Alternating Current Photovoltaic Module Model

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Abstract—This paper presents modeling of an Alternating Current (AC) Photovoltaic (PV) module using Matlab/Simulink. The proposed AC-PV module model is simple, realistic, and application oriented. The model is derived on module level as compared to cell level directly from the information provided by the manufacturer data sheet. DC-PV module, MPPT control, DC, VSI and LC filter, all were treated as a single unit. The model accounts for changes in variations of both irradiance and temperature. The AC-PV module proposed model is simulated and the results are compared with the datasheet projected numbers to validate model’s accuracy and effectiveness. Implementation and results demonstrate simplicity and accuracy, as well as reliability of the model.

Keywords—AC PV Module, Datasheet, Matlab/Simulink, PV modeling.

I. INTRODUCTION

PHOTOVOLTAIC (PV) systems design, simulation, analysis, and optimization require modellling of the system. As one of the core elements, PV module requires realistic and accurate modelling. A model that is simple and yet accounts for variations of parameters such as voltage and current based on irradiance and temperature fluctuations. Traditionally, modules are modelled on cell levels using Shockley equation and one (or two) diode equivalent models based on diode equivalent circuit and Shockley equation. Againg these models are on cell level and for DC-PV systems. Sangsawang and Chaitusaney [9] report module level model by modifying one-diode equivalent circuit to derive modified Shockley equation for a PV module. The authors claim the model uses additional calculation to find parameters not listed in datasheet. Sera et al. [10] follow the work of [9] and focus on finding parameters not listed in datasheet. Farivar and Assaeei [11] again loosely follow methods outlined by [9] and [10] while applying additional manipulations. Syed and Yazdani [12] presented PV module modeling on module level directly from datasheet that does not require any manipulation of Shockley equations, diode equivalent circuits, or calculation of extra parameters not listed in datasheet. However, the aforementioned model has also been modeled for DC-PV Systems. This paper presents an approach for modeling AC-PV module that is extracted directly from manufacturer datasheet. The proposed AC-PV module model is simple, requires no additional calculations, and accounts for irradiance and temperature variations. The proposed model shows no significant loss in accuracy and allows simple integration into Matlab/Simulink. The proposed model does not require crystalline structure details and does not use conventional Shockley equation. The model is validated for different irradiance (G) and temperature (T) as an individual module as well as a part of the multiple kW Utility Interactive (UI) PV System. The energy injected into the electric grid is validated to verify the accuracy of the AC-PV model. The rest of the paper is organized into the following sections: (II) PV Systems, (III) AC-PV Module Datasheet, (IV) AC-PV Module Model, (V) Simulation Results, and (VI) Conclusion.

II. PV SYSTEMS

Based on the type of current at the PV array level, PV systems can be broadly divided into DC-PV and AC-PV systems.

A. DC-PV System

A DC-PV system consists of a number of DC-PV modules connected in series-string to allow for a usably high DC voltage level and in parallel for higher DC current. This array, series-parallel combination of DC-PV modules, is built until the desired level of DC power is achieved, given by (1) to (3), where \( n_p \) is the number of modules in the string, \( n_s \) is the number of strings in parallel, \( V_{m} \) is string voltage, \( I_p \) is the net current of strings in parallel, \( V_m \) and \( I_m \) are module voltage and current, and \( P \) is the array power.

\[
V_s = n_s V_m
\]

\[
I_p = n_p I_m
\]

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Then DC-PV array is connected to grid through Maximum Power Point Tracking (MPPT) converter (optional), a DC-link Capacitor, and utility interactive Voltage Source Inverter (VSI). Perturb and Observe (PO) Maximum Power Point Tracking (MPPT) algorithm in conjunction with BC is used to track maximum power point and ensure maximum power delivery. Three phase two level Voltage Source Inverter (VSI) is used to convert DC into AC at 60 Hz and 208 V delivery. Three phase two level Voltage Source Inverter (VSI) track maximum power point and ensure maximum power.

DC wiring expertise is required for proper sizing of the array and installations. The number of modules in a string is usually limited by the system’s maximum V_DC (600V or 1000V); therefore, one usually has to deal with the high voltage on a string level. Also, the current in a series string is defined by and thus depends on the weakest link in the string (module with the lowest current). DC-PV system balance of system (BOS) such as DC fuses, conductors, disconnects, are also required, adding to the system’s cost, design complexity and installation time. DC BOS also cause increased power loss. In addition, central VSI results in single point of failure and cannot perform well in areas with shading and soiling (or snow). Output power of the DC-PV system is calculated using (3) and (4), where P_o,acpv is the AC output power (or power into the grid) of DC-PV system and d is the de-rating factor, usually 0.75 < d < 0.80. De-rating factor accounts for all the loss from DC-PV array to the grid.

\[ P_o = V_s I_p \]  
\[ P_{o,acpv} = d P_o \]  

**B. AC-PV System**

The NFPA 70 National Electrical Code (NEC) defines an AC module as a complete, environmentally protected unit consisting of solar cells, an inverter and other components, exclusive of a tracking system, designed to produce AC power from the sunlight. AC modules must be evaluated by a nationally recognized testing laboratory using both UL 1741 and UL 1703 as a single unit. Fig. 2 shows AC-PV module. Thus, AC-PV module is a DC-PV module with integrated micro-inverter (MI) that produces AC voltage and current at grid frequency and voltage rather than DC. In an AC-PV module there is no need to size array, no series or parallel strings, no current mismatch loss, no DC BOS, no DC loss, no shading/soiling/snow issues on one module affecting the others, and no single point of failure. In an AC-PV module we do not have to deal with high voltage and system performance is not partially defined by the weakest link. AC-PV module outperforms the DC-PV due to MI integrated MPPT on a module level rather than string or central level. In an AC-PV module there is no need for transformers or big capacitors and no fan for cooling is required. In addition, factory design, sizing and assembly ensures optimal performance and results in less installation time. Moreover, AC-PV system allows module level monitoring for performance and maintenance. Although AC-PV systems cost more than DC-PV systems, they yield energy improvements of up to 25% and are easier to design and install.

An AC-PV system consists of a number of AC-PV modules connected directly across AC system (grid) phases A, B, C and thus all the intermediary steps from PV array to the grid are eliminated. AC-PV modules are wired between two of the three phases. Typically during installation, for each AC-PV module wired between phases A-B, another is wired between phases B-C and yet another between phases B-C (Fig. 3). This installation pattern ensures equal distribution across phases and prevents from imbalance within the 3-phase system. In contrast to DC-PV system, the number of modules in an AC-PV system is limited by the line’s current capacity and defines the maximum number of AC-PV modules connected to an AC circuit. The aforementioned will result in \(17 \times 0.94 \approx 16A\), \(16A \times 1.25 = 20A\) AC-PV modules in a 20A branch circuit. The output power of AC-PV is given by (5), where \(P_{o,acpv}\) is the AC output power (or power into the grid), \(n_u\) and \(P_{ui}\) are the number of MIs and continuous output power of individual AC-PV module, respectively.

\[ P_{o,acpv} = n_u P_{ui} \]
listed are the nominal AC operating voltage, nominal frequency, maximum AC current, maximum AC power, branch circuit maximum over current protection device rating, and the number of AC-PV modules that can be attached. Table I tabulates the AC Electrical Data for Sunpower E19/240 AC solar panel.

In addition to the label listed parameters, Datasheets provide Power Factor, Total Harmonic Distortion, DC electrical data, mechanical data, testing conditions, etc. Table II tabulates DC Electrical Data for Sunpower E19/240 AC solar Panel.

As usual datasheets do not provide the series and shunt resistances, diode ideality constant, diode reverse saturation current, and the bandgap energy of the semiconductor. Therefore modeling on cell level using Shockley equation or diode equivalent circuit and on module level that require series/shunt resistances or extra manipulations are not possible. Conventional VI curves are not possible either.

IV. AC-PV MODULE MODEL

As pointed out earlier an AC-PV module is the UL certified combination of a DC-PV module and a MI as a single unit (Fig. 2). Therefore, AC-PV module modeling requires models of both DC-PV module and MI.

A. DC-PV Module Model

In a DC-PV module, there is a defined relationship between current (I_m) and irradiance (G) (Fig. 4 and also between module voltage (V_m) and temperature (T) (Fig. 5). However there is no significant relationship between I_m and T or between V_m and G. Therefore, the effects of T on I_m and G on V_m can be ignored for all practical purposes.

Thus, I_m as a function of G at a given instant of t, is given as:

$$I_{mt} = kI_{STC}$$

where, I_{STC} = module current at STC; G_{STC} = 1000 W/m^2; G_t = W/m^2 at time t; I_{mt} = module current at G_t, k = G_t / G_{STC}.$$

On the same note, PV module power, P_m as a function of G at a given instant of t, is given by:

$$P_{mt} = kP_{STC}$$

where, P_{STC} = module power at STC; P_{mt} = module power at t.

Equation (8) is used to account for temperature variations:

$$P_{mt} = [P_{STC}C_p(T_m - T_r)]$$

where, C_p = module power temperature coefficient; T_m = module operating temperature; T_r = module reference (STC) temperature; P_{mt} = change in module power at temperature T.

Combining (7) and (8) results in the module behavior with respect to both irradiance and temperature:
where, \( P_m \) is the module power as a function of both \( G \) and \( T \) at a given instant.

\[
P_m = P_{mt} + P_{mT} \tag{9}
\]

In a similar way, the PV module voltage as a function of temperature is given by:

\[
V_m = V_{OC} + V_{mT} \tag{10}
\]

where, \( V_{mT} = V_{OC}C_{V}(T_m - T_r) \) is module voltage at temperature \( T \); \( V_{OC} \) = module open circuit voltage at STC; \( C_V \) = module voltage temperature coefficient.

As pointed out earlier, changes in irradiance do not change the voltage significantly; therefore, changes in \( V \) due to variations in \( G \) are ignored.

Dividing (9) by (10) gives module current (\( I_m \)) in terms of given \( G \) and \( T \):

\[
I_m = P_m/V_m \tag{11}
\]

DC-PV module model based on (9), (10), and (11) is shown in Fig. 6 and can easily be modeled in Matlab/Simulink. All the values for variables in (9), (10), and (11) are obtained directly from DC electrical data of Datasheet.

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**B. Micro-Inverter Model**

Both BC and VSI need to be modeled as parts of the DC-PV model to develop a true AC-PV module model. The MI shown in Fig. 2 (the shaded box) is modeled as BC, POMPPT, and a single phase full-bridge (FB) VSI. BC (shaded box) and FB-VSI (dashed box) are shown in Fig. 8.

**i) PO MPPT Control**

Maximum power point (\( P_{mp} \)), i.e., the point of operation for a DC-PV module with maximum voltage (\( V_{mp} \)) and maximum current (\( I_{mp} \)), lies around the knee of the IV curve (Fig. 9).

The output of the DC-PV model is converted into current using controlled current source (Fig. 7). Capacitor is used to supply \( V_{in} \) for the BC. Inputs \( G \) and \( T \) are used to model effects of irradiance and temperature across the model.
Maximum power point is approximated by:

\[ V_{mp} = 0.80V_{DC} \] (12)

Depending on the operating conditions such as irradiation and temperature, POMPPPT control algorithm continuously adjusts the voltage and current of DC-PV module to ensure \( P_{mp} \) operation. PO algorithm is an iterative process shown in Fig. 10. The operating point is perturbed (1: present V & I measured \& Present P calculated), system response is observed (2: past and present Ps are compared and the direction of the next step/perturbation is determined), (3: based on whether the recent P is greater or less than the previous P). This process mimics the hill-climbing phenomenon to reach the peak of the mountain (maximum power point with \( V_{mp} \) \& \( I_{mp} \)). This way DC-PV module is ensured to operate at mpp.

![Image](image_url)

Fig. 10 POMPPPT algorithm

ii) Boost Converter

VSI requires stiff DC voltage equal to or greater than \( \sqrt{2}V_s \) at the input for satisfactory operation (13). However, the output voltage of the DC-PV module depends on the number of series-connected-cells. The output voltage is usually less than 50V and varies with changes in temperature. The output voltage is inversely related to the temperature, i.e., DC-PV module has the highest output voltage for the lowest temperature and the lowest output voltage for the highest temperature. During operation this voltage continuously varies between the two extremes and PO MPPT control supplies \( V_{mp} \) (12) at given irradiance and temperature. Therefore, BC is required to keep voltage fixed at the required level \( (\text{given by (13)}) \), by varying \( D \), DC-PV voltages between the lowest and the highest. Output voltage of BC is given by (14). \( D \) (15) is the duty cycle and can assume any value between 0 and 1. Capacitor C (16) is chosen according to the required amount of output voltage ripple. BC is operated in CCM mode, by choosing \( L \) greater than \( L_{min} \) (to ensure \( I_L \) greater than \( I_{LB} \)) (17).

\[ V_{DC} \geq \sqrt{2}V_i \] (13)

\[ V_D = \frac{1}{1-D}V_i \] (14)

\[ D = \frac{T_{on}}{T} \] (15)

\[ C_D = \frac{T_{on}}{2V_D}DT' \] (16)

\[ L \geq L_{min} = \frac{V}{2I_{LB}}D(1-D)V_O \] (17)

iii) Voltage Source Inverter

FB-VSI has four switches and is used to convert DC power into AC power at desired voltage and frequency. The Switches are controlled to adjust the output voltage and frequency, in this case equal to grid voltage and frequency. Anti-parallel diodes are connected across switching devices to allow reverse current flow. VSI requires a stiff DC voltage source at input [1] for quality operation.

The dashed box in Fig. 8 shows a FB-VSI circuit. VSI has two legs each with two switches and two anti-parallel diodes. Leg-1 comprising S1, S3, D1 and D3 (aka Half-Bridge Inverter (HBI)) is the basic building block of this type of inverters. FB-VSI has two HBIs. To ensure proper operation of the bridge and to avoid short circuit no two switches of the same HBI should be turned on simultaneously.

Though output voltage can be controlled by adjusting \( V_{DC} \), usually the more convenient method of pulse width modulation (PWM) is used. PWM adjusts the pulse width by controlling on and off times of the switches to produce the desired output voltage. In Sinusoidal PWM, the on and off commands for switches are produced by comparing a modulating signal \( (V_{mod}) \) with a triangular carrier wave \( (V_C) \) to produce appropriate gating sequence for the switches. Frequency of the carrier wave \( (f_c) \) is selected adequately higher than the frequency of the modulating signal \( (f_m) \), usually equal to or greater than 10 times \( f_m \) for proper operation. The VSI rms output voltage and frequency are determined by \( f_m \) and the amplitude of \( V_{mod} \), respectively. Both the unipolar (using one carrier wave) and bipolar (using two carrier wave) modulation techniques are employed; however, the latter is preferred due to ease of implementation. Output voltage is given by (18), with \( V_A \) and \( V_B \) given by (19) and (20).

\[ V_D = V_A - V_B \] (18)

\[ V_A = \left(\frac{f_m}{f}\right)V_{DC} \] (19)

\[ V_B = \left(\frac{f}{f_m}\right)V_{DC} \] (20)

with \( t_{on} \) given by (21) and using (15), (19) and (20), (18) can be re-written as (22). Equation (22) shows that the amplitude of VSI output can be adjusted by varying D.

\[ t_{off} = T - t_{on} \] (21)

\[ V_O = (2D - 1)V_{DC} \] (22)
iv) PWM Control

As shown in Fig. 11, DC input voltage ($V_{DC}$), supplied by BC, at the input of VSI is measured and compared against the reference voltage given by (13). Produced voltage error ($V_{E}$) is applied across PI or lead-lag voltage-control compensator for processing. Output of the compensator ($i_d$), being DC in nature, is multiplied by $\sqrt{2}$ and $\sin\theta$ to get peak sinusoidal reference current ($i_{Dp}$ equal to $I_{Dp}\sin\theta$), synchronized with the grid voltage $V_s$. The sinusoidal reference current is compared against measured sinusoidal current ($i_s$) and error applied across current-control compensator to track reference current with no or minimal error. Output of the current-control compensator is applied across PWM controller to produce switching sequence for the FB-VSI switches.

![PWM Control Diagram](image)

**V. SIMULATION RESULTS**

To evaluate the effectiveness of the proposed model of the AC-PV module directly from datasheet, the model was simulated firstly as an individual ACOPV module, secondly as 675W, 3-ACOPV modules, one across each pair of phases and finally as a 4 kW system. ACOPV module Sunpower E19/240 AC module datasheet is used for modeling.

**A. Model as an AC-PV Module**

The model of the AC-PV module as a complete unit, producing AC at grid frequency and voltage is connected to the grid. The point of common coupling has a voltage of 208 VLL and a frequency of 60 Hz. The proposed AC-PV module model is connected between phases A and B and can supply 225 W of continuous power at max.

Fig. 12 shows $V_s$, $i_s$ and output power ($P_o$) of the individual AC-PV module model. $V_s$ equals 208V with peak amplitude of 294V. Current $i_s$ varies with changes in G and has rms value of 1.08A (225W/208V) with a peak of 1.53A. $P_o$ equals the reference power ($P^*$) minus loss. From sometime before 5 seconds up to almost 8 seconds the $P^*$ equals to 240 W (a DC-PV module power at STC); however, $P_o$ is limited to 225W, the continuous output power of the MI. In Fig. 13 we have zoomed in on a small section of Fig. 12 in order to reveal the sinusoidal nature of $V_s$ and $i_s$ as well as their rms values.

![Graphs of $V_s$, $i_s$, and $P_o$](image)

**B. Model as AC-PV Module across Each Pair of Phases**

To verify the effectiveness of the proposed AC-PV module model as a part of the system, a 675 W system is connected across the grid at point of common coupling with 208 VLL and 60 Hz frequency. AC-PV modules are evenly distributed among the three phases to keep the power system balanced. Thus, one AC-PV module is connected between phases A and B, another one between B and C, and another between C and A. Each AC-PV module produces 225 W of continuous power, thus the total power of the system is 225 x 3 = 675 W.

![Graphs of $V_s$, $i_s$, and $P_o$ for 675W system](image)
Fig. 14 shows $V_{abc}$, $i_{abc}$ and output power ($P_o$) of the AC-PV module model based PV system. $V_{LL}$ equals 208V with phase peak amplitude of 294V. Three phase currents, $i_{abc}$, vary with changes in $G$ and phase current has rms value of 1.08A with a peak of 1.53A. $P_o$ equals the reference power ($P^*$) minus loss and varies with changes in $G$. $P_o$ equals 675W when $P^*$ equals 720W at STC.

In Fig. 15 we have zoomed in on a small section of Fig. 14 in order to reveal the sinusoidal nature of $V_{abc}$ and $i_{abc}$ as well as their rms values.

C. Model as 4kW System

Finally, effectiveness of the proposed AC-PV module model as a part of the 4kW system was simulated. As usual AC-PV modules were evenly distributed among the three phases to keep the power system balanced. Thus, 6 AC-PV module were connected between phases A and B, 6 between B and C, and another 6 between C and A. Each AC-PV module produces 225 W of continuous power. Thus the total power of the system was $225 \times 18 = 4050$ W.

VI. CONCLUSION

AC-PV module was modeled directly from the data provided by the manufacturer in a datasheet and without using diode equivalent(s) or Shockley equation. Modeling was done on the module level rather than the cell level, treating AC-PV module as a single unit complete system. The proposed model is simple and accurate and yet accounts for the effects of irradiance and temperature. The model was simulated in Matlab/Simulink and simulation results confirmed the model’s adequacy.

REFERENCES