# The Influence of the Commons Structure Modification on the Allocation

Oana Pop, Constantin Barbulescu, Mircea Nemes, and Stefan Kilyeni

*Abstract*—The tracing methods determine the contribution the power system sources have in their supplying. The methods can be used to assess the transmission prices, but also to recover the transmission fixed cost. In this paper is presented the influence of the modification of commons structure has on the specific price of transfer. The operator must make use of a few basic principles about allocation. Most tracing methods are based on the proportional sharing principle. In this paper Kirschen method is used. In order to illustrate this method, the 25-bus test system is used, elaborated within the Electrical Power Engineering Department, from Timisoara, Romania.

*Keywords*—Power systems, P-U bus, P-Q bus, tracing methods.

## I. INTRODUCTION

KIRSCHEN method organises the network's buses and branches in homogeneous groups according to the following concepts: the domain of generator, commons and links [1]-[4]. This method is applied independently both for active and reactive power.

The domain of a generator represents a set of buses, which are supplied by the power of that certain generator. The power produced by a generator supplies a particular bus, if there is a path through the network from the generator to that bus and if the direction of power flow is from the generator to the bus. Note that the domain of the generator from the point of view of the active power is not the same as that from the point of view of the reactive power.

The commons of a generator are defined as a set of neighbouring buses supplied by the same generators. The sets of buses that are unconnected with one another, but are supplied by the same generators are treated as separate commons. A bus belongs to only one common. The rank of a common is defined as the number of generators supplying power to the buses included in this common.

Having the buses divided into commons, each branch can be either internal to a common (for example, it connects two buses which are part of the same common) or external (for example, it connects two buses which are part of different commons). A link is made of one or more external branches connecting the same commons. It is very important to note that power flows from all branches of a link are all in the same

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direction. Furthermore, this flow from a link is always from a common of rank $N$ to a common of rank $M$, where $M$ is always greater than $N$.

If the commons are represented as buses and branches as links, the state of system can be represented by an *acyclic graphic*. This graphic is direct, because the direction of the flow in a link is specified. It is acyclic because the links can only go from a common supplied by fewer generators to a common supplied by more generators.

Based on the previous information, the Kirschen method determines the contribution of the generators to the loads in a common, as well as the contribution of the generators in individual loads and branch flows.

The results obtained provide only a qualitative view of the transmission system. To obtain quantitative information various definitions and fundamental assumptions are necessary.

*The inflow of a common* is defined as the sum of the power injected by sources located in a common and the power imported in this common by external link. This inflow is always positive. For the root node of the state graph, this includes only the power from the sources in the common.

This assumption provides the basis of a recursive method for determining the contribution of each generator to the load in each common.

To calculate the contribution of each generator in each common, the following notations are used:

$$F_{ijk} = C_{ij} \cdot F_{jk} \qquad (1)$$

$$I_k = \sum_j F_{jk} \qquad (2)$$

$$C_{ik} = \frac{\sum_j F_{ijk}}{I_k} \qquad (3)$$

where: $C_{ij}$ – the contribution of the $i$ generator to the load and the outflow of the $j$ common; $C_{ik}$ – the contribution of the $i$ generator to the load and the outflow of the $k$ common; $F_{jk}$ – the flow on the link between the $j$ and $k$ commons; $F_{ijk}$ – the flow on the link between the $j$ and $k$ commons due to the $i$ generator; $I_k$ – the inflow of the $k$ common.

Unfortunately, the inflow of the root bus of the state graph is produced entirely by the generators embedded in these commons. The proportion of the outflow traceable to each of these generators can be resolved and contained in the commons of higher rank.

Considering that all the buses from a certain common cannot be distinguished one from the other from the point of view of power tracing, then the calculus can be applied for the individual loads too, as well as for the internal links from within each common.

Therefore, if the common to which a bus belongs and the contributions of each generator to each common are known, then this allows us to calculate how much power each generator contributes to each load. It also makes it possible to compute what

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proportion of the use of each branch can be apportioned to each generator.

It is reasonable to assume that generators contribute to the losses in a branch in proportion to their use of that branch. Therefore, it is possible to compute what proportion of the outputs of the generator is dissipated in system losses.

## II. DESCRIPTION OF TEST POWER SYSTEM ANALYZED

The test system used for the analysis has 25 buses and 29 branches. It was created on the south-west side of the National Power System. 6 P-U buses, (the slack bus is bus number 1) and 19 P-Q buses; the voltage level for 2 buses is 400 kV, 8 buses are at 220 kV, 10 buses at 110 kV, one bus at 24 kV, 2 buses at 15 kV and 2 buses at 10 kV. In this particular state of function, 4 consumer buses and 3 P-U buses have zero consume power (these 4 P-Q buses become passive buses), and the source from bus number 6 works as a synchronous compensator (Fig. 1).

Among the 29 branches, 17 are electrical overhead lines (one of 400 kV, 8 of 220 kV and 8 of 110 kV), one is under-ground line, 5 transformers and 6 autotransformers [5].

### TABLE I
#### CONFIGURATION OF THE P-U AND P-Q BUSES

| Nr | Load MW | Gen MW | Nr | Load MW | Gen MW |
|----|---------|--------|----|---------|--------|
| 1 | 80 | 711.48 | 14 | 237 | |
| 2 | 8 | 1042.68 | 15 | | |
| 3 | 80 | 680.85 | 16 | | |
| 4 | | 50 | 17 | | |
| 5 | | 20 | 18 | 120 | |
| 6 | | 4 | 19 | 32 | |
| 7 | 350 | | 20 | 22 | |
| 8 | 530 | | 21 | 20 | |
| 9 | 156 | | 22 | 35 | |
| 10 | 175 | | 23 | 12 | |
| 11 | 400 | | 24 | 58 | |
| 12 | | | 25 | 24 | |
| 13 | 170 | | | | |

### TABLE II
#### ACTIVE POWER FLOWS ON THE SYSTEM BRANCHES

| From bus | To bus | From MW | From bus | To bus | From MW |
|----------|--------|---------|----------|--------|---------|
| 1 | 7 | 631.5 | 6 | 13 | 4 |
| 7 | 9 | 241.3 | 11 | 14 | 103.7 |
| 2 | 10 | 1034.7 | 13 | 14 | 133.3 |
| 10 | 8 | 489.8 | 23 | 25 | 11 |
| 7 | 8 | 40.2 | 23 | 24 | 58 |
| 17 | 19 | 23.7 | 10 | 15 | 369.9 |
| 17 | 20 | 24.5 | 15 | 23 | 81 |
| 3 | 11 | 600.8 | 15 | 16 | 48 |
| 12 | 11 | 9.5 | 22 | 21 | 13 |
| 11 | 17 | 48.2 | 16 | 22 | 48 |
| 4 | 18 | 50 | 20 | 19 | 8.3 |
| 9 | 12 | 85.3 | 18 | 20 | 5.8 |
| 12 | 18 | 75.8 | 5 | 21 | 20 |
| 11 | 13 | 58.4 | 21 | 25 | 13 |
| 15 | 13 | 240.9 | | | |

The generated and consumed active powers, for the 25 buses test system are synthesized in Table I. Table II presents the active power flows on the branches of the Test 25 buses test power system.
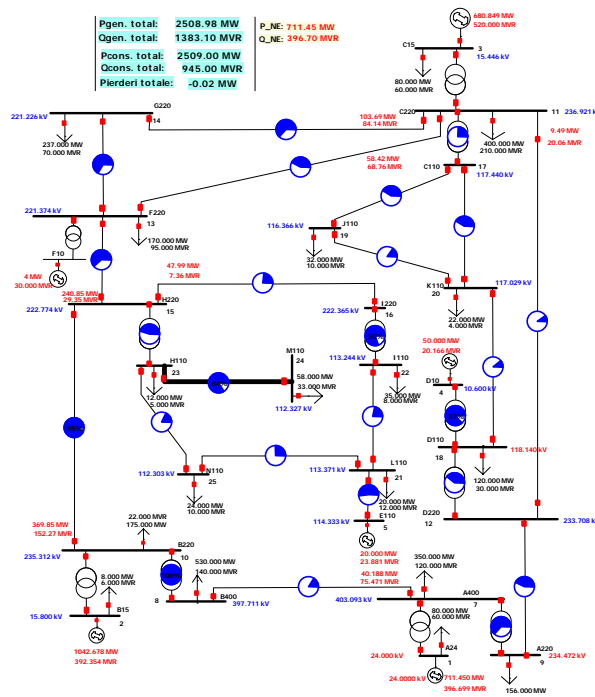


Fig. 1 Configuration of Test 25 buses test power system

## III. NUMERICAL SIMULATIONS

For the test system presented in Fig. 1, four application cases of the Kirschen method are analysed. The differences between them are made by choosing different buses to realise the commons analysed. By using these commons, the contribution of each generator in the active power can be computed. The first case is presented in detail, and for the rest, only the generators participation prices in the active power flow will be presented.

### A. Case 1

According to the structure of the analyzed test system and to the principles stated above, the commons will be defined as presented in Table III.

### TABLE III
#### DEFINITIONS OF ANALYZED SYSTEM COMMONS

| Nr. | Component bus | Input power [MW] | Output power [MW] |
|-----|---------------|------------------|-------------------|
| 1 | 1, 7, 9 | 711.48 | 586 |
| 2 | 2, 8, 10 | 1042.68 | 713 |
| 3 | 3, 11, 19, 20 | 680.85 | 134 |
| 4 | 4, 18, 12 | 50 | 120 |
| 5 | 5, 15, 16, 21, 22, 23, 24, 25 | 20 | 149 |
| 6 | 6, 14, 13 | 4 | 407 |

Table IV contains the definitions of the links between zones.

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TABLE IV
DEFINITIONS OF ANALYZED SYSTEM LINKS

| From | To | Branch | Value [MW] |
|------|----|--------|-----------|
| 1 | 2 | 7_8 | 40.2 |
| 2 | 5 | 10_15 | 369.9 |
| 5 | 6 | 15_13 | 240.9 |
| 1 | 4 | 9_12 | 85.3 |
| 4 | 3 | 12_11,18_20 | 15.3 |
| 3 | 6 | 11_13, 11_14 | 162.1 |

Fig. 2 presents the state graph, which expresses the link between the commons of the analyzed system.
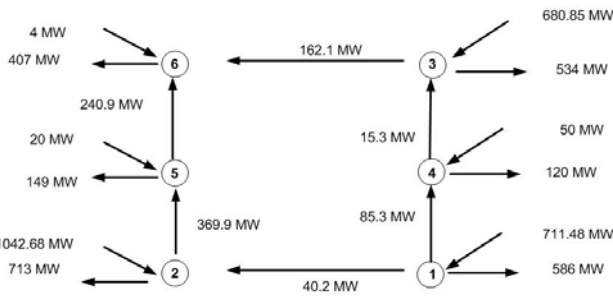


Fig. 2 State graph for case 1

From now on, the contribution of each generator in the load and in the power generated in each common will be computed.

The contributions are calculated starting with the root bus 1:

$$CG_1 = \frac{711.48}{711.48} = 1 \, p.u. \tag{4}$$

The absolute contribution in the inflow of common 2:

$$CG_1 = 40.2 \cdot 1 = 40.2 \, MW \tag{5}$$

$$CG_2 = 1042.68 \cdot 1 = 1042.68 \, MW \tag{6}$$

The relative contribution in the load and outflow of common 2:

$$CG_1 = \frac{40.2}{40.2 + 1042.68} = 0.037123 \, p.u. \tag{7}$$

$$CG_2 = \frac{1042.68}{40.2 + 1042.68} = 0.962877 \, p.u. \tag{8}$$

The absolute contribution in the inflow of common 5:

$$CG_1 = 0.037123 \cdot 369.9 = 13.73188 \, MW \tag{9}$$

$$CG_2 = 0.962877 \cdot 369.9 = 356.1681 \, MW \tag{10}$$

$$CG_5 = 20 \, MW \tag{11}$$

The relative contribution in the load and outflow of common 5:

$$CG_1 = \frac{13.73188}{13.73188 + 356.1681 + 20} = 0.035219 \, p.u. \tag{12}$$

$$CG_2 = \frac{356.1681}{13.73188 + 356.1681 + 20} = 0.913486 \, p.u. \tag{13}$$

$$CG_5 = \frac{20}{13.73188 + 356.1681 + 20} = 0.051295 \, p.u. \tag{14}$$

The absolute contribution in the inflow of common 4:

$$CG_1 = 1 \cdot 85.3 = 85.3 \, MW \tag{15}$$

$$CG_4 = 20 \, MW \tag{16}$$

The relative contributions in the load and outflow of common 4:

$$CG_1 = \frac{85.3}{85.3 + 20} = 0.630451 \, p.u. \tag{17}$$

$$CG_4 = \frac{20}{85.3 + 20} = 0.369549 \, p.u. \tag{18}$$

The absolute contributions in the inflow of common 3:

$$CG_1 = 0.630451 \cdot 15.3 = 9.645898 \, MW \tag{19}$$

$$CG_4 = 0.369549 \cdot 15.3 = 5.654102 \, MW \tag{20}$$

$$CG_3 = 680.85 \, MW \tag{21}$$

Verifying the participations for generators 1 and 4 in the power flow on branch12-11, respectively 18-20.

$$CG_1 = \frac{9.645898}{9.645898 + 5.654102} = 0.6305 \, p.u. \tag{22}$$

$$CG_1 = \frac{5.654102}{9.645898 + 5.654102} = 0.3695 \, p.u. \tag{23}$$

Branch 12-11: $CG_1 = 0.6305 \cdot 9.5 = 5.98928 \, MW \tag{24}$

$$CG_4 = 0.3695 \cdot 9.5 = 3.51072 \, MW \tag{25}$$

Branch 18-20: $CG_1 = 0.6305 \cdot 5.8 = 3.65661 \, MW \tag{26}$

$$CG_4 = 0.3695 \cdot 5.8 = 2.14339 \, MW \tag{27}$$

The relative contributions to the load and outflow of common 3:

$$CG_1 = \frac{9.645898}{9.645898 + 5.654102 + 680.85} = 0.013856 \, p.u. \tag{28}$$

$$CG_4 = \frac{5.654102}{9.645898 + 5.654102 + 680.85} = 0.008122 \, p.u. \tag{29}$$

$$CG_3 = \frac{680.85}{9.645898 + 5.654102 + 680.85} = 0.978022 \, p.u. \tag{30}$$

The absolute contributions to the inflow of common 6:

$$CG_1 = 0.013856 \cdot 162.1 + 0.035219 \cdot 240.9 = 10.73032 \, MW \tag{31}$$

$$CG_4 = 0.008122 \cdot 162.1 = 1.31657 \, MW \tag{32}$$

$$CG_3 = 0.978022 \cdot 162.1 = 158.5374 \, MW \tag{33}$$

$$CG_2 = 0.913486 \cdot 240.9 = 220.0587 \, MW \tag{34}$$

$$CG_2 = 0.051295 \cdot 240.9 = 12.35701 \, MW \tag{35}$$

$$CG_6 = 4 \, MW \tag{36}$$

Using the concept described above, the participations of the 1, 4, 3, 2 and 5 generators in the active power flow on the 11-13, 11-14 and 15-13 branches have been calculated (Table V).

TABLE V
CHECKING THE PARTICIPATION TO SOME SYSTEM BRANCHES

| Branch / Generating unit | 11-13 | 11-14 | 15-13 |
|--------------------------|---------|-------|---------|
| G1 | 0.80919 | 1.44 | 8.48425 |
| G4 | 0.47432 | 0.84 | |
| G3 | 57.1165 | 101 | |
| G2 | | | 220.059 |
| G5 | | | 12.357 |

In what follows, the contribution of each generator in the active power flow of system will be computed [6]. In order to calculate the transfer cost by the MW-km method, the

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following formula will be used [7], [9]:

$$TC_t = \frac{\sum\limits_{k \in t} CL_k P_k}{P_{G_t}} [\$/MW] \qquad (37)$$

where: $TC_t$ represents the specific flow cost for the $t$ transaction; c – the specific cost in \$/MWkm; $L_k$ – the length of the $k$ line in

km; $P_k$ – the transfer power on the $k$ line; $P_{G_t}$ – the power produced by the source of the $t$ transaction. As for the specific cost, the authors used a value for $c = 2\$/MWkm$.

The final results can be studied in Table VI.

TABLE VI
GENERATION CONTRIBUTION TO ACTIVE POWER FLOW ON SYSTEM BRANCHES

| Fr Nr | To Nr | G1 | G2 | G3 | G4 | G5 | G6 |
|---|---|---|---|---|---|---|---|
| 1 | 7 | 227887.81 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 7 | 9 | 147454.65 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 2 | 10 | 0.00 | 25163.70 | 0.00 | 0.00 | 0.00 | 0.00 |
| 10 | 8 | 0.00 | 149654.55 | 0.00 | 0.00 | 0.00 | 0.00 |
| 7 | 8 | 0.00 | 13948.92 | 0.00 | 0.00 | 0.00 | 0.00 |
| 17 | 19 | 23.76 | 0.00 | 2383.21 | 13.93 | 0.00 | 0.00 |
| 17 | 20 | 15.00 | 0.00 | 1504.21 | 8.79 | 0.00 | 0.00 |
| 3 | 11 | 0.00 | 0.00 | 34289.86 | 0.00 | 0.00 | 0.00 |
| 12 | 11 | 1126.66 | 0.00 | 0.00 | 660.41 | 0.00 | 0.00 |
| 11 | 17 | 68.57 | 0.00 | 6878.33 | 40.19 | 0.00 | 0.00 |
| 4 | 18 | 0.00 | 0.00 | 0.00 | 6753.88 | 0.00 | 0.00 |
| 9 | 12 | 14652.16 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 12 | 18 | 10988.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 11 | 13 | 220.33 | 0.00 | 15552.02 | 129.15 | 0.00 | 0.00 |
| 15 | 13 | 644.62 | 16719.71 | 0.00 | 0.00 | 938.87 | 0.00 |
| 6 | 13 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 2201.39 |
| 11 | 14 | 333.47 | 0.00 | 23537.80 | 195.47 | 0.00 | 0.00 |
| 13 | 14 | 237.72 | 5628.91 | 1460.99 | 12.13 | 316.08 | 0.00 |
| 23 | 25 | 34.47 | 894.01 | 0.00 | 0.00 | 0.00 | 0.00 |
| 23 | 24 | 14.34 | 372.02 | 0.00 | 0.00 | 0.00 | 0.00 |
| 10 | 15 | 3344.83 | 86755.92 | 0.00 | 0.00 | 0.00 | 0.00 |
| 15 | 23 | 435.89 | 11305.90 | 0.00 | 0.00 | 0.00 | 0.00 |
| 15 | 16 | 113.78 | 2951.23 | 0.00 | 0.00 | 0.00 | 0.00 |
| 22 | 21 | 14.27 | 370.10 | 0.00 | 0.00 | 0.00 | 0.00 |
| 16 | 22 | 258.31 | 6699.79 | 0.00 | 0.00 | 0.00 | 0.00 |
| 20 | 19 | 114.79 | 0.00 | 710.41 | 67.28 | 0.00 | 0.00 |
| 18 | 20 | 627.14 | 0.00 | 0.00 | 367.61 | 0.00 | 0.00 |
| 5 | 21 | 0.00 | 0.00 | 0.00 | 0.00 | 496.75 | 0.00 |
| 21 | 25 | 14.11 | 365.86 | 0.00 | 0.00 | 584.56 | 0.00 |
| Total | | 408624.664 | 320830.6289 | 86316.81269 | 8248.8463 | 2336.26 | 2201.38535 | 828558.6 |
| TC | | 2436.01806 | 1912.633468 | 514.5781293 | 49.17554 | 13.9276 | 13.1235702 | |
| Participation price | | 3.42387427 | 1.83434368 | 0.755787808 | 0.9835108 | 0.69638 | 3.28089256 | |

*B. Case 2*

According to the structure of the analyzed test system and to the principles stated above, the commons will be defined as presented in Table VII.

TABLE VII
DEFINITIONS OF ANALYZED SYSTEM COMMONS

| Nr. zone | Component buses | Input power [MW] | Output power [MW] |
|---|---|---|---|
| 1 | 1, 7, 9, 12 | 711.48 | 586 |
| 2 | 2, 8, 10, 15 | 1042.68 | 713 |
| 3 | 3, 11, 17, 19 | 680.85 | 112 |
| 4 | 4, 18, 20 | 50 | 142 |
| 5 | 5, 16, 21, 22, 23, 24, 25 | 20 | 149 |
| 6 | 6, 14, 13 | 4 | 407 |

Table VIII contains the definitions of the links between the commons.

Fig. 3 offers the acyclic graph, which express the links between the commons of the analyzed test system, according to case 2.

TABLE VIII
DEFINITIONS OF ANALYZED SYSTEM LINKS

| From | To | Branch | Value [MW] |
|---|---|---|---|
| 1 | 2 | 7_8 | 40.2 |
| 2 | 5 | 15_23,15_16 | 129 |
| 2 | 6 | 15_13 | 240.9 |
| 1 | 4 | 12_18 | 75.8 |
| 4 | 3 | 20_19 | 8.3 |
| 3 | 6 | 11_13, 11_14 | 162.1 |
| 1 | 3 | 12_11 | 9.5 |
| 3 | 4 | 17_20 | 24.5 |

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TABLE IX
PARTICIPATION PRICE FOR CASE 2

|  | G1 | G2 | G3 | G4 | G5 | G6 | |
|---|---|---|---|---|---|---|---|
| Total | 420472.698 | 361513.0963 | 35778.91976 | 7511.1848 | 1081.31 | 2201.38535 | 828558.6 |
| TC | 2506.65019 | 2155.16221 | 213.2962168 | 44.777968 | 6.44622 | 13.1235702 | |
| Participation price | 3.52314919 | 2.066944997 | 0.313279308 | 0.8955594 | 0.32231 | 3.28089256 | |
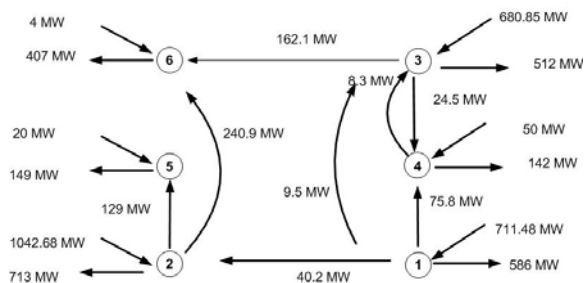

Fig. 3 State graph for case 2

*C. Case 3*

According to the structure of the analyzed test system and to the principles stated above, the commons will be defined as presented in Table X.

TABLE X
DEFINITIONS OF ANALYZED SYSTEM COMMONS

| Zone nr. | Component buses | Input power [MW] | Output power [MW] |
|---|---|---|---|
| 1 | 1, 7, 9, 12 | 711.48 | 586 |
| 2 | 2, 8, 10, 15, 16, 23, 24 | 1042.68 | 783 |
| 3 | 3, 11, 17, 14 | 680.85 | 717 |
| 4 | 4, 18, 20, 19 | 50 | 174 |
| 5 | 5, 21, 22, 25 | 20 | 79 |
| 6 | 6, 13 | 4 | 170 |

Table XI offers the definitions of the links between the commons.

TABLE XI
DEFINITIONS OF ANALYZED SYSTEM LINKS

| From | To | Branch | Value [MW] |
|---|---|---|---|
| 1 | 2 | 7_8 | 40.2 |
| 2 | 5 | 23_25,16_22 | 59 |
| 2 | 6 | 15_13 | 240.9 |
| 1 | 4 | 12_18 | 75.8 |
| 3 | 4 | 17_19,17_20 | 48.2 |
| 6 | 3 | 13_14 | 133.3 |
| 1 | 3 | 12_11 | 9.5 |
| 3 | 6 | 11_13 | 58.4 |

Fig. 4 contains the acyclic graph, which expresses the links between the commons of the analyzed test system, according to case 3.
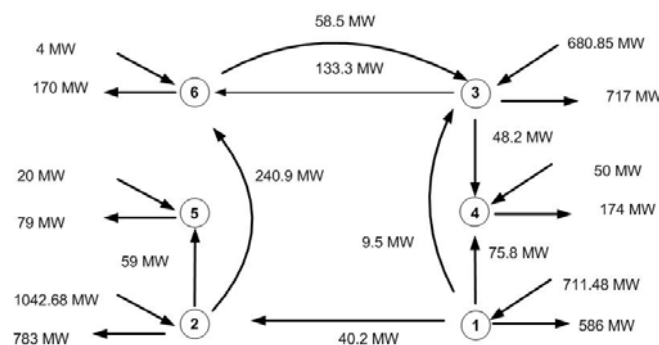

Fig. 4 State graph for case 3

TABLE XII
PARTICIPATION PRICE FOR CASE 3

|  | G1 | G2 | G3 | G4 | G5 | G6 | |
|---|---|---|---|---|---|---|---|
| Total | 527439.399 | 210770.4355 | 79676.49156 | 7217.1496 | 1081.31 | 2373.05843 | 828557.8 |
| TC | 3144.33558 | 1256.510189 | 474.9922502 | 43.025114 | 6.44623 | 14.147013 | |
| Participation price | 4.41942933 | 1.205077482 | 0.697645958 | 0.8605023 | 0.32231 | 3.53675326 | |

*D. Case 4*

TABLE XIII
DEFINITIONS OF ANALYZED SYSTEM COMMONS

| Nr. | Component buses | Input power [MW] | Output power [MW] |
|---|---|---|---|
| 1 | 1, 7, 9, 12 | 711.48 | 586 |
| 2 | 2, 8, 10, 15, 16, 22, 23, 24 | 1042.68 | 818 |
| 3 | 3, 11, 13, 14, 17 | 680.85 | 887 |
| 4 | 4, 18, 20, 19 | 50 | 174 |
| 5 | 5, 21, 25 | 20 | 44 |
| 6 | 6 | 4 | 0 |

TABLE XIV
DEFINITIONS OF ANALYZED SYSTEM LINKS

| From | To | Branch | Value [MW] |
|---|---|---|---|
| 1 | 2 | 7_8 | 40.2 |
| 4 | 3 | 11_12 | 9.5 |
| 3 | 4 | 17_19,17_20 | 48.2 |
| 1 | 4 | 9_12 | 85.3 |
| 2 | 5 | 22_21,23_25 | 24 |
| 6 | 3 | 6_13 | 4 |
| 2 | 3 | 15_13 | 240.9 |

According to the structured of analyzed test system and to the principles stated above, the commons will be defined as

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presented in Table XIII.

Table XIV contains the definitions of the links between the commons.

Fig. 5 presents the acyclic graph, which expresses the links between the commons of the analyzed test system, according to case 4.

In what follows, a series of graphical representations of various costs, using the data from Table VI, IX, XIII and XV, will be drawn.

Fig. 6 offers a 3D representation of the total cost for each generator, using all four analyzed variants.
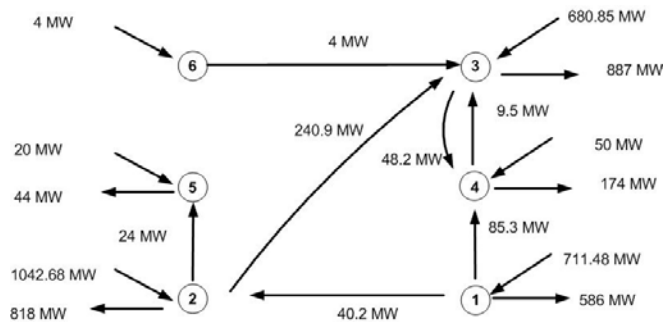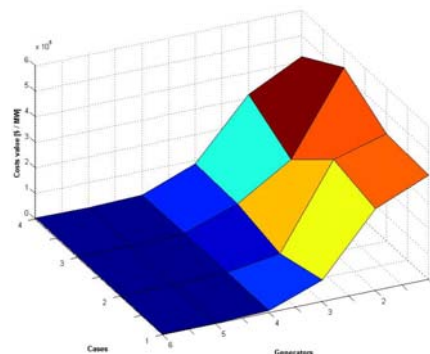
Fig. 6 Total cost representation

Fig. 5 State graph for case 4

TABLE XV
PARTICIPATION PRICE FOR CASE 4

|  | G1 | G2 | G3 | G4 | G5 | G6 |  |
|---|---|---|---|---|---|---|---|
| Total | 418281.6105 | 314354.7091 | 85384.9224 | 7234.681749 | 1081.307885 | 2221.360867 | 828558.5926 |
| TC | 2493.588004 | 1874.027239 | 509.0226604 | 43.129593 | 6.446222601 | 13.2426544 |  |
| Participation price | 3.504790021 | 1.797317719 | 0.747628201 | 0.86259186 | 0.32231113 | 3.3106636 |  |

In Fig. 7 the specific cost for transactions is presented. As input data the specific cost of transfer for transactions for each generator and in all four analyzed cases has been taken into consideration.
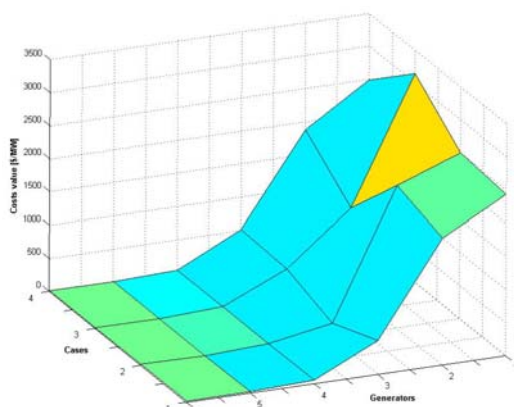
Fig. 7 Specific cost representation of transfer for transactions

In Fig. 8 the participation cost for each generator in all four analyzed cases is presented.
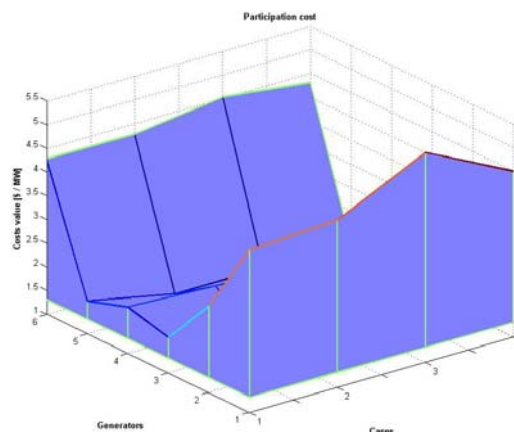
Fig. 8 Participation cost representation

## IV. CONCLUSION

The specific cost of the sources is not decisive for the optimal state of the system, the allocation being tackled from a different point of view. It must be punctuated that for all four chosen cases of commons, the occasional transmission costs are practically identical. There is the possibility of decision according to the common structure based on the acyclic graph. The Kirschen method is suitable to estimate the performance of the system, even if the definition of the commons depends on the system operators.

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