design plan. Additionally, cost and CO<sub>2</sub> emissions of the individual cases were compared. The result showed that the CO<sub>2</sub> emission increased in the individual cases at a relatively low cost while the cost was increased in the individual cases with relatively less CO<sub>2</sub> emission. However, when the CO<sub>2</sub> emission for strength level was constant, the difference between the solution where the cost is the minimum and the CO<sub>2</sub> emission is the maximum and the solution where the cost is the maximum and the  $CO_2$ emission is the minimum was approximately 1.9-2.4%, indicating that the range of the solution distribution was very narrow

On the other hand, optimization was performed for the case in which the CO<sub>2</sub> emission rates for concrete strength level and that for steel strength level were not constant. Fig. 5(b) shows the algorithm application result obtained by applying the CO<sub>2</sub> emission values in Tables I and II. As in the previous case, the 15 optimal design plans are distributed on the left bottom side of the graph, indicating a trend in which CO<sub>2</sub> emissions increased in the individual cases at a relatively low cost and that the cost was increased in the individual cases with relatively less CO<sub>2</sub> emission. However, the ranges of the maximum and minimum values were wider than those in the previous case and the suggested solutions contain more variation. Thus, the users can select economic or environmental solution according to their preference. The result showed that the cost and CO<sub>2</sub> emission can be reduced by about 31-34% and 6.4-10.6% when compared to those of the initial design plan. The effect of the CO<sub>2</sub> emission reduction was smaller than that in the previous case because the minimum CO<sub>2</sub> emission value for each material strength level was applied in the previous case.



Fig. 5 (a) (b)  $CO_2$  emission is constant and not constant on strength

Table III compares the initial plan designed by the design office, the No. 1 optimal design plan where the CO<sub>2</sub> emission is the greatest and the cost is the lowest, and the No. 15 optimal design plan where the CO<sub>2</sub> emission is the lowest and the cost is the highest, among the optimal design plans shown in Fig. 5(b). Table III shows that the SRC quantity of the optimal design plans No. 1 and No. 15 are less than that of the initial design plan by 2.7% and 1.9%, respectively, also showing that the CO<sub>2</sub> emission rates are less by 6.4% and 10.6%, respectively. That is the decrement of the CO<sub>2</sub> emission was not proportional to the decrement of the SRC quantity relative to the initial design plan. The SRC quantity of the No. 1 optimal design plan was less than that of the No. 15 optimal design plan by 1.58 t, while the CO<sub>2</sub> emission was greater by 2140 (kg- CO<sub>2</sub>). This occurred because the CO<sub>2</sub> emission is determined by the ratio of the concrete and steel in the SRC columns where the two materials are used.

		Steel	Concrete	SRC
Initial design	Quantity (ton)	67.34 (32.4%)	140.33 (67.6%)	207.68
	COST (Million-\)	64.13 (95.3%)	3.12 (4.7%)	67.30
	CO <sub>2</sub> Emission (Thousand-kg)	31.97 (62.1%)	19.53 (37.9%)	51.50
No.1	Quantity (ton)	41.06 (20.3%)	161.07 (79.7%)	202.13
	COST (Million-\)	38.75 (87.2%)	5.69 (12.8%)	44.44
	CO <sub>2</sub> Emission (Thousand-kg)	18.23 (37.8%)	29.96 (62.2%)	48.19
No.15	Quantity (ton)	43.57 (21.4%)	160.14 (78.6%)	203.71
	COST (Million-\)	41.38 (89.2%)	5.00 (10.8%)	46.38
	CO <sub>2</sub> Emission (Thousand-kg)	19.28 (41.9%)	26.77 (58.1%)	46.05

TABLE III THE ANALYSIS RESULTS OF THE CANDIDATE OPTIMAL DESIGN SOLUTIONS

## V.CONCLUSION

In this study, we proposed an optimization algorithm that is applicable to SRC columns considering the cost and CO2 emission simultaneously depending on the type of steel and the concrete strength levels. We applied the proposed optimum design technique to an actual column design to verify its economic feasibility and environmental friendliness. The following conclusions are reached: 1) The analysis was performed for the case where the  $CO_2$  emission for each material strength level is constant and not constant. The result showed that the cost and the  $CO_2$  emission of the optimal design plans for the two cases were decreased by 31-34% and 6.4-10.6%, respectively, when compared to those of the initial design plan for each case.

2) When the load condition is identical, the quantity ratio of each material affects the  $CO_2$  emission and cost generated by the columns. If the design has a relatively large concrete quantity ratio, the entire cost may be decreased by reducing the quantity ratio of the steel that govern the cost of the structure, and the  $CO_2$  emission from the cross-sections may be increased as the  $CO_2$  emission of the concrete is increased.

## REFERENCES

- Zhang, Z., Wu, X., Yang, X., Zhu, Y., BEPAS A life cycle building environmental performance assessment model, Building and Environmental 51(5) (2006), pp. 669-675
- [2] Radhi, H., On the optimal selection of wall cladding system to reduce direct and indirect CO<sub>2</sub> emissions, Energy 35(3) (2010), pp. 1412-1424
- [3] Gartner, E., Industrially interesting approaches to "low-CO2" cements, Cement and Concrete Research 34(9) (2004), pp. 1489-1498
- [4] Wang, W., Zmeureanu, R., Rivard, H., Applying multi-objective genetic algorithms in green building design optimization, Building and Environment 40(11) (2005), pp. 1512-1525
- [5] Sartori, I., Hestnes, A.G., Energy use in the life cycle of conventional and low-energy buildings: A review article, Energy and Buildings 39(3) (2007), pp. 249-257
- [6] Ki-Bong Park, Takafumi Noguchi, Environmental Concern Concrete and Reinforced Concrete Construction for Low Carbon Green Growth, Korea Concrete Institute 21(4) (2009), pp.44-49
- [7] Guggemos, A.A., Horvath, A., Comparison of Environmental Effects of Steel- and Concrete-Framed Buildings, Journal of Infrastructure Systems 11(2) (2005), pp. 93-101
- [8] Cole, R.J., Energy and greenhouse gas emissions associated with the construction of alternative structural systems, Building and Environment 34(3) (1998), pp. 335-348
- [9] Moon, K.S., Sustainable structural engineering strategies for tall building, The Structural Design of Tall and Special Buildings 17(5) (2008), pp. 895-914
- [10] Paya-Zaforteza, I., Yepes, V., Hopitaler, A., Gonzalez-Vidosa, F., CO2-optimization of reinforced concrete frames by simulated annealing, Engineering Structures 31(7) (2009), pp. 1501-1508
- [11] Paya, I., Yepes, V., Gonzalez-Vidosa, F., Hospitaler, A., Multiobjective optimization of concrete building frames by simulated annealing, Computer-Aided Civil and Infrastructure Engineering 23(8) (2008), pp. 596-610
- [12] Saw, H.S. and Liew, J.Y.R., Assessment of current methods for the design of composite columns in buildings, Journal of Constructional Steel Research 53(2) (2000), pp. 121-147
- [13] Holland, J.H., Adaptation in natural and artificial system, Univ. Michigan Ann Arbor, MIT. (1975)
- [14] C. Lee and J. Ahn, Flexural Design of Reinforced Concrete Frames by Genetic Algorithm, Journal of Structural Engineering 129(6) (2003), pp. 762-774