Power Control of DFIG in WECS Using Backstipping and Sliding Mode Controller

A. Boualouch, A. Essadki, T. Nasser, A. Boukhriss, A. Frigui

Abstract—This paper presents a power control for a Doubly Fed Induction Generator (DFIG) using in Wind Energy Conversion System (WECS) connected to the grid. The proposed control strategy employs two nonlinear controllers, Backstipping (BSC) and sliding-mode controller (SMC) scheme to directly calculate the required rotor control voltage so as to eliminate the instantaneous errors of active and reactive powers. In this paper the advantages of BSC and SMC are presented, the performance and robustness of this two controller’s strategy are compared between them. First, we present a model of wind turbine and DFIG machine, then a synthesis of the controllers and their application in the DFIG power control. Simulation results on a 1.5MW grid-connected DFIG system are provided by MATLAB/Simulink.

Keywords—Backstipping, DFIG, power control, sliding-mode, WESC.

NOMENCLATURE

- \( \rho \)  Air Density (kg/m\(^3\))
- \( \Omega_t \)  Tip Speed Ratio
- \( \lambda \)  Turbine Radius
- \( R \)  Rotor radius (m)
- \( v \)  Wind speed (m/sec)
- \( C_p \)  Power Coefficient
- \( \beta \)  Pitch angle
- \( T_{me} \)  Electromagnetic torque (Nm)
- \( V_{dc}, V_{qs} \)  Direct and Quadratic Stator Voltages
- \( i_{dq}, i_{qs} \)  Direct and Quadratic Stator currents
- \( \Phi_{ds}, \Phi_{qs} \)  Direct, Quadratic Stator Flux (Wb)
- \( P_s, Q_s \)  Active and reactive stator Power
- \( P_{ref}, Q_{ref} \)  Reference active and reactive stator Power
- \( R_r, R_s \)  Rotor and stator Resistance (\( \Omega \))
- \( L_r, L_s \)  Rotor and mutual Inductance (H)
- \( \rho \)  Pole pair number
- \( \theta_r \)  Rotor position
- \( \omega_s, \omega_r \)  Synchronous and Angular speed
- \( g \)  Slip

I. INTRODUCTION

THE wind energy conversion system WECS produce electricity from wind, it has several advantages, first it is an inexhaustible source, and then it does not pollute the environment, but in the other side, its cost remains high and its energy efficiency is still low compared to conventional sources [1], [2].

The Doubly Fed Induction Generator (DFIG) is the most used in high power wind production. The stator of DFIG is directly related to grid side, the rotor is connected to the grid by two converters AC/DC/AC. The advantage of this type of machine is its ability to operate over a large range of wind speeds with a lower rotor converter [3]-[5].

A vector control scheme is applied to the DFIG, which makes the DFIG similar to DC machine; it allows a decoupling of the active and reactive power in the DFIG. In the proposed controller, the machine parameters must be determined exactly, because it is used to calculate the controller parameters. The controller's robustness is affected following changes in these parameters [4].

These last years, several researches are about the nonlinear controllers such as Backstipping (BSC) and sliding mode control (SMC) which have enjoyed great success in recent years for their simplicity of implementation and robustness against disturbances which may affect process[6]-[8].

In this article and after modeling the wind turbine and DFIG, we have established a vector control to control the active and reactive power control using a SMC and BSC. The aim of this work is to present the performance and robustness of these controllers.

II. TURBINE MODEL

The mechanical power transferred from the wind to the aerodynamic rotor is [9]:

\[
P_w = \frac{1}{2} \rho R^3 \lambda^2 C_p (\lambda, \beta)
\]  (1)

The input torque in the transmission mechanical system is then [10]:
The power coefficient $C_p$ of the wind turbine given by [11]:

$$\frac{1}{\lambda} = \frac{1}{\lambda + 0.08\beta} + 0.035\beta^{1.3}$$

Fig. 2 shows the power coefficient for different values of $\beta$.

### III. DFIG MODEL

The mathematical models of three phases DFIG in the Park frame are written as [7]-[10]:

$$\begin{align*}
V_{d\omega} &= R_{d\omega}I_{d\omega} + \frac{d\Phi_{d\omega}}{dt} - \omega\Phi_{q\omega} \\
V_{q\omega} &= R_{q\omega}I_{q\omega} + \frac{d\Phi_{q\omega}}{dt} + \omega\Phi_{d\omega} \\
V_{d\alpha} &= R_{d\alpha}I_{d\alpha} + \frac{d\Phi_{d\alpha}}{dt} - \omega\Phi_{q\alpha} \\
V_{q\alpha} &= R_{q\alpha}I_{q\alpha} + \frac{d\Phi_{q\alpha}}{dt} + \omega\Phi_{d\alpha} \\
\Phi_{d\omega} &= L_{d\omega}I_{d\omega} + L_{m\omega}I_{q\omega} \\
\Phi_{q\omega} &= L_{q\omega}I_{q\omega} + L_{m\omega}I_{d\omega} \\
\Phi_{d\alpha} &= L_{d\alpha}I_{d\alpha} + L_{m\alpha}I_{q\alpha} \\
\Phi_{q\alpha} &= L_{q\alpha}I_{q\alpha} + L_{m\alpha}I_{d\alpha}
\end{align*}$$

The electromagnetic torques is expressed as [7], [9], [13]:

$$T_e = -\frac{3}{2}pL_{m\omega}(\Phi_{d\omega}I_{q\delta} - \Phi_{q\omega}I_{d\delta})$$

### IV. POWER CONTROL STRATEGY

To simplify the study of the power control strategy, we use a vector control of DFIG based on stator field oriented (SFO), by setting the stator field aligned with d-axis [7], [10], [13]. We have:

$$\Phi_{q\alpha} = 0 \quad \text{and} \quad \Phi_{d\alpha} = \Phi_{q\delta}$$

in this case the torque becomes:

$$T_e = -\frac{3}{2}pL_{m\omega}(\Phi_{q\delta}I_{d\delta})$$

This electro-mechanic torque and the reactive power depend only on the q-axis rotor current; the machines used in wind conversion are generally high power so we can neglect the stator resistance $R_s$ [14]. We can write:

$$\begin{align*}
\Phi_{d\omega} &= \Phi_{q\delta} = L_sI_{d\delta} + L_{m\omega}I_{q\delta} \\
\Phi_{q\omega} &= 0 = L_sI_{q\delta} + L_{m\omega}I_{d\delta}
\end{align*}$$

and

$$\begin{align*}
V_{d\delta} &= 0 \\
V_{q\delta} &= \omega\Phi_{d\delta}
\end{align*}$$

The statoric power is controlled by the rotor voltages $V_{rd}$ and $V_{rq}$, It is an independent control of active and reactive powers. In the d-q reference frame, the power can be written as:

$$\begin{align*}
P &= V_{q\delta}I_{d\delta} - V_{d\delta}I_{q\delta} = -L_{m\omega}\left(\frac{d\Phi_{d\delta}}{dt} - \frac{d\Phi_{q\delta}}{dt}\right)I_{q\delta} \\
Q &= V_{d\delta}I_{q\delta} - V_{q\delta}I_{d\delta} = L_{m\omega}\left(\frac{d\Phi_{d\delta}}{dt} - \frac{d\Phi_{q\delta}}{dt}\right)I_{d\delta}
\end{align*}$$

### V. SLIDING MODE CONTROLLER

In recent years the sliding mode controller has been very successful, it has three main features:
- Simplicity of implementation
- Robustness against system uncertainties
- External disturbances affecting the process.

The basic idea of sliding mode control is first to draw the states of the system in an area properly selected, then design a law command that will always keep the system in this region [14]. The sliding mode control goes through three stages:
The sliding mode control consists to return the state trajectory towards the sliding surface and to develop it above, with a certain dynamics up to the equilibrium [10], [11]. Its design consists mainly to determine three stages [7]-[15].

A. The Switching Surface Choice

For a non-linear system represented by:

\[
X = f(X,t) + g(X,t)u(X,t)
\]

\[
X \in \mathbb{R}^n, u \in \mathbb{R}
\]

(14)

where \( f(X,t), g(X,t), \) are two continuous and uncertain non-linear functions, supposed limited. The general equation to determine the sliding surface given by [15], [16]:

\[
S(X) = (d/dt + \lambda)^{-1} e
\]

\[
e = X^d - X
\]

\[
X^d = [x^d, \dot{x}^d, \ddot{x}^d, ...]^T
\]

\[
X = [x, \dot{x}, ..., x^{n-1}]^T
\]

where \( e \) is the size to resolve error, \( \lambda \) is positive coefficient, \( n \) is order of the system, \( X^d \) is desire greatness.

B. Convergence Condition

The convergence condition is defined by the Lyapunov equation [7], [8], [15]; it makes the surface attractive and invariant.

\[
S(X)S(X) \leq 0
\]

(16)

C. Control Calculation

The control algorithm is defined by the relation:

\[
u = u^s + u^n
\]

(17)

where \( u \) is control signal, \( u^s \) is equivalent control signal, \( u^n \) is switching control, sat \((S(X) / \varphi)\) is Saturation function, \( u^n \) can be obtained by considering the condition for the sliding regime:

\[
S(X,t) = 0.
\]

(18)

The equivalent control keeps the state variable on sliding surface, once they reach it. \( u^n \) is needed to assure the convergence of the system states to sliding surfaces in finite time.

In order to alleviate the undesirable chattering phenomenon, J. J. Slotine proposed an approach to reduce it, by introducing a boundary layer of width \( \varphi \) on either side of the switching surface [17].

Then, \( u^n \) is defined by:

\[
u^n = u^\text{maxsat}(S(X) / \varphi)
\]

(19)

where sat\((S(X))\) is the proposed saturation function and defined by:

\[
sat(S(X) / \varphi) = \begin{cases} 
\text{sign}(S) |S| > \varphi \\
\text{S} / \text{sat} |S| < \varphi 
\end{cases}
\]

(20)

\( \varphi \) is the boundary layer width, \( u^\text{max} \) is the controller gain designed from the Lyapunov stability. Commonly, in DFIG control using sliding mode theory, the surfaces are chosen according of the error between the reference input signal and the measured signals [17].

D. Power Control

To control the power we set \( n=1 \), the expression of the active and reactive power control surface becomes:

\[
S(P) = (P_{\text{ref}} - P_\text{r})
\]

\[
S(Q) = (Q_{\text{ref}} - Q_\text{r})
\]

(21)

The derivative of the surface is:

\[
S(P) = (P_{\text{ref}} - P_\text{r})
\]

\[
S(Q) = (Q_{\text{ref}} - Q_\text{r})
\]

(22)

Replacing it in the power expression:

\[
S(P) = (P_{\text{ref}} + V_\text{r}L_\text{r}I_\text{r})
\]

\[
S(Q) = (Q_{\text{ref}} - (V_\text{r}L_\text{r}I_\text{r})
\]

(23)

Taking the current expression from the voltage equation:

\[
S(P) = (P_{\text{ref}} + V_\text{r}L_\text{r}I_\text{r} + (V_\text{r} - R_\text{r}I_\text{r}))
\]

\[
S(Q) = (Q_{\text{ref}} + V_\text{r}L_\text{r}I_\text{r} + (V_\text{r} - R_\text{r}I_\text{r}))
\]

(24)

where

\[
\sigma = (1 - \frac{L_\text{r}^2}{L_\text{r}L_\text{r}})
\]

(25)
During the sliding mode and in permanent regime, we have:

\[
\begin{align*}
S(P) &= (P_{\text{ref}} - P) + \frac{L_v}{L_v + R} (V_{\text{o}} - V_{\text{o}}) \\
S(Q) &= (Q_{\text{ref}} - Q) + \frac{L_v}{L_v + R} (V_{\text{o}} - V_{\text{o}})
\end{align*}
\]

During the convergence mode, so that the condition is:

\[
\begin{align*}
S(P) &= 0, \dot{S}(P) = 0, V_{\text{o}}^* = 0 \\
S(Q) &= 0, \dot{S}(Q) = 0, V_{\text{o}}^* = 0
\end{align*}
\]

Verified, we set:

\[
\begin{align*}
S(P) &= -V_{\text{o}}^* + \frac{L_v}{L_v + R} V_{\text{o}} \\
S(Q) &= -V_{\text{o}}^* + \frac{L_v}{L_v + R} V_{\text{o}}
\end{align*}
\]

The switching term is given by:

\[
\begin{align*}
V_{\text{o}}^* &= K_{V_{\text{o}}} \sin S(P) \\
V_{\text{o}}^* &= K_{V_{\text{o}}} \sin S(Q)
\end{align*}
\]

K_{V_{\text{o}}} and K_{V_{\text{q}}} are positive constant given in Table III.

VI. BACKSTEPPING CONTROLLER

A. Principles Technique Backstepping

The basic idea of the Backstepping design is the use of the so-called virtual control to systematically decompose a complex nonlinear control design problem into simpler smaller ones [18]. Roughly speaking, Backstepping design is divided into various design steps [19], [20]. In each step we essentially deal with an easier, single-input-single-output design problem, and each step provides a reference for the next design step. The overall stability and performance are achieved by a Lyapunov function for the whole system [18].

B. Application of Backstepping for Machine Control

Research on the development of the DFIG control technology has multiplied in recent decades. We currently find several techniques present in the literature, such as vector control, DTC, nonlinear controls such as Backstepping and control sliding mode [21].

C. Power Control

We define the errors \(e_1\) and \(e_2\) representing the error between the actual power \(P_s\) and the reference power \(P_{\text{ref}}\) and the error between reactive power \(Q_s\) and its reference \(Q_{\text{ref}}\):

\[
\begin{align*}
e_1 &= P_s - P_{\text{ref}} \\
e_2 &= Q_s - Q_{\text{ref}}
\end{align*}
\]

The derivative of this equation gives:

\[
\begin{align*}
\dot{e}_1 &= P_{\text{ref}} - P_s \\
\dot{e}_2 &= Q_{\text{ref}} - Q_s
\end{align*}
\]

Therefore, the switching term is given by:

\[
\begin{align*}
V_{\text{o}}^* &= K_{\text{V_{o}}} \sin S(P) \\
V_{\text{o}}^* &= K_{\text{V_{q}}} \sin S(Q)
\end{align*}
\]

The pursuits of goals are achieved by choosing the references of the current components representing the stabilizing functions as:

\[
\begin{align*}
l_{\text{ref}} &= X \left[ k_1 e_1 + \dot{P}_{\text{ref}} + \frac{L_v}{L_v + R} (V_{\text{o}} - g \omega \beta I_{\beta} - \frac{L_v}{L_v + R} \frac{1}{a}) \right] \\
l_{\text{ref}} &= X \left[ k_2 e_2 + \dot{Q}_{\text{ref}} + \frac{L_v}{L_v + R} (V_{\text{o}} + g \omega \beta I_{\beta} \frac{1}{a}) \right]
\end{align*}
\]

with:

\[
X = \frac{L_v}{L_v + R} (\beta = L_v - \frac{L_v^2}{L_v + R} \alpha = L_v - \frac{L_v^2}{L_v + R})
\]

where \(k_1\) and \(k_2\) are positive constants given in Table IV (Appendix). The derivative of the Lyapunov function becomes:

\[
\dot{V}_e = -k_1 e_1^2 - k_2 e_2^2
\]
So, \( I_{qref} \) and \( I_{dref} \) in (40) are asymptotically stable. We define the errors \( e_3 \) and \( e_4 \) respectively representing the error between \( I_q \) and his reference \( I_{qref} \), and his reference \( I_{dref} \):

\[
\begin{align*}
    e_3 &= I_{qref} - I_q \\
    e_4 &= I_{dref} - I_d 
\end{align*}
\]

(42)

The derivative of this equation gives:

\[
\begin{align*}
    \dot{e}_3 &= I_{qref} - \frac{1}{\alpha} V_{\alpha} - S_1 \\
    \dot{e}_4 &= I_{dref} - \frac{1}{\alpha} V_{\phi} - S_2 
\end{align*}
\]

(43)

with

\[
S_1 = \frac{1}{\alpha} \left( R I_q - g_\omega \beta I_d - g \frac{L_q}{L_d} \right) \\
S_2 = \frac{1}{\alpha} \left( - R I_d + g_\omega \beta I_q \right) 
\]

(45)

(46)

Actual control laws of the machine \( V_d \) and \( V_q \) shown in (44), then we can go to the final step.

The final Lyapunov function is given by:

\[
V_z = \frac{1}{2} (e_3^2 + e_4^2 + e_3^2 + e_4^2) 
\]

(47)

The derivative of equation is given by:

\[
\dot{V}_z = e_3 \dot{e}_3 + e_4 \dot{e}_4 + e_3 \dot{e}_3 + e_4 \dot{e}_4 
\]

(48)

This can be rewritten as:

\[
\dot{V}_z = -k_3 e_3^2 - k_4 e_4^2 - k_3 e_3^2 - k_4 e_4^2 + e_3 \left( k_3 \dot{e}_3 + I_{qref} - \frac{1}{\alpha} V_{\alpha} - S_1 \right) + e_4 \left( k_4 \dot{e}_4 + I_{dref} - \frac{1}{\alpha} V_{\phi} - S_2 \right) 
\]

(49)

where \( k_3 \) and \( k_4 \) are positive constants given in the Appendix (Table IV). Control voltages \( V_d \) and \( V_q \) are selected as:

\[
\begin{align*}
    V_{\alpha} &= \alpha (k_3 \dot{e}_3 + I_{qref} - S_1) \\
    V_{\phi} &= \alpha (k_4 \dot{e}_4 + I_{dref} - S_2) 
\end{align*}
\]

(50)

which ensures that \( V_z < 0 \). The stability control is obtained by a good choice of gains: \( k_1, k_2, k_3 \) and \( k_4 \).

VII. SIMULATIONS AND RESULTS

Simulations of SMC and BSC control strategy for a DFIG based wind power generation system were carried out, using MATLAB/Simulink, and Fig. 1 shows the scheme of the implemented system. The DFIG is rated at 1.5 MW with its parameters given in Table I. The nominal converter dc-link voltage was set at 1400 V.

A. Reference Tracking

The machine speed is attached to 1600 rpm in ideal conditions, the active power reference \( P_{ref} \) is 0.75MW and 1.5MW (supply of power to the network). The reactive power reference \( Q_{ref} \) is -0.5MVAR (inductive), 0.25MVAR (capacitive) and 0MVAR (\( \cos \phi = 1 \)). Figs. 4 and 5 show the response of active and reactive power for DFIG by the SMC and BSC controller, Fig. 6 shows the rotoric and statoric currents.
From the figure, we can conclude a quicker response for BSC, and the answers are without overshoots, no effect coupling between two axes. The negative sign of the reactive power shows that the generator functions in capacitive mode, for inductive mode the power becomes automatically positive. In the end, the decoupling between the two axis is perfectly respected.

To reduce any possible overshoot of the reference voltage $V_{qr}$, it is often useful to add a voltage limiter.

**B. Robustness Test**

The parameters of the system are subject to changes driven by different physical phenomena, so our controller should provide good control whatever the variation of the generator parameters. In order to test the robustness of the controller we varied the rotor resistance $R_r$ to $1.5R_r$, and the inductance value of the rotor and stator decreased by 10% from its nominal value. Fig. 7 shows the effect of varying the parameters of the generator $R_r$, $L_s$, $L_r$, and $L_m$ on the response of the active and reactive power.

From simulation results, we found that the BSC is more robust, the response time is almost the same despite changes in the parameters of the DFIG.

**VIII. CONCLUSION**

The work presented in this paper devoted to power control of DFIG used in wind turbine by the sliding mode controller, after modeling the DFIG in the d and q axis, we have established a vector control of DFIG based in stator flux oriented, then the SMC are synthesized and compared to a conventional PI controller.

We have presented the performance of the BSC and SMC and compared between them, the robustness of the controllers is evaluated and allows us to have a decoupling between active and reactive power thus independent control.

The simulation results show that the BSC is much more efficient compared to SMC, it also improves the performance of the DFIG, and ensure some important strength despite the variation of the parameters of the DFIG.

**APPENDIX**

**TABLE I**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Quantity</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P$</td>
<td>Rated power</td>
<td>1.5MW</td>
</tr>
<tr>
<td>$V_s$</td>
<td>Stotoric voltage</td>
<td>690V – 50Hz</td>
</tr>
<tr>
<td>$V_r$</td>
<td>Rotoric voltage</td>
<td>389V-14Hz</td>
</tr>
<tr>
<td>$R_s$</td>
<td>Stotoric resistance</td>
<td>0.012Ω</td>
</tr>
<tr>
<td>$R_r$</td>
<td>Rotoric resistance</td>
<td>0.021Ω</td>
</tr>
<tr>
<td>$L_s$</td>
<td>Statoric inductance</td>
<td>0.0136H</td>
</tr>
<tr>
<td>$L_r$</td>
<td>Rotoric inductance</td>
<td>0.013H</td>
</tr>
<tr>
<td>$L_m$</td>
<td>mutual inductance</td>
<td>0.0135H</td>
</tr>
<tr>
<td>$p$</td>
<td>Pole pairs</td>
<td>2</td>
</tr>
<tr>
<td>$F$</td>
<td>The friction Coefficient</td>
<td>0.024N.m.s$^{-1}$</td>
</tr>
<tr>
<td>$J$</td>
<td>The moment of inertia</td>
<td>1000 kg.m$^2$</td>
</tr>
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</table>

**TABLE II**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Quantity</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R$</td>
<td>Radius of the wind</td>
<td>35.25 m</td>
</tr>
<tr>
<td>$G$</td>
<td>Gain multiplier</td>
<td>0.48</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Air density</td>
<td>1.225kg/m$^3$</td>
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TABLE III
SMC PARAMETERS

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kv1</td>
<td>5000</td>
<td>Without</td>
</tr>
<tr>
<td>Kv2</td>
<td>1800</td>
<td>Without</td>
</tr>
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</table>

TABLE IV
BSC PARAMETERS

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>k1</td>
<td>8060</td>
<td>Without</td>
</tr>
<tr>
<td>k2</td>
<td>5000</td>
<td>Without</td>
</tr>
<tr>
<td>k3</td>
<td>3590</td>
<td>Without</td>
</tr>
<tr>
<td>k4</td>
<td>6000</td>
<td>Without</td>
</tr>
</tbody>
</table>

REFERENCES


