APPLE: Providing Absolute and Proportional Throughput Guarantees in Wireless LANs

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Abstract—This paper proposes an APPLE scheme that aims at providing absolute and proportional throughput guarantees, and maximizing system throughput simultaneously for wireless LANs with homogeneous and heterogeneous traffic. We formulate our objectives as an optimization problem, present its exact and approximate solutions, and prove the existence and uniqueness of the approximate solution. Simulations validate that APPLE scheme is accurate, and the approximate solution can well achieve the desired objectives already.

Keywords—IEEE 802.11e, throughput guarantee, priority.

I. INTRODUCTION

IEEE 802.11e EDCA [1] can provide differentiated services when a variety of applications coexist. However, it is more desirable to provide different levels of guaranteed services simultaneously for many multimedia applications.

In our APPLE scheme, we consider an EDCA network with one high-priority (HP) class and one low-priority (LP) class. By setting different contention windows (CWs), APPLE aims at achieving three objectives simultaneously: providing an absolute (or a fixed) throughput guarantee for HP nodes, and a proportional throughput guarantee for LP nodes (where all LP nodes share the available bandwidth according to the desired ratios), and maximizing the system throughput. We present the exact and approximate solutions to the optimal CWs, and prove the existence and uniqueness of the approximate solution. Our experiment verifies that the approximate solution can well achieve the desired objectives already.

A distinct difference between our APPLE scheme and the related schemes is that we can achieve the above three objectives simultaneously in the general network (i.e. each node may have an arbitrary packet size), while the others just provide one or two of them under the assumption that all nodes have the same packet size. For example, the scheme in [2] just provided absolute throughput guarantee, not considering proportional throughput guarantee. The scheme in [3] only provided a weighted bandwidth allocation, not considering the absolute throughput guarantee. The scheme in [4] focused on supporting absolute and proportional priorities, rather than absolute and proportional throughput guarantees. Supporting absolute priority means that absolute-priority nodes will always benefit from all available throughput even if some non-absolute-priority nodes exist already, consequently lowering the bandwidth utilization because they may acquire more bandwidth than the required one. In contrast, supporting absolute throughput guarantee in APPLE scheme means that HP nodes are guaranteed to acquire the bandwidth for providing the required throughput only, rather than occupy more bandwidth. Another significant difference is that most of the related papers did not discuss the existence and uniqueness of the solutions.

The rest of this paper is organized as follows. Section II introduces model assumptions and the problem formulation. Section III specifies the optimal attempt rate. Section IV verifies the accuracy of our model. Finally, Section V concludes this paper.

II. MODEL ASSUMPTIONS AND PROBLEM FORMULATION

In APPLE scheme, we consider a one-hop wireless LAN with two classes: HP class and LP class. The HP (LP) class has \( n \) \((m)\) nodes and therefore the total node number is \( N = n + m \). Each node \( i \), \( 1 \leq i \leq N \), always generates a random backoff count uniformly distributed in \([0, CW_i]\) for each new transmission or retransmission, where \( CW_i > 1 \). All nodes send data to the AP (access point), while the AP only acts as a receiver. We assume that 1) all nodes can hear each other and run in the basic mode; 2) ideal channel conditions (i.e., the transmission errors are a result of packet collision only); and 3) all nodes are in saturated operation (i.e., each node always has packets to transmit) and have arbitrary packet size.

We now formulate our problem. Let \( \beta \triangleq (\beta_1, \beta_2, ..., \beta_N) \), where \( \beta_i \) represents the attempt rate of node \( i \) per slot (namely, the mean number that node \( i \) attempts to transmit a packet in a slot). In saturated operation, \( \beta_i \) is calculated by \( CW_i \) as [5],

\[
\beta_i = \frac{2}{CW_i + 1}. \tag{1}
\]

Then, finding the optimal \((CW_1, CW_2, ..., CW_N)\) boils down to finding the optimal \( \beta \).

Let \( \Gamma_i \triangleq \Gamma_i(\beta) \), \( 1 \leq i \leq N \), be the throughput of node \( i \). Let \( a_i \), \( 1 \leq i \leq n \), represent the fixed throughput required by each HP node \( i \). Let \( r_i \), \( 1 \leq i \leq m \), represent the proportional throughput ratio between LP nodes \( n+i \) and \( n+1 \). In the considered wireless LAN, APPLE desires to find the optimal \( \beta \), so as to guarantee each HP node’s fixed throughput requirement \( a_i \), each LP node’s proportional throughput requirement \( r_i \), and at the same time maximize the system throughput \( \sum_{i=1}^{N} \Gamma_i \).

The optimal \( \beta = \arg \max_\beta \sum_{i=1}^{N} \Gamma_i \) \( \tag{2} \)
over $\Gamma_i = a_i, 1 \leq i \leq n,
\frac{\Gamma_{n+i}}{\Gamma_{n+1}} = r_i, 1 \leq i \leq m. \quad (3)

In the next section, we will express the throughput $\Gamma_i$ and find the optimal $\beta$.

III. THE OPTIMAL ATTEMPT RATE

This section first expresses the per-node throughput $\Gamma_i$, and then calculates the exact and approximate solutions to the optimal $\beta$.

A. Per-node Throughput

Denote $P_e$ as the probability that a slot is idle. We have

$$P_e = \Pi_{i=1}^{N} (1 - \beta_i). \quad (5)$$

Let $\Omega$ be the mean time that elapses for one decrement of the back-off counter. Note that the back-off counter decreases by one for each idle slot and is suspended when the channel is busy. For the general network with arbitrary packet size, the successful transmission time of each node depends on its packet size only. If multiple nodes are in collision, however, the collision time should be calculated based on the larger or the largest packet size. Assume that the packet size of each node is $L_i$, $L_1 \leq L_2 \leq \ldots \leq L_N$, then $\Omega$ can be expressed by

$$\Omega = \left\{ \begin{array}{ll}
\sigma, & 1 \leq i \leq N - 1, \\
T_o^n\beta, & \beta_i \prod_{j=1}^{N} (1 - \beta_j), & 1 \leq i \leq N - 1, \\
T_o^n\beta, & \beta_N.
\end{array} \right. \quad (6)

where $\sigma$ is the duration of one time slot; $T_o^n \gg \sigma$ is the time that the channel is occupied by node $i$, and $T_o^n$ is given in Table I. So the mean value of $\Omega$ is

$$\Omega = \sigma\Pi_{i=1}^{N} (1 - \beta_i) + \sum_{i=1}^{N-1} T_o^n\beta_i \prod_{j=1}^{N} (1 - \beta_j) + T_o^n\beta_N. \quad (7)$$

The throughput of node $i$, $\Gamma_i, 1 \leq i \leq N$, is defined as the number of bits that node $i$ successfully transmits in a time duration of $\Omega$. We have

$$\Gamma_i = \frac{L_iP_i}{\Omega}, \quad (8)$$

where $P_i$ is the successful transmission probability of node $i, 1 \leq i \leq N$, where

$$P_i = \beta_i\Pi_{j=1}^{N} (1 - \beta_j). \quad (9)$$

B. Exact Solution to the Optimal $\beta$

The exact solution to the optimal $\beta$ can be found in the following five steps.

Step 1: Express $\beta_{n+i}, 1 \leq i \leq m$, in terms of $\beta_{n+1}$. From (4), (9) and (8), we have

$$r_i = \frac{\Gamma_{n+i}}{\Gamma_{n+1}} = \frac{\beta_{n+i}(1 - \beta_{n+1})L_{n+i}}{\beta_{n+1}(1 - \beta_{n+1})L_{n+1}}. \quad (10)$$

Then $\beta_{n+i}$ can be expressed in terms of $\beta_{n+1}$, namely

$$\beta_{n+i} = \frac{r_i\beta_{n+1}L_{n+i}}{(1 - \beta_{n+1})L_{n+i} + r_i\beta_{n+1}L_{n+1}}, 1 \leq i \leq m. \quad (11)$$

Step 2: Express $\beta_i, 1 \leq i \leq n$, in terms of $\beta_1$. Note $\frac{\Gamma_i}{\Gamma_1} = \frac{a_i}{a_1}$ and regard $\frac{a_i}{a_1}$ as the throughput ratio between nodes $i$ and 1. From (11), we have

$$\beta_i = \frac{\frac{a_i}{a_1}\beta_1L_1}{(1 - \beta_1)L_i + \frac{a_i}{a_1}\beta_1L_1}, 1 \leq i \leq n. \quad (12)$$

Step 3: Setup a relationship between $\beta_{n+1}$ and $\beta_1$. After substituting (9), (5) and (7) into (8), we rewrite $\Gamma_1 = a_1$ as

$$a_1 = \frac{L_1\beta_1\Pi_{i=2}^{N} (1 - \beta_i)\Pi_{i=1}^{m} (1 - \beta_{n+i})}{\sigma\Pi_{i=1}^{N} (1 - \beta_i) + \sum_{i=1}^{N-1} T_o^n\beta_i \prod_{j=1}^{N} (1 - \beta_j) + T_o^n\beta_N}. \quad (13)$$

Further, substituting (11) and (12) into (13), we obtain an implicit relationship between $\beta_{n+1}$ and $\beta_1$.

Step 4: Express $\Sigma_{i=1}^{N}\Gamma_i$ in terms of $\beta_{n+1}$ and $\beta_1$. With (3) and (4), the system throughput $\Sigma_{i=1}^{N}\Gamma_i$ is written as

$$\Sigma_{i=1}^{N}\Gamma_i = \Sigma_{i=1}^{N} a_i + \Gamma_1\Pi_{i=1}^{m} r_i \quad (14)$$

$$= \Sigma_{i=1}^{N} a_i + \beta_{n+1}(1 - \beta_1)L_{n+1} \beta_1(1 - \beta_1)L_1 a_1\Sigma_{i=1}^{m} r_i, \quad (15)$$

where from (14) to (15), we use the expression of $\frac{L_{n+i}}{L_n}$, which can be obtained according to (9) and (8).

Step 5: Find the optimal $\beta$. We first search all pairs of $\beta_{n+1}$ and $\beta_1$ that satisfy (13), then choose their optimal values maximizing (15), and finally calculate other $\beta_i$s by (11) and (12).

In general, it is not easy to know whether the exact solution exists and is unique. We therefore seek the approximate solution in the next subsection and prove that the solution is uniquely exist.

C. Approximate Solution to the Optimal $\beta$

In this section, we first specify the method to calculate the approximate solution to the optimal $\beta$, and then we prove the existence and uniqueness of the approximate solution.

1) Calculation of the Optimal $\beta$: In order to find the approximate solution to the optimal $\beta$, we first adopt a key approximation, $\beta_i \ll 1$, which is widely used in the related literatures such as [4]. The approximation holds true since $\beta_i$ represents the per-node attempt rate in a very short slot and therefore it is generally much small. And then, we repeat and modify five calculation steps in Section III-B as:

Step 1: Express $\beta_{n+i}, 1 \leq i \leq m$, in terms of $\beta_{n+1}$. Based on the approximation, $\beta_i \ll 1$, (10) reduces to $r_i = \frac{\beta_{n+i}L_{n+i}}{\beta_{n+1}L_{n+1}}$, so we have

$$\beta_{n+i} = \frac{r_i\beta_{n+1}L_{n+i}}{L_{n+i}}, 1 \leq i \leq m. \quad (16)$$

Step 2: Express $\beta_i, 1 \leq i \leq n$, in terms of $\beta_1$. According to (16), (12) reduces to

$$\beta_i = \frac{a_i\beta_1L_1}{a_1L_1}, 1 \leq i \leq n. \quad (17)$$
TABLE I
PARAMETERS FOR 802.11b

<table>
<thead>
<tr>
<th>m/M</th>
<th>5/7</th>
</tr>
</thead>
<tbody>
<tr>
<td>δ</td>
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</tr>
<tr>
<td>T_n</td>
<td>228 μs</td>
</tr>
<tr>
<td>l</td>
<td>HEADER + PHEAD + SF + ACK + DIFS</td>
</tr>
<tr>
<td>SIFS</td>
<td>10 μs</td>
</tr>
<tr>
<td>DIFS</td>
<td>50 μs</td>
</tr>
<tr>
<td>Rmin</td>
<td>24 bytes @ Rmin + 14 bytes @ Rmax</td>
</tr>
<tr>
<td>Rmax</td>
<td>11 Mbps</td>
</tr>
<tr>
<td>L</td>
<td>24 bytes @ Rmin + 4 bytes @ Rmax</td>
</tr>
</tbody>
</table>

Step 3: Setup a relationship between β_{n+1} and β_1. We can obtain the relationship between β_{n+1} and β_1 by substituting (16) and (17) into (13).

Step 4: Express \Sigma_{i=1}^{N} \Gamma_i in terms of \beta_{n+1} and \beta_1. From the derivation of (14) and (15), (15) can be re-written as

\[ \Sigma_{i=1}^{N} \Gamma_i = \Sigma_{i=1}^{N} a_i + \frac{\beta_{n+1} L_{n+1}}{\beta_1 L_1} - \alpha_1 \Sigma_{i=1}^{m} r_i. \]

Step 5: Find the optimal β as like in Section III-B.

2) The Existence and Uniqueness of the Approximate Solution: In the following, we only consider a simple case of m = 1 and m ≥ 1, and prove that the approximate solution is uniquely exist. From the case of n = 1 and m ≥ 1, we have an insight into the existence and uniqueness of the general case of n > 1 and m ≥ 1.

With the approximation β_1 ≪ 1, we can calculate the per-node attempt rate \beta_i by

\[ \beta_i = \left\{ \begin{array}{ll} \sigma + L_2 \sum_{i=1}^{N-1} \omega_i e^\lambda, & i = 1, \ldots, N, \\ r_i^{-1} \beta_2 L_2, & i = 2, \ldots, N, \end{array} \right. \]  

where \sigma = \frac{T_i}{a_1} + \sigma - T_i^{1}, \omega_i = \frac{T_i^{1}}{L_1}, and \lambda = \beta_2 L_2 \sum_{j=1}^{m} r_j are constants when the total node number N, the packet size L_i and the throughput ratio r_j are given; \beta_2 is the unique solution to the function h(\beta_2) = 0, where h(\beta_2) = \sigma - \beta_2 L_2 \sum_{i=1}^{N} \omega_i e^{-\lambda}.

Proof: Please refer to the Appendix.

IV. MODEL VERIFICATION

In this section, we demonstrate the efficiency of our proposed APPLE scheme for wireless LANs. We use the 802.11e EDCA simulator [6] in NS2 version 2.28 [7] as a validation tool. In simulation, we differentiate the \textit{CW} parameter by substituting \textit{AIFS}, \textit{TXOP} = 0, and \textit{CW} = \textit{CW}_{\text{max}} = \textit{CW}_i for node \textit{i}. The other protocol parameter values are listed in Table I and are set by IEEE 802.11b. Each simulation run lasts 200 seconds.

In our experiment, the HP class has n = 2 nodes with the fixed throughput requirements: a_1 = 0.5 Mbps and a_2 = 1 Mbps. The LP class has m nodes with the proportional throughput ratios: r_1 = 1, (1 ≤ i ≤ 2) and r_2 = 2, (2 ≤ i ≤ m), where m = 4, 6, 8, ... 20. We set the packet size of two HP nodes to L_1 = L_2 = 500 bytes, and set the packet size of all LP nodes to L_3 = ... = L_N = 1500 bytes. We set \textit{CW}_i = \frac{2}{\beta_i} - 1 by (1) in simulation, where the exact and approximate solutions to \beta_i can be calculated in Section III-B and III-C, respectively. Table II shows the obtained values of \textit{CW}_i and the theoretical system throughput.

We now explain that the derived \textit{CW}_i can maximize the system throughput (as shown in Fig. 1), guarantee the fixed throughput requirement of HP nodes (as shown in Fig. 2), and guarantee the proportional throughput ratios of LP nodes (as shown in Fig. 3). In Figs. 1-3, the labels “ana_exact” and “ana_appx” denote the theoretical exact and approximate throughput, respectively; the labels “sim_exact” and “sim_appx” denote the simulation results based on the exact and approximate solutions, respectively.

Fig. 1 plots the system throughput vs. the number of LP nodes. From Fig. 1, we can see that 1) the sim_exact and sim_appx simulation curves closely match the ana_exact theoretical curve which plots the maximum system throughput limit, and 2) the ana_appx theoretical curve matches the ana_exact theoretical curve well with the nodes number increasing. This manifests that the proposed APPLE scheme can maximize the system throughput. In addition, the simulation shows that the maximum system throughput is a quasi constant regardless of how the node number varies.

Fig. 2 plots the per-node throughput of HP class vs. the number of LP nodes. There are 2 nodes in HP class. The fixed throughput requirements of nodes 1 and 2 are a_1 = 0.5 Mbps and a_2 = 1 Mbps, respectively. From Fig. 2, we can see that 1) the sim_appx simulation curves closely match the corresponding sim_exact simulation curves, respectively, and 2) each simulation value is almost equal to the corresponding target value, which is either a_1 = 0.5 Mbps or a_2 = 1 Mbps. This manifests that the proposed APPLE scheme can guarantee the fixed throughput requirements of HP class.

Fig. 3 plots the per-node throughput of LP class vs. the number of LP nodes. There are m nodes in LP class, where m varies from 4 to 20. The required throughput ratio between the first and later \frac{m}{2} nodes is 1:2. From Fig. 3, we can see that 1) the sim_appx simulation curves almost overlap with the corresponding sim_exact simulation curves, respectively, and 2) with the number of LP nodes increasing, the simulated throughput ratio between the first and later \frac{m}{2} nodes is still...
V. Conclusion

In wireless LANs, it is desirable to provide different levels of guaranteed services simultaneously for applications with different requirements. This paper proposes an APPLE scheme, which considers providing the absolute throughput guarantee for HP nodes, providing the proportional throughput guarantee for LP nodes, and at the same time maximizing the bandwidth utilization. We formulate the optimization problem, investigate the existence and uniqueness of the solutions. Simulations validate that the proposed APPLE scheme is very accurate.

APPENDIX

In this appendix, we prove (19) and the approximate solution to the case of $n = 1$ and $m \geq 1$ is uniquely exist.

Proof: We prove (19) and the approximate solution in three steps below.

Step 1: Express $\beta_{i+1}$, $1 \leq i \leq m$, in terms of $\beta_2$. From (16), we have

$$\beta_{i+1} = \frac{r_i \beta_2 L_i}{L_{i+1}}, 1 \leq i \leq m. \tag{20}$$

Step 2: Express $\beta_1$ in terms of $\beta_2$. After substitute (20) into (13) and apply the approximation, $(1 - x)^y \approx e^{-xy}$ for $x \ll y$, we have

$$\beta_1 = \frac{\sigma + \beta_2 L \sum_{i=1}^{N-1} \omega_i e^{\lambda}}{\varphi}. \tag{21}$$

where $\omega_i = \frac{r_i T_{i+1}}{T_i}$, $\varphi = \frac{T_i}{\lambda} + \sigma - T_i$ and $\lambda = \beta_2 L \sum_{j=1}^{i \leq m} \frac{r_j}{T_j}$ are constants when the total node number $N$, the packet size $L_i$ and the throughput ratio $r_i$ are given. Hence, we get (19).

Step 3: Prove that $\beta$ exists and is unique. First, we can express the system throughput $\Sigma_{i=1}^{N} \Gamma_i$ in terms of $\beta_2$. Then, (18) reduces to

$$\Sigma_{i=1}^{N} \Gamma_i = a_1 + \frac{L_2 \beta_2}{L_1} a_1 \Sigma_{i=1}^{m} \Gamma_i. \tag{22}$$

Substitute (21) into (22), then $\Sigma_{i=1}^{N} \Gamma_i$ is the function of $\beta_2$. So the optimal value for $\beta_2$ can be derived through setting the first-order derivative of $\Sigma_{i=1}^{N} \Gamma_i$ to zero, we get $h(\beta_2) = 0$. Due to the reasons that (i) $h'(\beta_2) < 0$, (ii) $h(0) > 0$ and $h(1) < 0$, the solution to $\beta_2$ must exist uniquely in domain $(0, 1)$. Further, the solution to $\beta$ must exist uniquely.
REFERENCES


