

# Thrust Enhancement on a Two Dimensional Elliptic Airfoil in a Forward Flight

S. M. Dash, K. B. Lua, T. T. Lim

**Abstract**—This paper presents results of numerical and experimental studies on a two-dimensional (2D) flapping elliptic airfoil in a forward flight condition at Reynolds number of 5000. The study is motivated from an earlier investigation which shows that the deterioration in thrust performance of a sinusoidal heaving and pitching 2D (NACA0012) airfoil at high flapping frequency can be recovered by changing the effective angle of attack profile to square wave, sawtooth, or cosine wave shape. To better understand why such modifications lead to superior thrust performance, we take a closer look at the transient aerodynamic force behavior of an airfoil when the effective angle of attack profile changes gradually from a generic smooth trapezoidal profile to a sinusoid shape by modifying the base length of the trapezoid. The choice of using a smooth trapezoidal profile is to avoid the infinite acceleration condition encountered in the square wave profile. Our results show that the enhancement in the time-averaged thrust performance at high flapping frequency can be attributed to the delay and reduction in the drag producing valley region in the transient thrust force coefficient when the effective angle of attack profile changes from sinusoidal to trapezoidal.

**Keywords**—Two-dimensional Flapping Airfoil, Thrust Performance, Effective Angle of Attack, CFD and Experiments.

## I. INTRODUCTION

THE study of the aerodynamics of a pitching and plunging airfoil is relevant to many engineering applications including Micro-Air-Vehicles (MAVs) and Under-Water-Vehicles (UWVs) which mimics natural flyers or swimmers [1]-[7]. Past studies [1]-[5] have shown that thrust producing conditions of an oscillating airfoil is associated with jet-like flow structures downstream of the airfoil where the vortices are arranged to produce momentum excess. Triantafyllou et al. [6], [7] characterized the thrust performance of flapping foil in terms of flapping frequency ( $f$ ) or Strouhal number ( $S_T$ ). In subsequent studies [8], [9], it was found that although higher flapping frequency produced higher time-average thrust, there exists a critical Strouhal number ( $S_{Tc}$ ), above which thrust performance of a sinusoidal heaving and pitching airfoil deteriorated considerably. In [10], it was found that the deterioration in thrust performance is linked to the transient thrust force profile switching from a single peak parabolic-like shape to drag producing multiple peaks non-parabolic type in one flapping stroke; i.e. upstroke or downstroke. In this paper, we extended our investigation to determine if thrust performance can be further improved by reducing the drag producing valley region in the multiple-peak transient thrust

force profile when the Strouhal number ( $S_T$ ) is above the critical value of  $S_{Tc}$ .

In a related past experiment by [9] on a 2D oscillating NACA0012 airfoil at  $Re=30,000$  and  $S_T$  varying from 0.2 to 0.8, it was found that modifying the instantaneous effective angle of attack profile from sinusoidal to cosine, sawtooth or square-wave type can lead thrust enhancement. Subsequent numerical simulations by [11] and [12] further confirmed the findings of [9]. Although the past studies have provided some valuable insights into the salient factors responsible for the thrust enhancement, the details are still not fully understood. The attempt by [9] to relate the thrust enhancement to changes in the far field wake topology, although useful, is indicative of the mean thrust only; it does not give much insight into the temporal thrust behavior. To address this issue, we systematically investigate how changes in the effective angle of attack profile influence the transient and time-average thrust of flapping foil. Here, we focus on a smooth trapezoidal effective angle of attack profile and vary the base length of the trapezoid until it eventually transforms into a sinusoidal wave.

The present study consisted of both experimental and numerical investigations using a 2D elliptic airfoil. The experiments were conducted in a water channel using the flapping airfoil mechanism previously used by [13]. The numerical simulations were conducted using a commercial CFD package (FLUENT v15.0) with laminar viscous flow model. The simulation was conducted on at  $Re=5000$ ,  $S_T$  from 0.1 to 0.8 and induced effective angle of attack amplitude ( $\alpha_0$ ) from  $10^0$  to  $20^0$ .

The remainder of the paper is arranged as follows. Section II presents the experimental setup and methodology. Section III discusses the numerical scheme, problem definition, and validation of the CFD solver. Results are discussed in Section IV, and some concluding remarks are drawn in Section V.

## II. EXPERIMENTAL SET UP AND PROCEDURE

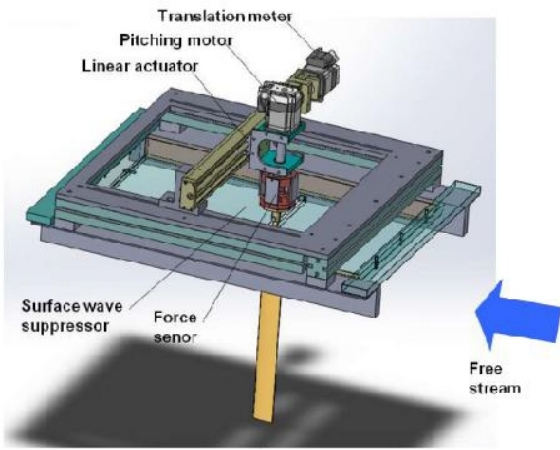
The experiments were conducted in a re-circulating water channel as shown in Fig. 1, where the flapping wing mechanism was placed on top of its test section. The linear translation (heaving) of the elliptic airfoil was controlled by a Mdrive23 stepper motor with fine resolution of 0.005 mm and the rotation (pitching) motion was controlled by a second Mdrive23 stepper motor with resolution of 0.018 deg. Although complete elimination of the vibration from discrete micro-stepping action of the motor is impossible, various measures were adopted to ensure that the vibration was kept to a very minimum level, such that the flow field is unaffected. This minimal level of vibration was encountered by [13] in a

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related investigation on the vortex shedding process of a 2D flapping elliptic wing in a free stream where they found good agreement between their experimental results and the computation of [2].



(a)



(b)

Fig. 1 (a) Two dimensional flapping airfoil setup with (b) details of flapping mechanism

The elliptic airfoil used in the study has a length ( $L$ ) of 0.4 m, chord ( $c$ ) of 0.04 m and maximum thickness ( $t$ ) of 0.005 m. Accordingly, the aspect ratio of the airfoil ( $L/c$ ) was 10, which was much higher than the critical aspect ratio limit [13]-[15] ( $<1.5$ ) to minimize three dimensional effect. To further avoid the influence of the wing tip vortices, the elliptic airfoil was bounded in between two perspex (or plexiglas) endplates. The top endplate was placed on the water surface, which also prevented free surface effects. The base plate of the water tunnel served as the bottom endplate, where the gap was less than 0.002 m.

The force measurement system used in the present study consisted of a two-component force sensor, a Wheatstone bridge, a Butterworth filter, and a PC installed with a data acquisition (A/D) card. The force sensor has four bending bars, where strain gauges were affixed to all the sixteen surfaces of the bars. The measured analog signals were then low-pass filtered at a cut-off frequency of 15 Hz, before they were converted into digital signals by the A/D card with a sampling rate of 200 Hz. These signals were then converted

into two Cartesian forces (normal and axial) and moments by using an A/D conversion calibration matrix. The maximum capacity of the force sensor is  $\pm 10$  N (based on the range of the A/D card) with a minimum resolution of  $\pm 0.003$  N (based on the noise level of the analog output signal from the digital filter). Upon completion of the calibration of the force sensor, a known weight, ranging from 0.059 N to 1.106 N, was applied at different known locations to check the accuracy of the calibration matrix. The errors in the measured forces (by the sensor) were found to be less than 2.0% of the applied weight. Since the measured hydrodynamic forces by the sensor also contained the contribution from the inertia force, the inertia term was removed using the same procedure adopted by [13]. Each set of force measurement was repeated twenty times, and the results were subsequently ensemble-averaged and then digitally smoothed, to resolve the net hydrodynamic force components. The smoothing process only accentuated but did not alter the trend of the measured forces.

### III. COMPUTATIONAL METHODOLOGY

A commercial CFD solver FULENT v15.0 was used to simulate the flow field of a flapping 2D elliptic airfoil. The accuracy and efficiency of FLUENT solver in application to flapping airfoil has been well verified and documented in the literature [16], [17]. Here, we have solved the unsteady two-dimensional Navier-Stokes equations using finite volume method (FVM) with incompressible flow assumption. The governing equations are solved in an inertial reference frame that incorporates a moving mesh following the arbitrary Lagrangian Eulerian (ALE) formulation [18]. A second order upwind scheme was applied for spatial discretization, while the time integration was performed with first-order implicit scheme. The pressure and velocity coupling was satisfied using the Pressure-Implicit with Splitting Operators (PISO) scheme [18] with a higher order approximation of the correction relation between pressure and velocity. The under-relaxation coefficients for pressure, momentum, and body force were set to 1.0. The accuracy of the solver was set to double precision, and the initial condition was maintained as the inlet uniform velocity. The convergence criterion for the adopted iterative method was satisfied with mass and momentum residuals below  $O(10^{-5})$  in magnitude.

#### A. Problem Definition

An elliptic airfoil of thickness to chord ratio 0.125 is selected for this study which is subjected to both pitching and heaving motion. In this case, the resulting effective angle of attack profile as shown in Fig. 2 can be expressed as,

$$\alpha(t) = \arctan\left(\frac{h'(t)}{U_\infty}\right) - \theta(t) \quad (1)$$

$\alpha(t)$ ,  $U_\infty$ ,  $h'(t) = dh(t)/dt$ ,  $\theta(t)$  are instantaneous effective angle of attack of the flapping airfoil, incoming flow velocity, vertical heave velocity and instantaneous pitching angle

respectively. The Reynolds number was fixed at  $Re = \rho U_\infty c / \mu = 5000$ , where  $\rho$  and  $\mu$  are the density and the dynamic viscosity of fluid, respectively.

$$\alpha(t) = \begin{cases} \alpha_0 \sin(2\pi f_1 t^*) & 0 \leq t^* < T_K \\ \alpha_0 & T_K \leq t^* < 0.5 - T_K \\ \alpha_0 \sin(2\pi f_1 (t^* - T_K)) & 0.5 - T_K \leq t^* < 0.5 + T_K \\ -\alpha_0 & 0.5 + T_K \leq t^* < 1.0 - T_K \\ \alpha_0 \sin(2\pi f_1 (t^* - 2T_K)) & 1.0 - T_K \leq t^* < T_K \end{cases} \quad (2)$$

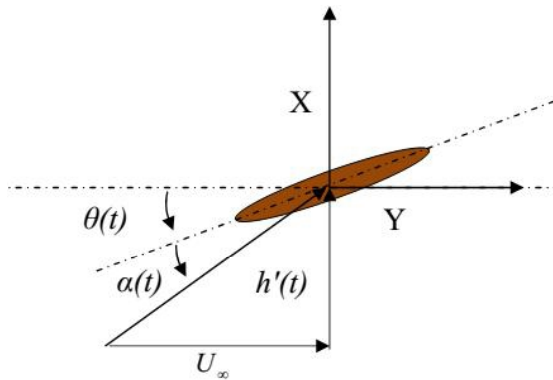


Fig. 2 Schematic drawing showing the effective angle of attack  $\alpha(t)$  seen by an observer travelling with the pivot point of the airfoil

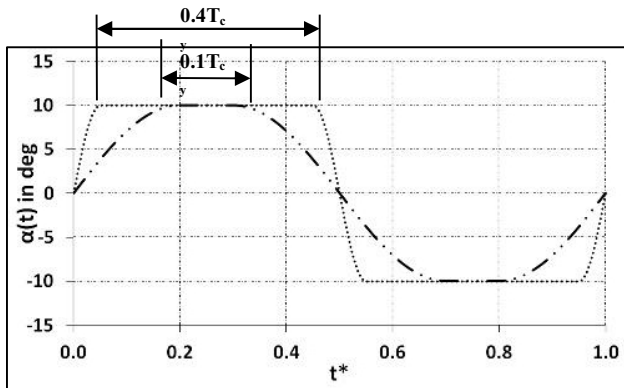


Fig. 3 Different trapezoid base length followed in the present study

TABLE I  
 $T_k$  AND  $f_1$  USED FOR DIFFERENT TRAPEZOID BASE LENGTHS

Cases	$T_k$	$f_1$
$0.4T_{cy}$	0.1	5.00
$0.3T_{cy}$	0.2	2.50
$0.2T_{cy}$	0.3	1.67
$0.1T_{cy}$	0.4	1.25

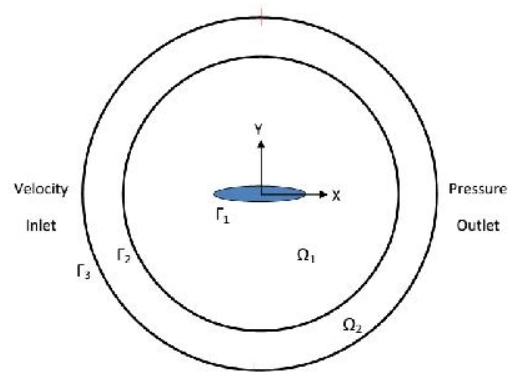
Here, we have followed  $\alpha(t)$  profile as shown in (2). As shown in Fig. 3, five different base lengths of the trapezoidal  $\alpha(t)$  are considered; namely  $0.4T_{cy}$ ,  $0.3T_{cy}$ ,  $0.2T_{cy}$ ,  $0.1T_{cy}$  and  $0.0T_{cy}$  where the corresponding  $T_k$  are  $f_1$  are shown in Table I.

In all the simulations reported here, the non-dimensional flapping cycle time  $T_{cy}$  is set to 1.0. Note that the base length of  $0.0T_{cy}$  produces the smooth trapezoidal profile similar to the sinusoidal  $\alpha(t)$  profile adopted by [11] and [9]. In order to maintain the smooth trapezoidal  $\alpha(t)$ , only the pitching motion profile is altered using (1) while the heaving motion profile remains sinusoidal as expressed in (3):

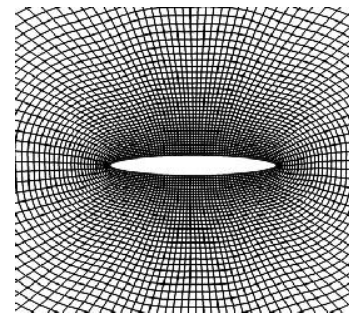
$$h(t) = h_0 \cos(\omega t) \quad (3)$$

where  $h_0$  is the heaving amplitude,  $\omega = 2\pi f$  is the angular frequency,  $f$  is the corresponding flapping frequency, and  $\phi$  is the phase angle between heaving and pitching motion. Only the case with  $\phi = 90$  deg was considered here since this phase angle produces maximum thrust performance with better efficiency [14].

### B. Computational Domain



(a)



(b)

Fig. 4 (a) Schematic of O-type computational domain and (b) body conformal moving mesh around the elliptical airfoil

To analyze the thrust performance of the flapping airfoil, three different effective angles of attack amplitudes, namely  $\alpha_0 = 10, 15$  and  $20$  degrees were selected while  $h_0$  was made constant at  $0.75c$ .  $S_T$  ranged from 0.1 to 0.8 and depending on its value, the  $\theta(t)$  is derived from (1) with a 90 deg phase difference from the corresponding heaving motion.

Lift (L) and drag (D) are defined as the component of the force normal to and parallel to the flapping motion,

respectively. The corresponding lift and drag coefficients are determined from

$$C_L = \frac{L}{0.5\rho U_\infty^2 S} \quad (4)$$

$$C_D = \frac{D}{0.5\rho U_\infty^2 S} \quad (5)$$

where  $S$  is the airfoil planform area and is set to  $S=1.0$ . The thrust coefficient  $C_T$  is obtained by computing the negative component of  $C_D$ .

In the present simulation, an O-type computational domain as shown in Fig. 4 is used. This domain consists of two zones; an inner zone  $\Omega_1$  (rotating and translating) and an outer zone  $\Omega_2$  (only translating). The elliptic airfoil  $\Gamma_1$  with reference length scale  $c$  (=chord length) is located at the centre of the computational domain. The outer boundary  $\Gamma_3$  is located at a radius of  $30c$  which is sufficiently far from the airfoil and has negligible far-field boundary influence (ref. Table I). At the inlet, velocity boundary condition is defined by setting the incoming flow along X direction only, and atmospheric pressure boundary condition was applied at the outlet. A sliding interface boundary condition was enforced between the zones  $\Omega_1$  and  $\Omega_2$  to ensure time dependent momentum flux continuity across the sliding interface  $\Omega_1$  and  $\Omega_2$ . Moreover, the outer boundary of  $\Omega_1$  is located at  $15c$ , which is sufficiently far to have negligible influence on the airfoil as will be discussed later in the validation study (ref. Table II).

To ensure accurate result, high quality moving mesh is generated near the elliptic airfoil. To do this, a conformal mapping was used to create the body-conformal mesh. The intermediate boundary  $\Gamma_2$  separates the inner conformal mesh ( $\Omega_1$ ) and the outer mesh ( $\Omega_2$ ). The complete inner mesh  $\Omega_1$  moved according to the airfoil kinematics, while sliding interface boundary condition maintained the flux continuity across the outer mesh  $\Omega_2$  without need to perform re-meshing.

### C. Validation with Oscillating NACA0012 Airfoil

Validation was carried out using an oscillating NACA0012 airfoil subjected to simple harmonic pitching and heaving motion according to (6) and (7):

$$h(t) = h_0 \cos(\omega t) \quad (6)$$

$$\theta(t) = \theta_0 \cos(\omega t - \phi) \quad (7)$$

This flapping problem was previously investigated experimentally by [14] and later numerically by [11]. Here, we have adopted the same flow conditions, namely  $h_0 = 0.75c$ ,  $Re = 20,000$ ,  $\phi = 90$  deg and  $\alpha_0 = 15$  deg, and the Strouhal number was varied from 0.1 to 0.5 for validation purpose.

TABLE II  
 DOMAIN DEPENDENCY STUDY TO CHECK THE SIZE INFLUENCE OF REGION  $\Omega_1$  AND REGION  $\Omega_2$

Cases	$\Omega_1$ Radius	$\Omega_2$ Radius	Avg. $C_T$	% Error =
				$\left  \frac{C_{T_{NewDomain}} - C_{T_{OldDomain}}}{C_{T_{NewDomain}}} \right  \times 100$
Case 1	10c	20c	0.3824	--
Case 2	15c	30c	0.3815	0.24
Case 3	20c	40c	0.3810	0.13

A computational domain was generated with a NACA0012 airfoil placed at the center of the domain. The domain dependency study was conducted to determine a suitable size of inner  $\Omega_1$  zone and outer  $\Omega_2$  zone. We have proportionately increased the radius of zone  $\Omega_1$  and  $\Omega_2$  and computed the average  $C_T$  for  $\alpha_0 = 15$  deg,  $S_T=0.3$ . The results are shown in Table I. Based on the insignificant error ( $< 0.24\%$ ) in the average  $C_T$  results, the domain size of  $\Omega_1=15c$  and  $\Omega_2=30c$  were selected for this and subsequent simulations. Similarly, the mesh independency check were conducted to determine a suitable mesh size, and from the results presented in Table III, a mesh size with 194700 cells and 1000 time steps per cycle were selected, where the error in the average  $C_T$  is  $< 0.32\%$ . The grid resolution around the airfoil up to one chord length was 13860 ( $198 \times 70$ ). This enabled the leading and trailing edge vortices to be captured with at least 1000 cells.

TABLE III  
 GRID INDEPENDENT STUDY TO CHECK THE INFLUENCE OF MESH SIZES

	Number of Cells	Avg. $C_T$	% Error =
			$\left  \frac{C_{T_{NewMesh}} - C_{T_{OldMesh}}}{C_{T_{NewMesh}}} \right  \times 100$
Mesh 1	104400	0.3861	--
Mesh 2	146100	0.3824	0.99
Mesh 3	194700	0.3812	0.32
Mesh 4	239700	0.3807	0.13

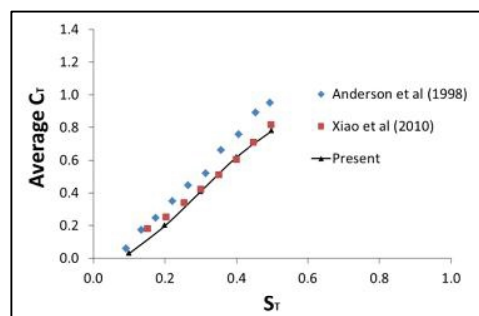


Fig. 5 Time average  $C_T$  of a NACA 0012 undergoing SHM.  $h_0 = 0.75c$ ,  $Re = 20,000$ ,  $\phi = 90$  deg and  $\alpha_0 = 15$  deg. Comparison with the numerical result of [11] performed under the same condition. The experimental results of [14] were obtained at a higher  $Re=40,000$

Fig. 5 compares the time-average  $C_T$  obtained in the present simulations with the experimental results of [14] and laminar numerical simulations of [11]. It can be observed from the figure that reasonably good agreement was obtained. The slight deviation from the experimental results of [14], may be

due to the  $Re$  effects; the experiments were conducted at  $Re=40,000$  while the present simulations carried out at  $Re=20,000$ . Nevertheless, both results show similar trend.

Having established the accuracy of the FLUENT v15.0 solver in capturing the flow features of flapping airfoil, we proceeded to perform the simulation, and the results are presented in the next section.

#### IV. RESULTS AND DISCUSSIONS

In this section, we examine mean of alleviating the deterioration in the thrust performance of the oscillating airfoil at flapping frequency beyond  $S_{Tc}$ .

To verify that thrust degradation occurs when flapping frequency is above a certain critical value; we start with a case in which the elliptic airfoil is subjected to sinusoidal heaving and pitching (SHM) motion as shown in (6) and (7). The Reynolds number was maintained constant at  $Re=5000$  while  $S_T$  ranged from 0.1 to 0.8 for three different constant peak magnitude of the effective angle of attacks ( $\alpha_0$ ), namely 10, 15 and 20 deg. The time-averaged thrust performance ( $C_T$ ) is plotted in Fig. 6, which clearly indicates that the thrust performance initially increases with increasing flapping frequency. However, above a certain critical  $S_{Tc}$ , it degrades significantly for all  $\alpha_0$ . This observation is in agreement with the findings of [9] and [11].

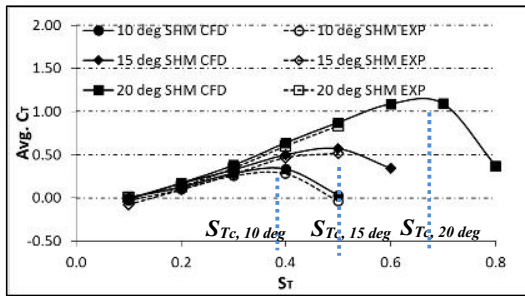
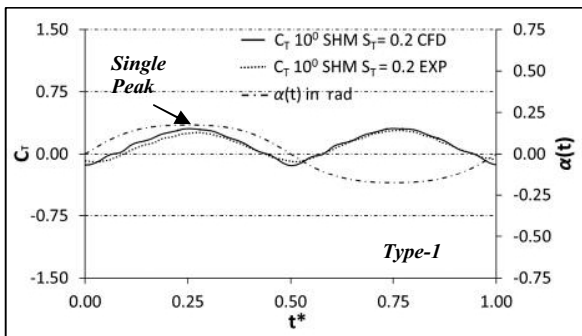
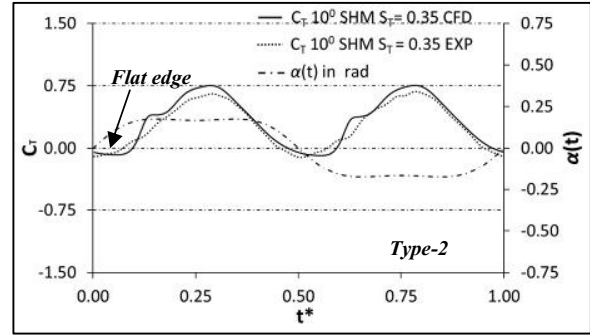


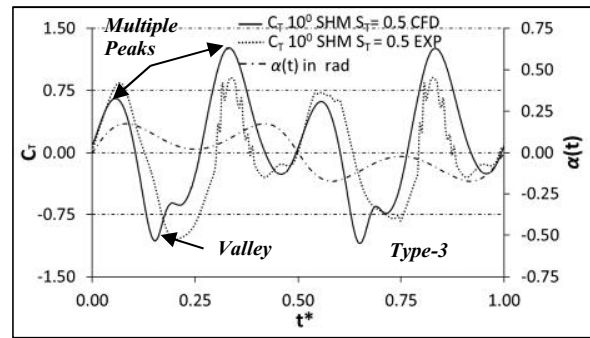
Fig. 6 Time averaged  $C_T$  for different  $S_T$  with varied  $\alpha_0$  (namely 10, 15 and 20 degs), where the vertical dotted lines represent  $S_{Tc}$ . The comparison between experiment and numerical results are also shown



(a)



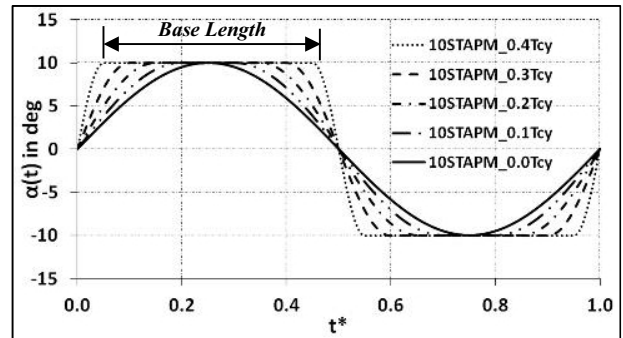
(b)



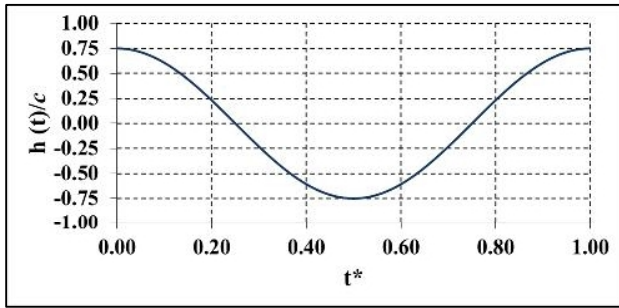
(c)

Fig. 7 Categories of transient thrust coefficient  $C_T$  and the profiles of the effective angle of attack  $\alpha(t)$ . (a)  $\alpha_0 = 10^\circ$ ,  $S_T = 0.2$ , (b)  $\alpha_0 = 10^\circ$ ,  $S_T = 0.35$  and (c)  $\alpha_0 = 10^\circ$ ,  $S_T = 0.5$

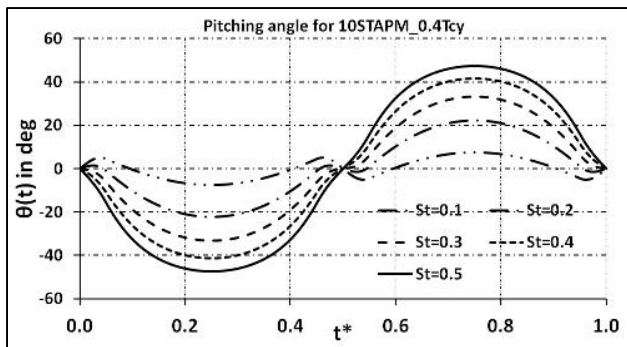
In [10], it was found that as flapping frequency increases, the thrust performance of the airfoil undergoing SHM is associated with transient  $C_T$  switching from a single peak (Type-1) to a single peak with flat edge (Type-2) and then to multiple peaks (Type-3) in one flapping stroke (upstroke or downstroke) as shown in Fig. 7. The thrust deterioration when  $S_T > S_{Tc}$  can be attributed to the drag producing valley in Fig. 7 (c). The associated flow physics and other details of this transient  $C_T$  profile are discussed in [10] and hence will not be repeated here for brevity. The present study focuses more on possible means of alleviating thrust deterioration when  $S_T > S_{Tc}$ .



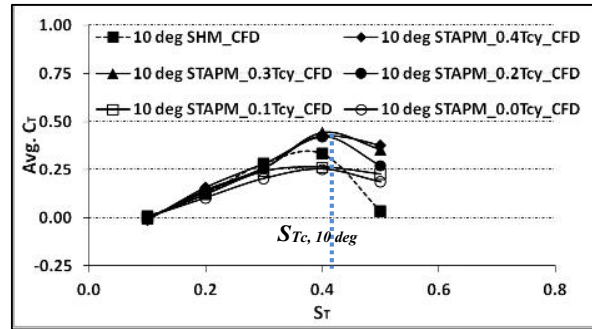
(a)



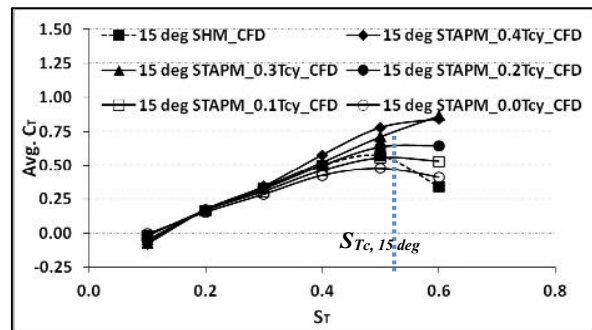
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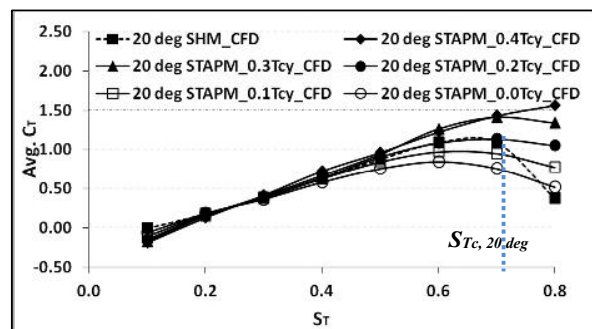
(c)



(a)



(b)



(c)

Fig. 8 (a) The effective angle of attack profiles that gradually changes from smooth trapezoidal to sinusoidal type with reduction in trapezoid base length. Here, (b) and (c) shows the sample heaving and pitching kinematics of the flapping elliptic airfoil for smooth trapezoidal effective angle of attack profile with  $\alpha_0 = 10^\circ$  and base length of  $0.4T_{cy}$

In related past studies [9] and [11] on the 2D oscillating airfoil, it was found that the degradation in thrust performance of the airfoil subjected to SHM flapping motion beyond  $ST > ST_c$  may be recovered by altering the effective angle of attack profile to square wave or cosine wave type. They associated this thrust recovery to formation of reverse von-Karman vortex street. But exactly how it affects the temporal force generation is not entirely clear.

In the present study, instead of using a square wave effective angle of attack profile, which contains infinite acceleration condition at sharp corners, we used a smooth trapezoidal effective angle of attack profile that avoids the drawbacks of the square wave. Subsequently, we reduced the trapezoid base length (see Fig. 8 (a)) until the trapezoid transforms into a sinusoidal wave. This gradual alteration in the effective angle of attack profile would help to enlighten the best thrust generating condition. As before, we used three different effective angle of attack amplitudes ( $\alpha_0$ ), namely 10, 15 and 20 deg. For a fixed heaving amplitude  $h_0 (= 0.75c)$ , constant  $\alpha_0$  is maintained at different  $ST$  by adjusting the pitching amplitudes  $\theta_0$  using (1). One such sample calculated pitching angle profiles are shown in Fig. 8 (c) for the smooth trapezoidal effective angle of attack profile with  $\alpha_0 = 10$  deg and  $ST$  in the range 0.1 to 0.5.

Fig. 9 Time average  $C_T$  performance as function of  $ST$  of the elliptic airfoil for smooth trapezoidal effective angle of attack profile compared with sinusoidal heaving and pitching kinematics of the flapping airfoil for (a)  $\alpha_0 = 10^\circ$ , (b)  $\alpha_0 = 15^\circ$  and (c)  $\alpha_0 = 20^\circ$ .

The time-averaged  $C_T$  of the airfoil with this smooth trapezoidal effective angle of attack profile are shown in Fig. 9 for  $\alpha_0 = 10, 15$  and  $20$  deg and at different  $ST$ . From the figure, it can be observed that the thrust performance at low and intermediate  $ST$  for the smooth trapezoidal is similar to that of SHM. However, at  $ST > ST_c$ , the thrust performance is enhanced for smooth trapezoidal effective angle of attack profiles. This observation is consistent for all  $\alpha_0$  considered in this study. Furthermore, the thrust performance is highest when the base length of the smooth trapezoid effective angle of attack profile is broadest i.e. for  $0.4T_{cy}$ . The performance decreases with the reduction in the trapezoid base length (compare  $C_T$  for  $0.4T_{cy}$  to  $0.0T_{cy}$  in Fig. 9).

To better understand the behavior of time-averaged  $C_T$  variation in Fig. 9, we take a closer look at the transient  $C_T$  for different values of  $S_T$  and  $\alpha_0$  over one flapping cycle. For the case of  $\alpha_0 = 10^\circ$ , Fig. 10 shows the transient  $C_T$  for smooth trapezoidal effective angle of attack profiles as a function of  $S_T$  during the 6<sup>th</sup> flapping cycle, when the periodic flow condition has already been established. Generally, the transient  $C_T$  profiles can be broadly categorized into three types, namely Type-1, Type-2, and Type-3. To the best of our knowledge, these characteristics have not been previously reported in the literature.

The Type-1 and Type-2 transient  $C_T$  profiles mainly occur below the critical  $S_{Tc}$  where the time-average  $C_T$  increases monotonically with  $S_T$ . The Type-1 profile is characterized by a single peak in the transient  $C_T$  variation over one flapping stroke (see Fig. 10 (a)) which is observed at low  $S_T$ . The Type-2 profile is similar to Type-1 except that it contains a flat edge just after the stroke reversal (see Fig. 10 (b)). The Type-2 pattern is observed at intermediate  $S_T$ . The Type-3 profile (see Fig. 10 (c)) differs from the other two types in that multiple peaks are observed over a given stroke at  $S_T > S_{Tc}$  when the time-average  $C_T$  deteriorated (see Fig. 9). This thrust deterioration is contributed from the drag producing valley region in the transient  $C_T$  plots (see Fig. 10 (c)). Further note that the time-average thrust deterioration is less for the broad trapezoidal profile (see for the case of  $0.4T_{cy}$  in Fig. 9), where the transient  $C_T$  is significantly different from the SHM (compare for the case of  $0.4T_{cy}$  and SHM in Fig. 10 (c)).

Based on the trend of Type-3 transient  $C_T$  profile, we further sub-categorize this type into Type-3a and Type-3b. In Type-3a, just after the stroke reversal, the transient  $C_T$  increases and attains the first peak before falling into the drag producing valley region. On the other hand, in Type-3b, after the stroke reversal, a valley region is formed which later increases to form the first peak. Moreover, Type-3b has a second valley and second peak region just before the stroke reversal (see Fig. 10 (c)). The Type-3a pattern is observed for the trapezoidal profile with a broader trapezoid base length ( $>0.3T_{cy}$ ) as well as the SHM. On the other hand, the Type-3b pattern is observed for the trapezoidal profile with smaller trapezoid base length ( $<0.3T_{cy}$ ). Note that for both Type-3a and Type-3b, the drag producing valley region is comparatively reduced for the smooth trapezoidal profile which results in higher time average  $C_T$  than SHM (ref. Fig. 9). Again, this drag producing region increases with increasing flapping frequency (or  $S_T$ ), which further degrades the time-averaged  $C_T$ . It is worth noting that as  $\alpha_0$  increases, the transition of the transient  $C_T$  profiles from Type-1 to Type-2 and then to Type-3 is delayed to higher and higher  $S_T$  which further helps in thrust enhancement at higher flapping frequency or  $S_T$ .

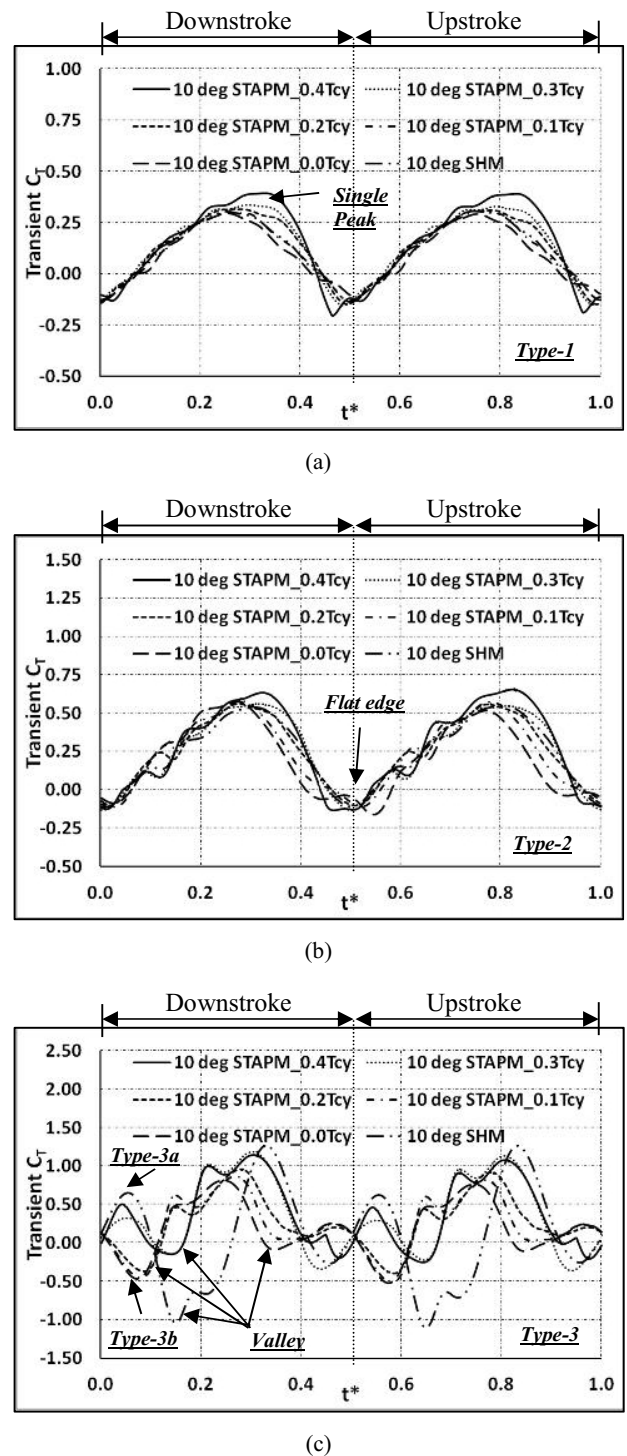


Fig. 10 Categories of the transient thrust coefficient  $C_T$  for smooth trapezoidal effective angle of attack profiles compared with SHM type flapping of the airfoil, for  $\alpha_0 = 10^\circ$  and (a)  $S_T = 0.2$ , (b)  $S_T = 0.3$  and (c)  $S_T = 0.5$

## V. CONCLUSIONS

Numerical and experimental studies have been conducted to investigate thrust performance of a 2D flapping elliptic airfoil in a forward flight condition at  $Re = 5000$ . The results show

that for all effective angle of attack profiles, higher flapping frequency produces higher time-averaged thrust  $C_T$  up to a certain critical Strouhal number ( $S_{Tc}$ ); beyond which thrust generation deteriorated. The thrust deterioration can be alleviated by using a smooth trapezoidal effective angle of attack profile with a broader trapezoid base length. Furthermore, for a fixed  $\alpha_0$ , increasing  $S_T$  to higher and higher value causes the transient  $C_T$  to switch from Type-1 (single peak) to Type-2 (single peak with flat edge) and finally to Type-3 (multiple peaks) pattern after crossing the critical Strouhal number  $S_{Tc}$ . The drag producing valley region in multiple-peak or Type-3 transient  $C_T$  pattern is mainly altered with modified smooth trapezoidal effective angle of attack profile, which subsequently bring enhancement in thrust performance.

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