

Application of PSO Technique for Seismic Control of Tall Building

A. Shayeghi, H. Shayeghi, H. Eimani Kalasar

Abstract—In recent years, tuned mass damper (TMD) control systems for civil engineering structures have attracted considerable attention. This paper emphasizes on the application of particle swarm application (PSO) to design and optimize the parameters of the TMD control scheme for achieving the best results in the reduction of the building response under earthquake excitations. The Integral of the Time multiplied Absolute value of the Error (ITAE) based on relative displacement of all floors in the building is taken as a performance index of the optimization criterion. The problem of robustly TMD controller design is formatted as an optimization problem based on the ITAE performance index to be solved using the PSO technique which has a story ability to find the most optimistic results. An 11-story realistic building, located in the city of Rasht, Iran is considered as a test system to demonstrate effectiveness of the proposed method. The results analysis through the time-domain simulation and some performance indices reveals that the designed PSO based TMD controller has an excellent capability in reduction of the seismically excited example building.

Keywords—TMD, Particle Swarm Optimization, Tall Buildings, Structural Dynamics.

I. INTRODUCTION

A critical aspect in the design of civil engineering structures is the reduction of response quantities such as velocities, deflections and forces induced by environmental dynamic loads (i.e., wind and earthquake). Structural control methods are the most recent strategies for this purpose, which can be classified as active, semi-active, passive, and hybrid control methods [1]. In the last three decades or so, the reduction of structural response, caused by dynamic effects, has become a subject of research, and many structural control concepts have been implemented in practice. Tuned mass dampers (TMDs) are the oldest structural vibration control devices in existence. The concept of vibration control using a mass damper dates back to the year 1909, when Frahm invented a vibration control device called a dynamic corresponding vibration absorber [2]. Although active tuned mass damper systems nowadays has received considerable attention from many researchers [3-5], a passive control technique is still considered due to its simplicity. Moreover, many passive control devices such as TMD successfully installed in the real application to reduce the lateral motion of high rise buildings

[2,6-8]. In this paper, a TMD system is considered to be applied to multi-degree-of-freedom structure, without specifying which mode should be controlled. Thus, there is no need to transfer the structure to a single-mode model as have been done in the available research.

Several cost or objective functions have been developed to meet a specified performance in the optimization process. In practice, many performance indices can be chosen, as the objective functions resulted in a different result of the optimization. In the active vibration control area, there are also many optimization criteria which have been used by researchers. The most common ones are LQR, LQG, H_2 , H_∞ , sliding mode control, pole placement, independent model space control and so on [1,9-13]. It should be noted that in the active control optimization there is a trade off between the responses to be minimize the structural responses while maintaining the control energy to be used, the passive control optimization is free from balancing the two parameters.

In this paper, the Integral of Time multiplied Absolute value of Error (ITAE) based on the displacement of all building's floors is taken as a performance index of the optimization criteria. Usually, the traditional gradient-based search methods are used for solution of this problem. Unfortunately, the optimization requires computations of sensitivity factors and eigenvectors at its iteration process. This gives rise to heavy computational burden and slow convergence. Moreover, there is no local criterion to decide whether a local solution is also the global solution. Thus, conventional optimization methods that make use of derivatives and gradients are, in general, not able to locate or identify the global optimum, but for real-world applications, one is often content with a good solution, even if it is not the best. Consequently, heuristic methods are widely used for the global optimization problem. Recently, global optimization techniques like genetic algorithm (GA) have been used for TMD and Active TMD (ATMD) parameter optimization [14-16]. Although, the GA technique seems to be good method for the solution of TMD parameter optimization problem, however, when the system has a highly epistemic objective function (i.e. where parameters being optimized are highly correlated), and number of parameters to be optimized is large, then they have degraded efficiency to obtain global optimum solution and also simulation process use a lot of computing time. In order to overcome these drawbacks, a Particle Swarm Optimization (PSO) based TMD (PSOTMD) is proposed for the control of structural dynamics in this paper. PSO is a novel population based met heuristic, which utilize the swarm intelligence generated by the cooperation and competition between the particle in a swarm and has emerged as a useful tool for engineering optimization. It has also been found to be

A. Shayeghi is with the Department of Technical Eng., Islamic Azad University, Germe Branch, Germe, Iran (e-mail: alishayeghi3@yahoo.com).

H. Shayeghi Eimani Kalasar are with the Department of Technical Eng., University of Mohaghegh Ardabili, Ardabil, Iran (corresponding author to provide phone: 98-551-2910; fax: 98-551-2904; e-mail: hshayeghi@gmail.com).

is tuned to a frequency close to one of the natural frequencies of the main system. Thus, there are three main parameters in a TMD system: TMD mass, TMD stiffness coefficient and TMD dumping ratio. Consequently, the objective is to find the optimum value of these parameters that involve in *state matrix*, A in Eq. (8). Usually, this problem is converted to a problem of single-degree-of-freedom (SDOF) structure where the parameter of the structure is at a specified mode (usually the first mode) to be chosen. In view of seeking a more realistic model, this paper is used the multi-degree-of-freedom (MDOF) model as a structural model without specifying to special mode. By considering the structure as an MDOF structure the optimization process is coming more difficult to solve. Moreover, in case of an inherent damping presence in the structure, the closed-form solution may not be available. Thus, only numerical solution could be possible to solve the problem of MDOF structures with inherent damping. For this reason, the PSO technique which is a useful tool for engineering optimization is being used to find optimal parameter of TMD for reduction of the structural vibrations.

III. PSO TECHNIQUE AND OPTIMIZATION OF TMD PARAMETERS

Particle swarm optimization algorithm, which is tailored for optimizing difficult numerical functions and based on metaphor of human social interaction, is capable of mimicking the ability of human societies to process knowledge [18]. It has roots in two main component methodologies: artificial life (such as bird flocking, fish schooling and swarming); and, evolutionary computation. Its key concept is that potential solutions are flown through hyperspace and are accelerated towards better or more optimum solutions. Its paradigm can be implemented in simple form of computer codes and is computationally inexpensive in terms of both memory requirements and speed. It lies somewhere in between evolutionary programming and the genetic algorithms. As in evolutionary computation paradigms, the concept of fitness is employed and candidate solutions to the problem are termed particles or sometimes individuals, each of which adjusts its flying based on the flying experiences of both itself and its companion. It keeps track of its coordinates in hyperspace which are associated with its previous best fitness solution, and also of its counterpart corresponding to the overall best value acquired thus far by any other particle in the population. Vectors are taken as presentation of particles since most optimization problems are convenient for such variable presentations. In fact, the fundamental principles of swarm intelligence are adaptability, diverse response, proximity, quality, and stability. It is adaptive corresponding to the change of the best group value. The allocation of responses between the individual and group values ensures a diversity of response. The higher dimensional space calculations of the PSO concept are performed over a series of time steps. The population is responding to the quality factors of the previous best individual values and the previous best group values. The principle of stability is adhered to since the population changes its state if and only if the best group value changes [18, 19]. As it is reported in [17], this optimization technique can be used to solve many of the same kinds of problems as

GA, and does not suffer from some of GAs difficulties. It has also been found to be robust in solving problem featuring non-linearity, non-differentiability and high-dimensionality. The PSO is the search method to improve the speed of convergence and find the global optimum value of fitness function.

PSO starts with a population of random solutions “particles” in a D-dimension space. The i th particle is represented by $X_i = (x_{i1}, x_{i2}, \dots, x_{iD})$. Each particle keeps track of its coordinates in hyperspace, which are associated with the fittest solution it has achieved so far. The value of the fitness for particle i ($pbest$) is also stored as $P_i = (p_{i1}, p_{i2}, \dots, p_{iD})$. The global version of the PSO keeps track of the overall best value ($gbest$), and its location, obtained thus far by any particle in the population. PSO consists of, at each step, changing the velocity of each particle toward its $pbest$ and $gbest$ according to Eq. (9). The velocity of particle i is represented as $V_i = (v_{i1}, v_{i2}, \dots, v_{iD})$. Acceleration is weighted by a random term, with separate random numbers being generated for acceleration toward $pbest$ and $gbest$. The position of the i th particle is then updated according to Eq. (10) [18].

$$v_{id} = w \times v_{id} + c_1 \times rand() \times (P_{id} - x_{id}) + c_2 \times rand() \times (P_{gd} - x_{id}) \quad (9)$$

$$x_{id} = x_{id} + cv_{id} \quad (10)$$

Where, P_{id} and P_{gd} are $pbest$ and $gbest$. Several modifications have been proposed in the literature to improve the PSO algorithm speed and convergence toward the global minimum. One modification is to introduce a local-oriented paradigm ($lbest$) with different neighborhoods. It is concluded that $gbest$ version performs best in terms of median number of iterations to converge. However, $pbest$ version with neighborhoods of two is most resistant to local minima. The PSO algorithm is further improved via using a time decreasing inertia weight, which leads to a reduction in the number of iterations [17]. Figure 2 shows the flowchart of the proposed PSO algorithm.

This new approach features many advantages; it is simple, fast and easy to be coded. Also, its memory storage requirement is minimal. Moreover, this approach is advantageous over evolutionary in many ways. First, PSO has memory. That is, every particle remembers its best solution (local best) as well as the group best solution (global best). Another advantage of PSO is that the initial population of the PSO is maintained, and so there is no need for applying operators to the population, a process that is time and memory-storage-consuming. In addition, PSO is based on “constructive cooperation” between particles.

A. TMD design using PSO

Tuned mass damper consisting of a mass, a damping, and a spring is an effective and reliable structural vibration control device commonly attached to the vibrating primary system for suppressing the undesirable vibrations induced by winds and earthquake loads. In the proposed method, we must find the TMD parameters optimally to get maximum reduction in building responses due to the different earthquake excitations. Thus, in optimization process the simulated earthquake using Kanai-Tajimi filter (Eq. (11)) is shown in Fig. 3 by MATLAB

software [23] is created and used as base earthquake excitation.

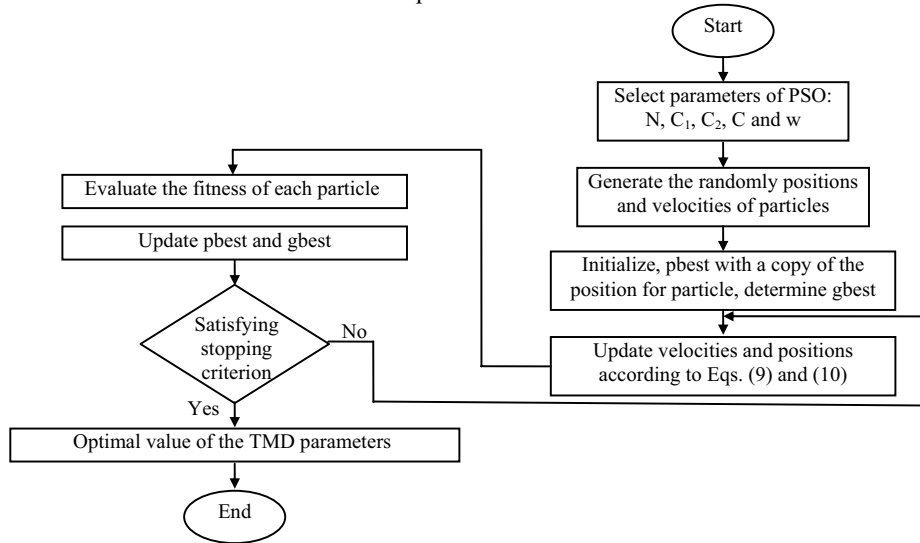


Fig. 2. Flowchart of the proposed PSO technique.

$$H(s) = S_0 \frac{(\omega_g^4 + 4\omega_g^2 \xi_g^2 s^2)}{(s^2 - \omega_g^2)^2 + 4\omega_g^2 \xi_g^2 s^2} \quad (11)$$

$$S_0 = 0.03 \frac{\xi_g g^2}{\pi \omega_g (4\xi_g^2 + 1)}$$

In this work, ω_g and ξ_g is considered as 37.3 and 0.3, which are for usual soils, respectively.

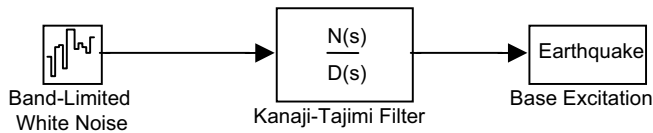


Fig.3. Base excitation used for tuning of the TMD Parameters

To acquire an optimal combination, this paper employs PSO to find the global optimum value of fitness function. It should be noted that choice of the properly objective function is very important in synthesis procedure for achieving the desired level of system robust performance. Because different objective functions promote different PSO behaviors, which generator fitness value providing a performance measure of problem considered [17]. For our optimization problem, the following objective function based on the system performance index of the ITAE is used [24].

$$J = \sum_{i=1}^N ITAE_i \quad (12)$$

$$ITAE_i = \int_0^{t=tsim} t |x_i(t)| dt$$

Where, x_i is relative displacement of i th story building response under base earthquake excitation and is obtained using the solution of Eq. (8). It is worth mentioning that the

lower the value of this objective function is, the better robustly the system performance in terms of time domain characteristics. The design problem can be formulated as the following constrained optimization problem, where, the constraints are the TMD parameters bounds.

Minimize J subject to

$$m_o^{\min} \leq m_o \leq m_o^{\max} \quad (13)$$

$$\beta_d^{\min} \leq \beta_d \leq \beta_d^{\max}$$

$$\zeta_d^{\min} \leq \zeta_d \leq \zeta_d^{\max}$$

To improve the overall building response in a robust way and optimization synthesis, PSO is used to solve the above optimization problem that search for optimal or near optimal set of TMD parameters.

IV. CASE STUDY

In order to investigate the performance of the proposed control strategy in reducing the structural responses under earthquake loads, an 11-story shear building, located in city of Rasht in the north of Iran, is chosen as an a test system. The structure represents a tall building. The structural properties of this building are listed in Table 1 [15].

The TMD frequency ratio to the first model frequency of the building has been choused β_d . The mass of the TMD system was chosen to be m_o percent of total mass of the building and its damping ratio (ζ_d) was considered to be percent of the critical value. These three parameters (m_o , β_d and ζ_d) of TMD are optimized by evaluating the cost function as given in Eq. (13). In order to acquire better performance, the number of particle, particle size, number of iteration, c_1 , c_2 and c is chosen as 25, 3, 250, 1.47, 2.2 and 1, respectively. Also, the inertia weight, ω , is linearly decreasing from 0.9 to 0.4. Results of TMD parameter set values using the proposed PSO method are given in Table 2. Also, Fig. 4 shows the minimum fitness value evaluation process.

TABLE I
 TEST BUILDING STRUCTURAL DATA

Stories	Mass(kg) $\times 10^5$	Stiffness(N/m) $\times 10^8$
1	2.15	4.68
2	2.01	4.76
3	2.01	4.68
4	2.00	4.5
5	2.01	4.5
6	2.01	4.5
7	2.01	4.5
8	2.03	4.37
9	2.03	4.37
10	2.03	4.37
11	1.76	3.12

TABLE II
 OPTIMAL VALUE OF TMD PARAMETERS.

TMD Parameters	PSO
m_0	0.06
β_d	0.3
ζ_d	0.13

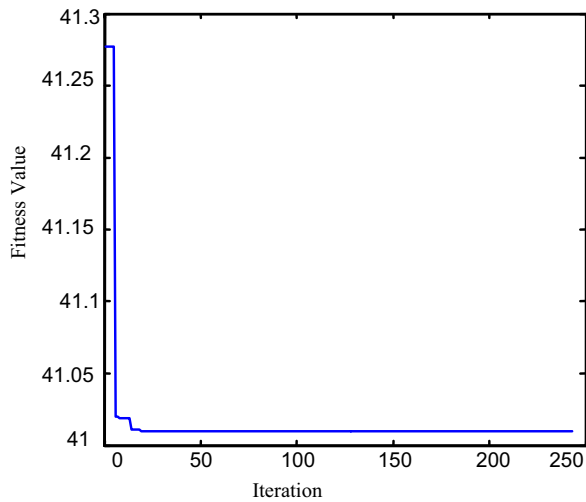


Fig. 4. Minimum fitness convergence by PSO

A. Simulation results

To investigate the effectiveness of the control system for different disturbances, three different seismic motions are used in the numerical simulations. These ground acceleration records are: El Centro 1940, Kobe 1995 and Tabas 1999 earthquakes. The absolute peak ground accelerations (PGAs) of these earthquake records are 0.3417, 0.8178 and 0.9512 g, respectively.

The result of controlled displacement response of the example building top story due to the El Centro NS earthquake calculated by the PSO-based TMD designed systems are compared with the corresponding uncontrolled ones in Fig. 5 and Table 3. Also, Fig. 6 depicted maximum

displacement of floors using the proposed method and uncontrolled systems. Fig. 7 shows the ITAE performance index. It can be seen that from the figures and Table, the response reduction ratio (ratio of the controlled to uncontrolled response) for maximum displacement of top floor of the 11-story example building is about 40% for the PSOTMD. Thus, PSO-based designed TMD is effective method.

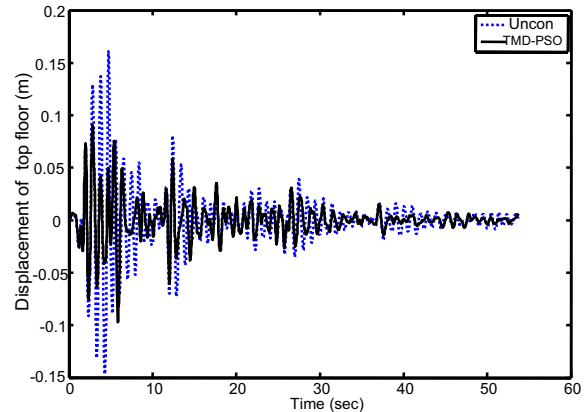


Fig.5. Displacement of top floor under El Centro 1940 earthquake

TABLE III
 COMPARISON OF THE EFFECTIVENESS CONTROLLER SYSTEM FOR THE EL CENTER 1940 EARTHQUAKE

Building floor	Maximum uncontrolled response (m)	Controlled to uncontrolled response ratio percent (Reduction Ratio) using PSOTMD
1	0.0224	44.0260
2	0.0432	43.8906
3	0.0627	42.8707
4	0.0811	41.7516
5	0.0973	40.5694
6	0.1112	39.3886
7	0.1253	39.4371
8	0.1381	39.5509
9	0.1486	39.6833
10	0.1558	39.6494
11	0.1608	39.4321

The effectiveness of the controller system and ITAE in reducing the response of the example building due to other earthquakes is also shown for comparison in Figs. 8-13 and Tables 4-5. Almost the same behavior as for the El Centro earthquake can be observed for these earthquakes, too. Moreover, it is seen from Table 4-5 that the Kobe 1995 and Tabas 1999 earthquakes cause the maximum displacement at the top floor of the example building, which is a very high value in comparison with the other earthquakes. This is expected due to fact that the PGA of the two earthquakes is very high and almost remains constant for a long period of time in comparison with the El Centro earthquake.

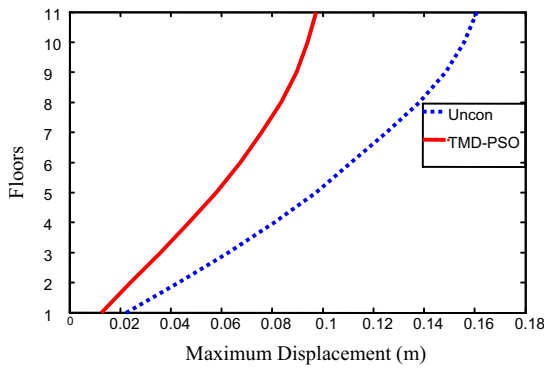


Fig. 6. Maximum displacement of floors under El Centro 1940 earthquake.

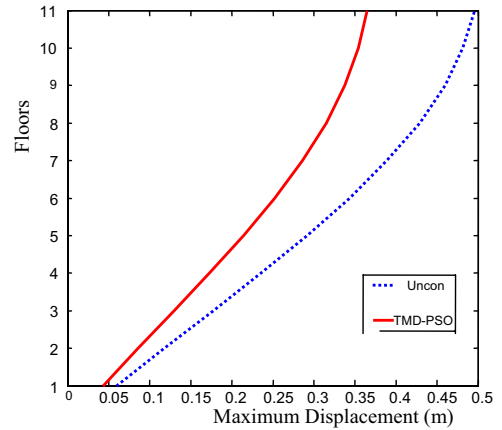


Fig. 9. Maximum displacement of floors under Kobe 1995 earthquake.

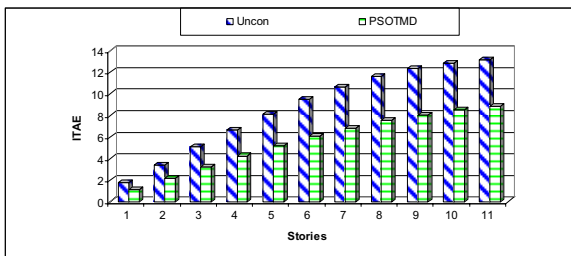


Fig. 7. ITAE performance index value for all floors under El Centro 1940 earthquake.

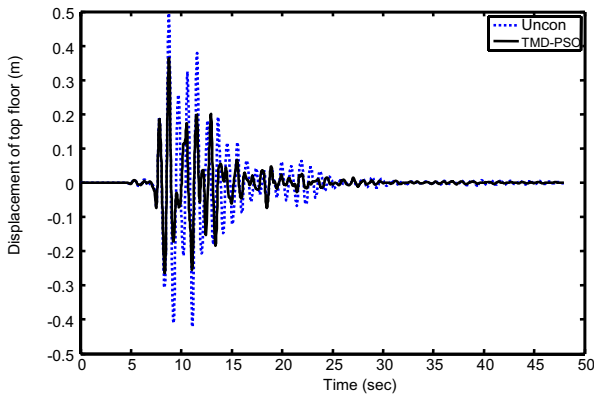


Fig.8. Displacement of top floor under Kobe 1995 earthquake

To demonstrate the robustness effectiveness of the proposed method, the average reduction ratios (controlled to uncontrolled displacement and acceleration ratio) for all three earthquakes on all 11 stories of the example building are shown in Table 6 and 7, respectively. According to these Tables, it can be seen that in general the PSOTMD system are capable of reducing the maximum displacement and acceleration of the building in each story to about 25.5 and 24.5 of the uncontrolled response, respectively. Thus, based on average the proposed method is very effective.

TABLE IV
 COMPARISON OF THE EFFECTIVENESS OF THE CONTROLLER SYSTEM FOR THE
 KOBE 1995 EARTHQUAKE

Building floor	Maximum uncontrolled response (m)	Controlled to uncontrolled response ratio percent (Reduction Ratio))
		PSOTMD
1	0.0596	27.4487
2	0.1184	27.2065
3	0.1771	26.9915
4	0.2361	26.8041
5	0.2919	26.6392
6	0.3433	26.5216
7	0.3890	26.4887
8	0.4289	26.5607
9	0.4602	26.5285
10	0.4814	26.4313
11	0.4956	26.3741

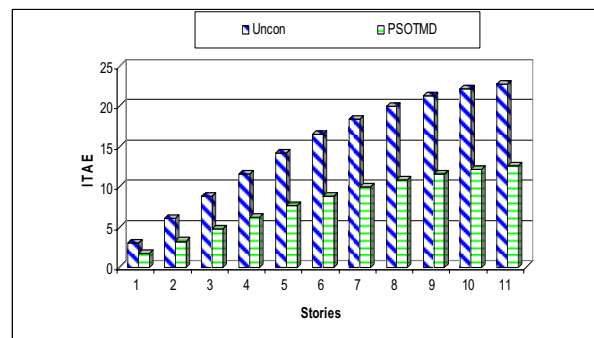


Fig. 10. ITAE performance index value for all floors under Kobe 1995 earthquake.

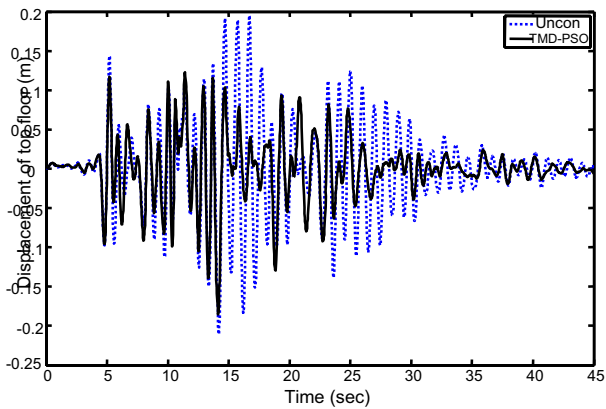


Fig. 11. Displacement of top floor under Tabas 1999 earthquake

TABLE V
 COMPARISON OF THE EFFECTIVENESS OF THE DIFFERENT CONTROLLER SYSTEMS FOR THE TABAS EARTHQUAKE

Building floor	Maximum uncontrolled response (m)	Controlled to uncontrolled response ratio percent (Reduction Ratio)
		PSOTMD
1	0.0596	2.127
2	0.1184	3.5263
3	0.1771	5.1041
4	0.2361	6.7949
5	0.2919	8.5140
6	0.3433	10.1406
7	0.3890	11.4235
8	0.4289	12.0975
9	0.4602	12.2247
10	0.4814	12.1353
11	0.4956	11.9566

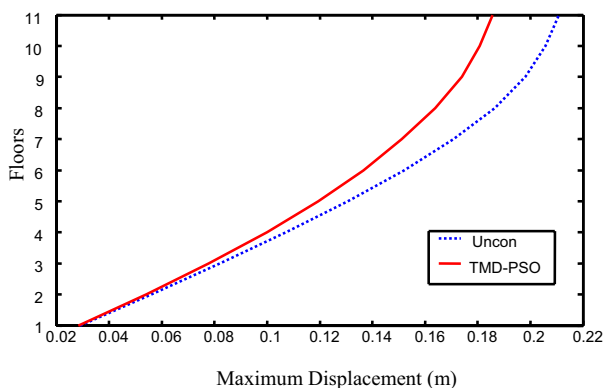


Fig. 12. Maximum displacement of floors under Tabas earthquake.

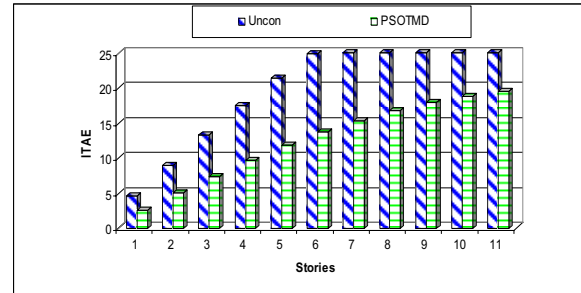


Fig.13. ITAE performance index value for all floors under Tabas earthquake.

TABLE X
 THE AVERAGE REDUCTION (FOR 11 FLOORS) IN MAXIMUM DISPLACEMENT RESPONSE OF THE EXAMPLE BUILDING

Earthquake excitation	Average response reduction percent
	PSOTMD
Elcentro earthquake	40.9318
Kobe earthquake	26.7268
Tabas earthquake	8.7313
Total average	25.4654

TABLE XI
 THE AVERAGE REDUCTION (FOR 11 FLOORS) IN MAXIMUM ACCELERATION RESPONSE OF THE EXAMPLE BUILDING

Earthquake excitation	Average response reduction percent
	PSOTMD
Elcentro earthquake	30.2467
Kobe earthquake	32.2242
Tabas earthquake	10.9083
Total average	24.4997

V. CONCLUSIONS

A new PSO based TMD controller is proposed for the reduction of the tall building responses subjected to earthquake excitations in this paper. This study emphasizes to design and optimize the parameters of the TMD control scheme for achieving the best results in the reduction of the building response under earthquake excitations. The problem of robustly TMD controller design is formatted as an optimization problem based on the ITAE performance index to be solved using PSO technique. The PSO algorithm proposed in this paper is easy to implement without additional computational complexity. Thereby experiments this algorithm gives quite promising results. The ability to jump out the local optima, the convergence precision and speed are remarkably enhanced and thus the high precision and efficiency are achieved. Also, it has simple structure and easy to implement and it does not depend on the nature of the function it minimizes and is insensitive to the initial searching point, there by ensuring quality solution for different trial runs.

For the numerical study, an 11-story realistic building is chosen and the problem is solved in state space, as well as a PSO based TMD controller system are also designed to

control the building response. The system performance characteristics in terms of 'ITAE' and 'the average reduction ratios' reveal that this control strategy is a promising control scheme for the getting the maximum reduction in displacement and acceleration response of the building's stories. It is effective and ensures robust performance for different earthquakes excitations.

REFERENCES

- [1] T.K. Datta, Control of dynamic response of structures. *Proc. of The Indo-US Symposium on Emerging Trends in Vibration and Noise Engineering*, 1996, pp.18-20.
- [2] R. Randa, T.T. Soong, Parametric study and simplified design of mass dampers. *Engineering Structures*, Vol. 20, No. 3, 1998, pp. 193 -204.
- [3] M. Aldawod, B. Samali, F. Naghady, CS. Kwok Kenny, Active control of along wind response of tall building using a fuzzy controller, *Engineering Structures*, Vol. 23, 2001, pp. 1512 - 1522.
- [4] T.T. Soong, R. Hanson, Recent developments in active and hybrid control research in US. *Proc. of the Int. Workshop on Structural Control*, 1993, pp.483-490
- [5] S. Sarbjeet, TK. Datt, Open closed loop linear control of building frames under seismic excitation, *Journal of Structure Engineering*, ASCE, Vol. 124, No. 1, 1998, pp. 43-51.
- [6] W. M. Jenkins, Towards structural optimization via the genetic algorithm, *Engineering Structures*, Vol. 19, No. 4, 1997, pp. 302-308.
- [7] A. Kareem, S. Kline, Performance of multiple tuned mass dampers under random loading, *Journal of Structure Engineering*, ASCE, Vol. 121, No. 2, 1995, pp. 348-361.
- [8] F. Sadek, B. Mohraj, A.W. Taylor, R.M. Chung, A method of estimating the parameters of tuned mass dampers for seismic application. *Earthquake Engineering and Structure Dynamics*, Vol. 26, 1997, pp. 617-635.
- [9] J.N. Yang, Recent advances in active control of civil engineering structures. *Probab. Engineering Mechanics*, Vol. 3, No. 4, 1988.
- [10] B. Samali, M. Al-Dawod, Performance of a five-storey benchmark model using an active tuned mass damper and a fuzzy controller. *Int. Journal of Structure Engineering*, Vol. 25, 2003, pp. 1597-1610.
- [11] QP. Ha, Active structural control using dynamic out put feed back sliding mode. *Proc. of the 2001 Australian Conference on Robotics and Automation*, Sydney, 2001, pp. 14-15.
- [12] MD. Symans, W. Kelly, Fuzzy logic control of bridge structures using intelligent semi-active seismic isolation systems, *Earthquake Engineering and Structure Dynamics*, Vol. 28, 1999, pp. 37-60.
- [13] S. Sarbjeet, TK. Datta, Nonlinear sliding mode control of seismic response of building frames, *Journal of Engineering Mechanics*, ASCE, Vol. 126, No. 6, 2000, pp. 340-347.
- [14] M.N. Hadi, Y. Arfiadi, Optimum design of absorber for MDOF structure, *Journal of Structure Engineering*, Vol. 124, No. 11, 1999, pp. 1272-1279.
- [15] S. Pourzeynali, H.H. Lavasani, A.H. Modarayi, Active control of high rise building structures using fuzzy logic and genetic, *Journal of Structure Engineering*, Vol. 29, 2007, pp. 346-357.
- [16] M.N. Hadi, Y. Arfiadi, Optimum direct (static) output feedback controller using real coded genetic algorithm, *Computer and Structures*, Vol. 79, 2001, pp. 1625-34.
- [17] H. Shayeghi, A. Jalili, H. A. Shayanfar, Multi-stage fuzzy load frequency control using PSO, *Energy Conversion and Management*, Vol. 49, 2008, pp. 2570-80.
- [18] J. Kennedy, R. Eberhart, Y. Shi, *Swarm intelligence*, Morgan Kaufmann Publishers, San Francisco, 2001.
- [19] M. Clerc, J. Kennedy, The particle swarm-explosion, stability, and convergence in a multidimensional complex space, *IEEE Trans. Evolutionary Computation*, 2002, 6 (1): 58-73.
- [20] S. H. Zahiria, S. A. Seyedin, Swarm intelligence based classifiers, *J. Franklin Institute*, 2007, 344: 362-76.
- [21] R.W. Clough, J. Penzien, *Dynamics of structures*, 2nd ed. *Mc Graw-Hill*; New York: 1993.
- [22] K. Kanai, An empirical formula for the spectrum of strong earthquake motions, *Bulletin Earthquake Research Institute*, University of Tokyo, 1961, 39: 85-95.
- [23] www.mathworks.com, MATLAB software, 2009.
- [24] H. Shayeghi, H. Eimani, H.A. Shayanfar, A. Shayeghi, PSO based TMD design for vibration control of tall building structures , *Proc. of the Int. Conf. on Artificial Intelligence (ICAI 09)*, Las Vegas, U.S.A., 2009.