

Utilization of Schnerr-Sauer Cavitation Model for Simulation of Cavitation Inception and Super Cavitation

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Abstract—In this study, the Reynolds-Stress-Navier-Stokes framework is utilized to investigate the flow inside the diesel injector nozzle. The flow is assumed to be multiphase as the formation of vapor by pressure drop is visualized. For pressure and velocity linkage, the coupled algorithm is used. Since the cavitation phenomenon inherently is unsteady, the quasi-steady approach is utilized for saving time and resources in the current study. Schnerr-Sauer cavitation model is used, which was capable of predicting flow behavior both at the initial and final steps of the cavitation process. Two different turbulent models were used in this study to clarify which one is more capable in predicting cavitation inception and super-cavitation. It was found that K- ϵ was more compatible with the Schnerr-Sauer cavitation model; therefore, the mentioned model is used for the rest of this study.

Keywords—CFD, RANS, cavitation, fuel, injector.

I. INTRODUCTION

CAVITATION is the phenomenon in which pressure drops very fast, and as the result of a steep pressure drop, the vapor region forms. The main advantage of cavitation phenomena is the formation of a two-phase flow inside the injector of the nozzle. Cavitation created inside the nozzle augments turbulence value which has a contribution to primary jet breakup, atomization, and combustion [1], [2]. Cavitation bubbles are very vibrant and go through oscillation, coalescence, cloud or cluster formation, and collapse in which bubble collapse, which is the last step of cavitation, is the most detrimental one that causes malfunction among several equipments [3]-[6]. Since the behavior of the flow inside the nozzle has a significant effect on the combustion and spray process, understanding the internal flow inside the nozzle is crucial in order to reduce pollutants as much as we can [7]-[9]. The occurrence of cavitation inside the nozzle is a very useful phenomenon as it can be controlled by injection pressure or even outlet pressure [10], [11]. Streamline contraction leads to narrowing velocity profile by decreasing the effective cross-section of the flow passing the injector [12]-[14].

Several computational and experimental investigations are reported that are focusing on cavitation inception, supercavitation, and the two-phase flow inside diesel injector nozzle [15], [16]. In general, there are two approaches that are mainly used for the prediction of cavitation inside diesel injector nozzle, which are single continuum models that are used as average mixture properties and two-fluid models in

which liquid and vapor phases are treated as two separate substances [17], [18]. Schmidt et al. [19] used thermal equilibrium for developing a model in which uniform distribution in each cell is utilized for the two phases. Afterward, using isentropic flow along with utilizing the Wallis approach, two-phase sound speed was modeled [20]. One of the major drawbacks of the single-phase approach is that turbulence is not considered comprehensively, which removes very crucial stochastic features from the flow. As mentioned earlier, in the two-fluid approach, vapor and liquid phases are considered as a combination of two forms of conservation equations. There are two major categories for the two-fluid model, which are the Eulerian-Eulerian approach and the Eulerian-Lagrangian approach [21].

In the present study, Winklhofer [22] rectangular shape nozzle is used to perform simulation and verification as the mentioned study has useful experimental data for making the comparison and also can be utilized for validation purposes. It is necessary to understand structure and formation in the near and internal nozzle region. Mostly, nozzles that are transparent are used to study cavitation behavior optically inside nozzles. In this study, the Winklhofer nozzle will be verified and validated for subsequent studies.

II. CAVITATION MODEL AND FORMULATION

Mostly cavitation is simulated using three main methods, which are the multiphase flow model, homogenous equilibrium model, and interface tracking model [9], [23]-[25]. In the current study, since the main focus is on severe variation of density, a multiphase flow model is selected in which real transformation is considered; hence, the Schnerr-Sauer cavitation model is used in the current investigation. The transport equation in the mentioned platform can be stated as following:

$$\frac{\partial}{\partial t}(\alpha \cdot \rho_v) + \nabla(\alpha \cdot \rho_v \cdot \vec{V}_V) = \frac{\rho_v \cdot \rho_l}{\rho} \cdot \frac{d\alpha}{dt} \quad (1)$$

In (1), density of vapor is ρ_v , density of liquid is ρ_l , vapor volume fraction is α , velocity of gases phase is \vec{V}_V and time is t . The relationship between density of liquid and density of vapor can be written as mass transfer equation which can be written as following:

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$$R = \frac{\rho_v \rho_l}{\rho} \cdot \frac{d\alpha}{dt} \quad (2)$$

Vapor volume fraction can be written as number of bubbles per unit of volume and radius of bubble as following:

$$\alpha = \frac{n_b \times \frac{4}{3} \times \pi R_b^3}{1 + n_b \times \frac{4}{3} \times \pi R_b^3} \quad (3)$$

in which R is the mass transfer between density of vapor and density of liquid, bubble radius is R_b . Finally, by adding (3) into (2), the following expression for mass transfer will be obtained:

$$R = \frac{\rho_v \rho_l}{\rho} \cdot \alpha \cdot (1 - \alpha) \cdot \frac{3}{R_b} \cdot \sqrt{\frac{2}{3} \cdot \left| \frac{p_v - p_l}{\rho_l} \right|} \quad (4)$$

$$R_b = \left(\frac{\alpha}{1 - \alpha} \cdot \frac{3}{4 \cdot \pi} \cdot \frac{1}{n} \right)^{\frac{1}{3}} \quad (5)$$

Also, p is static pressure of the far field and p_v is the static pressure of vapor.

Discharge coefficient can be written as an expression that includes mass flow rate and pressure difference.

$$C_d = \frac{\dot{m}}{A \sqrt{2 \rho_l (P_{in} - P_{back})}} \quad (6)$$

In (6) \dot{m} is mass flow rate and area of the section of the nozzle that stated as A . Inlet pressure and outlet pressure are orderly P_{in} and P_{back} . Cavitation number (K) inside the nozzle can be defined as following:

$$K = \frac{P_{in} - P_v}{P_{in} - P_{back}} \quad (7)$$

III. GEOMETRY OF THE DOMAIN

The rectangular shape nozzle introduced by Winklhofer et al. [22] is shown in Fig. 1. As the figure depicts, the inlet and outlet areas are assumed to be cubic shape in order to make the boundary condition closer to reality. The length of the orifice is 0.001 m , inlet area of the orifice is $301 \mu\text{m}$ by $300 \mu\text{m}$, and outlet area of the orifice is $284 \mu\text{m}$ by $300 \mu\text{m}$. The inlet radius of the orifice is $20 \mu\text{m}$. The pressure inlet is fixed to 10 MPa and the pressure outlet is fixed to $2 - 5 \text{ MPa}$. The turbulent intensity is $0.16 \times Re^{-1/8}$ for the inlet. Turbulent length scale for the inlet is defined as $0.07D$. Fig. 2 is showing the mesh topology used in this study. The mesh utilized in this work is quad dominant which means that the mesh is not fully structured, while it is mostly structured.

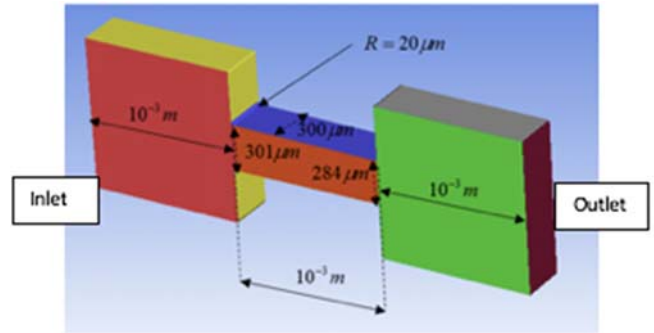


Fig. 1 Rectangular shape nozzle introduced by Winklhofer

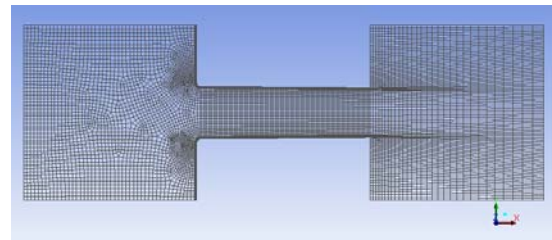


Fig. 2 Mesh for Winklhofer rectangular shape nozzle

IV. RESULT AND DISCUSSION

In this study, cavitation has been investigated both at the initial and final steps of formation. As can be seen in Fig. 3, when the simulated result is compared with the experimental result obtained by Winklhofer et al. [22] in both the initial and final stage of cavitation, the simulation was able to predict the formation of vapor volume fraction as described earlier in this study. When pressure drops down below the critical pressure, which is mostly vaporization pressure, cavitation starts to form, and then it continues to grow up in the orifice area until it reaches the end of the orifice area, which is called supercavitation. Further increase in pressure difference will end up in the formation of choke phenomena which is not favorable and affects the combustion process very adversely. Therefore, it is recommended to control the pressure difference until the flow reaches supercavitation, which helps the atomization process that is supposed to occur after cavitation.

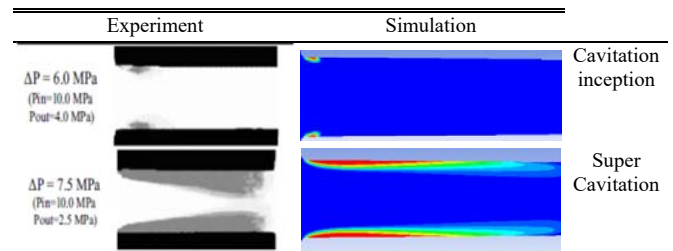


Fig. 3 Presentation of cavitation inception vs. super cavitation with vapor volume fraction

Velocity profile at a location of $53 \mu\text{m}$ from the orifice inlet is shown in Fig. 4, where the inlet pressure is fixed to 100 bar or 10 MPa and the outlet pressure was chosen to be 45 bar and 33 bar separately. Two different turbulent models are utilized in this study, which are $K - \epsilon$ and $K - \omega$ in order to select the

most appropriate turbulent model while Reynolds Stress Navier Stokes (RANS) is utilized. As can be seen from Fig. 4, the average error obtained when $K - \epsilon$ model was utilized, was 1.8% when compared to the experimental data, while the mentioned average error when $K - \epsilon$ was utilized, was 7.2%, which shows the capability of $K - \epsilon$ when cavitation simulation is of interest. Also, it can be seen from Fig. 4, that the current numerical approach was able to predict velocity profile trends at two different pressure differences that can be used as validation as well.

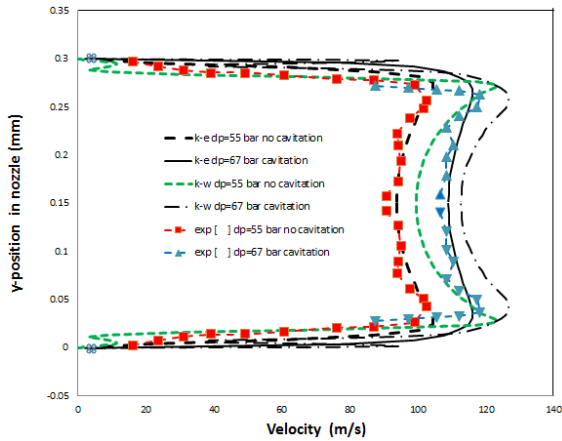


Fig. 4 Velocity profile at $53 \mu\text{m}$ from the orifice inlet at two different pressure differences which are 55 bar and 67 bar when the inlet pressure is fixed to 100 bar

Mass flow rate is shown at different pressure differences in Fig. 5 when two different turbulent approaches are utilized. It can be seen that the $k - \epsilon$ turbulent approach comparing to $k - \omega$ has a better agreement with previous experimental data obtained by Winklhofer et al. [22].

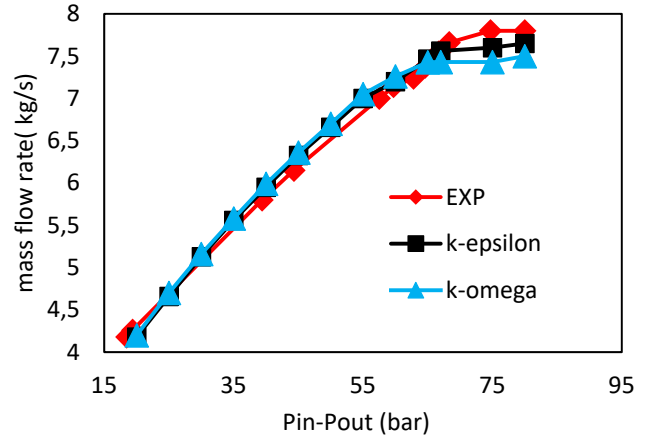
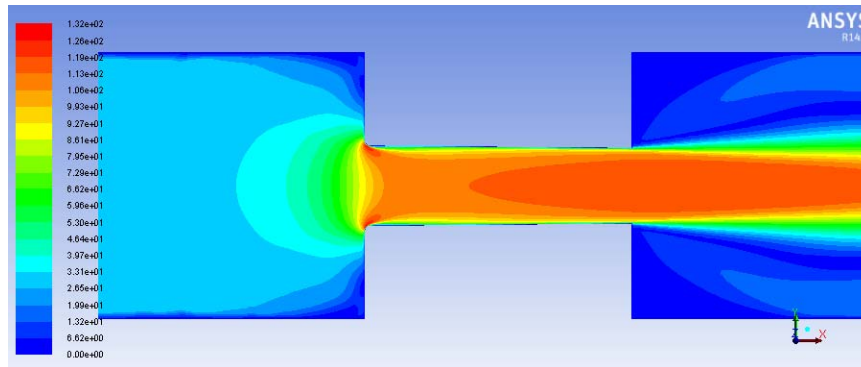
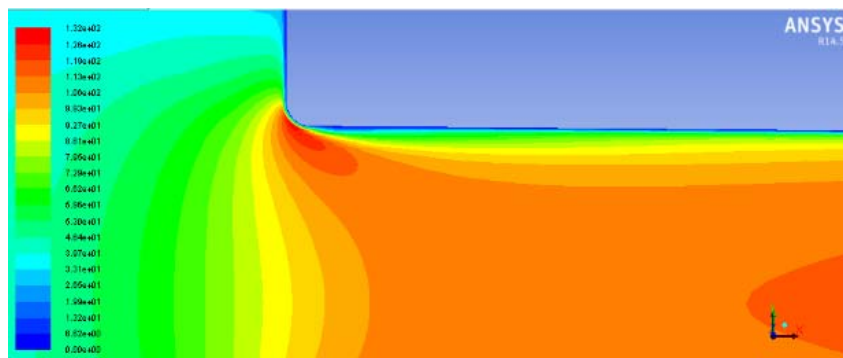


Fig. 5 Mass flow rate at different pressure differences when $k - \epsilon$ and $k - \omega$ compared to experimental data obtained by winklhofer [22]



(a)



(b)

Fig. 6 Velocity distribution at mid plane when $\Delta p = 6 \text{ Mpa}$

Fig. 6 shows velocity distribution at the mid plane of the nozzle when $\Delta p = 6 \text{ Mpa}$. As the mentioned figure shows, the highest amount of velocity is observed at the mid orifice area and near the inlet area. The inlet area is also shown as a close-up view in Fig. 6 (b).

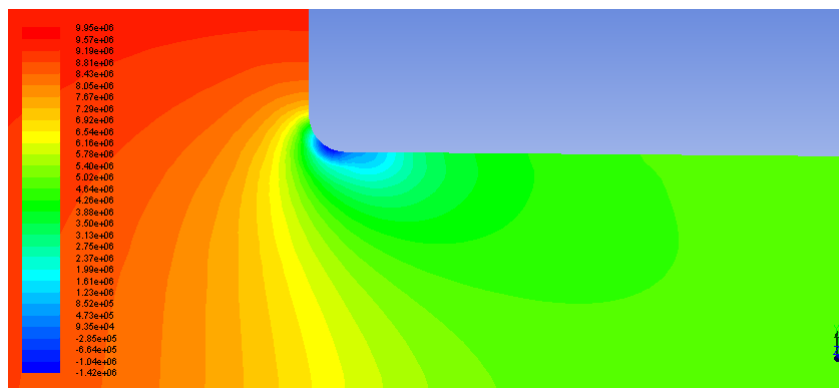


Fig. 7 Pressure distribution at mid plane when $\Delta p = 6 \text{ Mpa}$

Fig. 7 is showing pressure distribution at the inlet of the nozzle. Since $\Delta p = 6 \text{ Mpa}$ is corresponding to the cavitation inception, a very narrow region of low-pressure zone which is indicating the formation of cavitation can be seen at the inlet of the orifice.

V. CONCLUSION

In this study, flow inside the diesel injector nozzle is simulated in which a finite volume framework is utilized for solving RANS equations. Schnerr-Sauer cavitation model is used for simulating cavitation in multiphase flow. The carrying fluid in this study is diesel fuel, and other boundary conditions are following the experimental study for the verification purposes proposed by Winklhofer et al. [22]. The current numerical approach could successfully predict cavitation at both initial and final stages. $K - \omega$ and $K - \epsilon$ turbulent approaches were both investigated, and it was found that results obtained using $K - \epsilon$ have a better agreement with previous experimental data [26]-[31].

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